

# CS:5810 Formal Methods in Software Engineering

## Reactive Systems and the Lustre Language<sup>1</sup> Part 3

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Introduction to contract-based compositional reasoning and its advantages

Introduction of new specification language aimed at facilitating

- modular development and
- compositional reasoning

Discussion of

- implementation in Kind 2 model checker
- examples of contract-based specifications

# Compositional Reasoning: Assume-Guarantee Paradigm

Setting:

- (Reactive) system is composed of several components
- Every component is provided with its own **high-level** behavioral specification
- The high-level specification of a component  $C[x, y]$  with inputs  $x$  and outputs  $y$  is provided by a **contract**:
  - a set  $\mathcal{A}[x, y]$  of **assumptions** on  $C$ 's current input and past I/O behavior
  - a set  $\mathcal{G}[x, y]$  of **guarantees** on expected behavior, provided assumptions  $\mathcal{A}[x, y]$  hold

## Assume-Guarantee Reasoning (simplified form)

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**Def.**  $C$  *respects* its contract  $\langle \mathcal{A}, \mathcal{G} \rangle$  if all of its executions (i.e., traces) satisfy

$$\text{always } \mathcal{A} \Rightarrow \text{always } \mathcal{G}$$

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**Def.**  $C_1[x_1, y_1]$  *uses*  $C_2[x_2, y_2]$  if it feeds  $C_2$  some input  $\mathbf{i}$  and reads the corresponding output in  $\mathbf{o}$

$C_1$  uses  $C_2$  *safely* if  $C_1$ 's executions satisfy **always**  $\mathcal{A}_2[\mathbf{i}, \mathbf{o}]$

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$C_1$  uses  $C_2$  *safely* if  $C_1$ 's executions satisfy **always**  $\mathcal{A}_2[i, o]$

**Obs.** If

- 1  $C_1$  uses  $C_2$  safely and
- 2  $C_2$  respects its own contract  $\langle \mathcal{A}_2, \mathcal{G}_2 \rangle$

then  $C_2$  can be abstracted by  $\mathcal{A}_2[i, o] \wedge \mathcal{G}_2[i, o]$  in  $C_1$

# CocoSpec: a Contract Language for Kind 2

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An extension of Lustre with contracts

Objectives:

- follow **assume-guarantee** paradigm
- ease process of writing and reading formal specifications
- enable **modular** and **compositional** analysis
- facilitate automatic verification of specs
- improve feedback to user after analysis
- partition information for **specification-driven** test generation

# Contract-based specification

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A contract for a component  $C$

- describes **declaratively**  $C$ 's **behavior** under some **assumptions**
- captures **requirements from specification** documents



# Contract Example



stopwatch(`toggle`, `reset`: bool)  $\rightarrow$  `count`: int

## Assumptions:

reasonable input  $\neg(\text{reset} \wedge \text{toggle})$

## Guarantees:

output range `count`  $\geq 0$ , initially 0

resetting `reset` implies `count` is 0

running  $\neg \text{reset} \wedge \text{on}$  implies `count` increases by 1

stopped  $\neg \text{reset} \wedge \neg \text{on}$  implies `count` does not change

## Contract Example in Kind 2

```
node stopwatch(toggle, reset: bool) returns (c: int);
(*@contract
  var on: bool = toggle ->
    (pre on and not toggle) or (not pre on and toggle) ;

  assume not (reset and toggle) ;
  guarantee (0 <= c and c <= 1) -> 0 <= c ;

  guarantee reset => c = 0 ;
  guarantee (not reset and on) => c = (1 -> pre c + 1) ;
  guarantee (not reset and not on) => c = (0 -> pre c) ;
*)
let ... tel
```

# Contracts as an Abstraction Mechanism

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A component's contract is usually **simpler** than the component's definition

A contract is a **declarative over-approximation** of the component

Contracts enable **modular** and **compositional** analyses in alternative to a **monolithic** one

In compositional analyses we **abstract away** the complexity of a subsystem by its contract

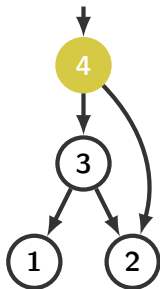
# Monolithic Analysis

Monolithic:

- analyze the top level
- considering the whole system

However:

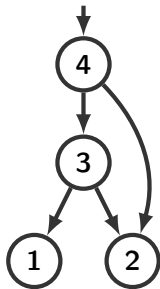
- complete system might be **too complex**
- changing subcomponents **voids old results**
- correctness of subcomponents is not addressed



# Modular Analysis

Modular:

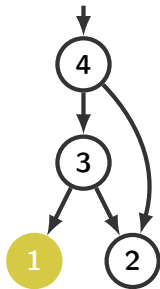
- analyze all components bottom-up
- **reusing results** from subcomponents



# Modular Analysis

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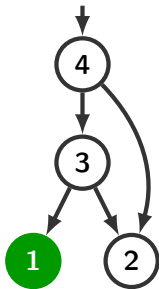
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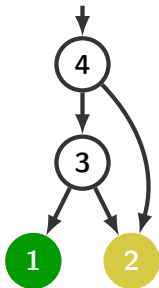
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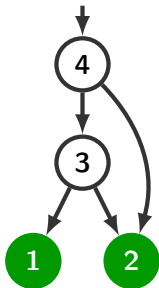




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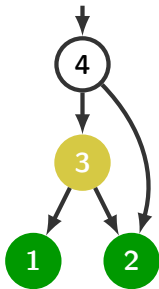
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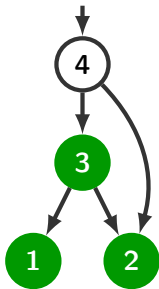
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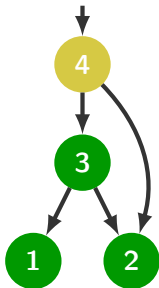
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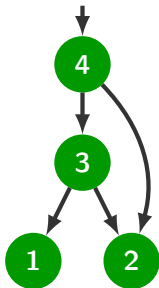
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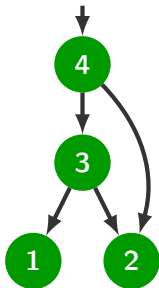
# Modular Analysis

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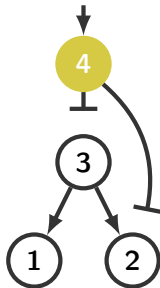
- changing subcomponents **voids old results**
- complexity can explode as we go up



# Compositional Analysis

Compositional:

- analyze the top level
- **abstracting subnodes** by their contracts
- complexity of the system analyzed is reduced
- changing subcomponents **preserves old results** as long as new version respects contract



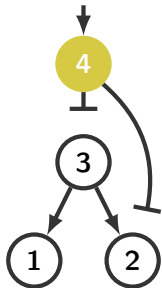
# Compositional Analysis

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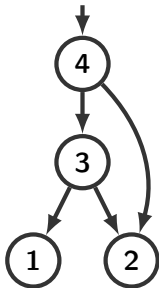
- counterexamples **might be spurious**
- correctness of subcomponents is assumed





# Compositional and Modular

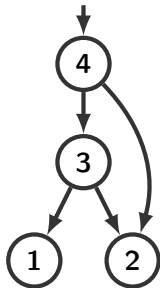
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# Compositional and Modular

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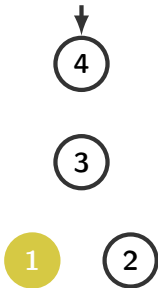
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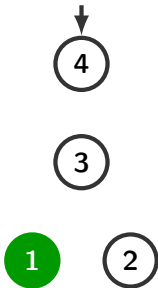
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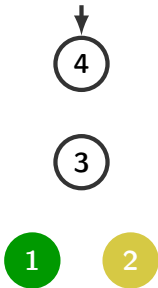
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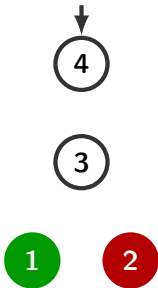
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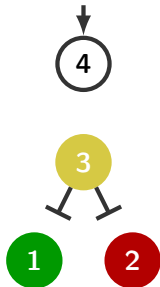
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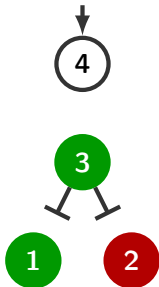
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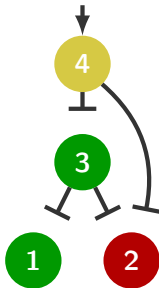




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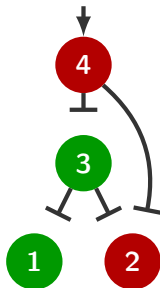
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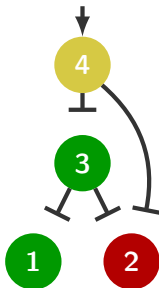
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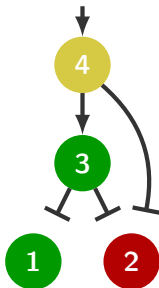
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In case of **failure** we can restart the analysis after refining by removing the abstraction, possibly repeatedly



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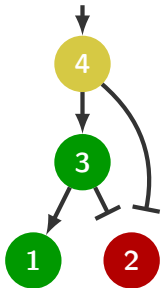
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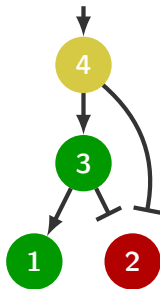
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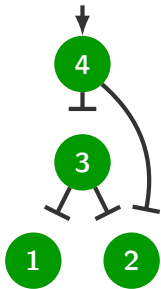
- no abstraction for the leaf components
- as we move up, we abstract subcomponents  
In case of **failure** we can restart the analysis after refining by removing the abstraction, possibly repeatedly
- all components are checked
- changing subcomponents **preserves old results** (as long as new versions are correct)
- results for subcomponents are reused
- refining identifies spurious counterexamples



## Compositional and Modular: Benefits

If all components are valid, **without refinement**:

- the system as a whole is correct
- changing a component by a different, **correct** one does not impact the correctness of the whole system



## Compositional and Modular: Benefits

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If all components are valid, **with refinement**:

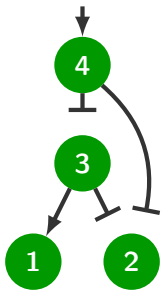
- the system as a whole is correct
- but the contracts are **not good enough** for a compositional analysis to succeed

Refinement gives hints as to why



## Compositional and Modular: Benefits

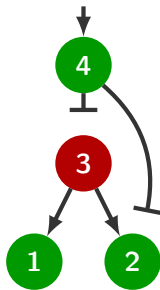
If we had to refine component 1 to prove 3 correct, that's probably because 1's contract is **too weak**



# Compositional and Modular: Benefits

If after refining all sub-components we still cannot prove 3 correct, that's because

- the assumptions of 3 are **too weak**, and/or
- the guarantees of 3 **do not hold**



# Modes

---

Often, specifications are *contextual (mode-based)*:

when/if this is the case, do that

# Modes: Example



stopwatch(**toggle**, **reset**: bool)  $\rightarrow$  **count**: int

## Assumption:

- reasonable input  $\neg(\text{reset} \wedge \text{toggle})$

## Guarantee:

- output range **count**  $\geq 0$ , initially 0

## Modes:

	<b>require</b>	<b>ensure</b>
• resetting	<b>reset</b>	<b>count</b> is 0
• running	$\neg\text{reset} \wedge \text{on}$	<b>count</b> increases by 1
• stopped	$\neg\text{reset} \wedge \neg\text{on}$	<b>count</b> does not change

# Modes

---

Often, specifications are *contextual (mode-based)*:

when/if this is the case, do that

*Assume-Guarantee contracts do not adequately capture this sort of specifications . . .*

. . . because modes are simply encoded as conditional guarantees

*Represent modes explicitly in the contract*

A **mode** consists of a *require* (**req**) and an *ensure* (**ens**) clause

- expresses a **transient behavior**
- corresponds to a guarantee **req**  $\Rightarrow$  **ens**

**Effect:** Separation between

- **global behavior** (guarantees) and
- transient behavior (modes)

# Modes in a Contract

A set of modes  $M$  can be added to a contract

Its semantics is an assume-guarantee pair  $\langle \mathcal{A}, \mathcal{G} \rangle$  with

$$\begin{aligned}\mathcal{A} &\equiv \bigvee_{m \in M} \text{req}_m \\ \mathcal{G} &\equiv \bigwedge_{m \in M} (\text{req}_m \Rightarrow \text{ens}_m)\end{aligned}$$

**Note:**  $\text{req}_m$ 's need not be mutually exclusive

# Modes: Example

stopwatch(**toggle**, **reset**)  $\rightarrow$  **count**

```
var on: bool = toggle -> (pre on and not toggle) or  
                        (not pre on and toggle) ;
```

## Assumption:

- reasonable input  $\neg(\mathbf{reset} \wedge \mathbf{toggle})$

## Guarantee:

- output range  $\mathbf{count} \geq 0$ , initially 0

## Modes:

	<b>require</b>	<b>ensure</b>
• resetting	<b>reset</b>	<b>count</b> = 0
• running	$\neg\mathbf{reset} \wedge \mathbf{on}$	<b>count</b> increases by 1
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# Modes: Advantages

---

*Detect shortcomings in the specification:*

- do the modes cover **all situations** the assumptions allow?
- enables **specification-checking** before model-checking

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*Produce better feedback for counterexamples:*

- indicate which modes are **active** at each step
- provide a **mode-based abstraction** of the concrete values
- abstraction is in terms of **user-specified** behaviors

# Contracts for Lustre

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Kind 2's input language extends Lustre with contracts

A **Kind 2 contract** is

- a set of assumptions,
- a set of guarantees, and
- a set of modes

Can contain *internal* variables

It can use *specification* nodes

Can be *inlined* in a node or *stand-alone*

Stand-alone contracts can be **imported** and **instantiated**

# Stand-alone Contract with Modes

```
contract stopwatch_spec(tgl, rst: bool) returns (c: int) ;
let
  var on: bool = tgl -> (pre on and not tgl) or (not pre on and tgl) ;

  assume not (rst and tgl) ;
  guarantee c = 0 -> c >= 0 ;

  mode resetting (
    require rst ; ensure c = 0 ; ) ;
  mode running (
    require not rst and on ; ensure c = (1 -> pre c + 1) ; ) ;
  mode stopped (
    require not rst and not on ; ensure c = (0 -> pre c) ; ) ;
tel

node stopwatch(toggle, reset: bool) returns (count: int) ;
(*@contract import stopwatch_spec(toggle, reset) returns (count) ; *)
let ... tel
```

# Additional Features

In contracts, one can

- refer to modes in formulas (with `::<mode_name>`)
- call **contract-free** nodes

```
node count(b: bool) returns (count: int) ;
let
  count = (if b then 1 else 0) + (0 -> pre count) ;
tel

contract stopwatch_spec(tgl, rst: bool) returns (c: int) ;
let
  ...
  mode running (...) ;
  mode stopped (...) ;
  ...
  guarantee not (::running and ::stopped) ;
  guarantee count(::resetting) > 0 => c < count(true) ;
tel
```

## Modes in Kind 2: Advantages

---

### Defensive check:

- modes **must** cover **all reachable states**
- **may** be declared as **mutually exclusive**

Check performed on the spec, **independently of the implementation**

## Modes in Kind 2: Advantages

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### Defensive check:

- modes **must** cover **all reachable states**
- **may** be declared as **mutually exclusive**

Check performed on the spec, **independently of the implementation**

### Mode references:

- can refer to a mode directly as a propositional var
- can write more **robust / trustworthy spec**
- can express guarantees **about the spec easily**

## Modes in Kind 2: Advantages

---

### Mode reachability:

- modes provide a finite abstraction of component  
(abstract state at time  $i$  = set of modes active at time  $i$ )
- can explore graph of connected modes
- from the initial state (BMC style)
- to compare with user's understanding



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- to compare with user's understanding

### Abstraction for counterexample (cex) traces:

- cex traces feature **concrete values** and can be hard to read
- we can **annotate states with active modes**
- therefore abstracting the states using **user-provided information**

## Modes in Kind 2: Advantages

---

### Test generation:

- can generate **witnesses** for abstract executions
- thus obtaining **specification-based, implementation-agnostic** test cases from the model

# Conclusion

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## Mode-based Assume-Guarantee Contracts:

- **more scalable** verification thanks to compositional reasoning
- bring contract language **closer to specification documents**
- **improve** user feedback (blame assignment, abstract cex traces)
- **raise trust** in specification, improve maintainability, ...
- enable **specification-based** test generation