
22c181: Formal Methods in Software Engineering

The University of Iowa

Spring 2008

Introduction to OCL

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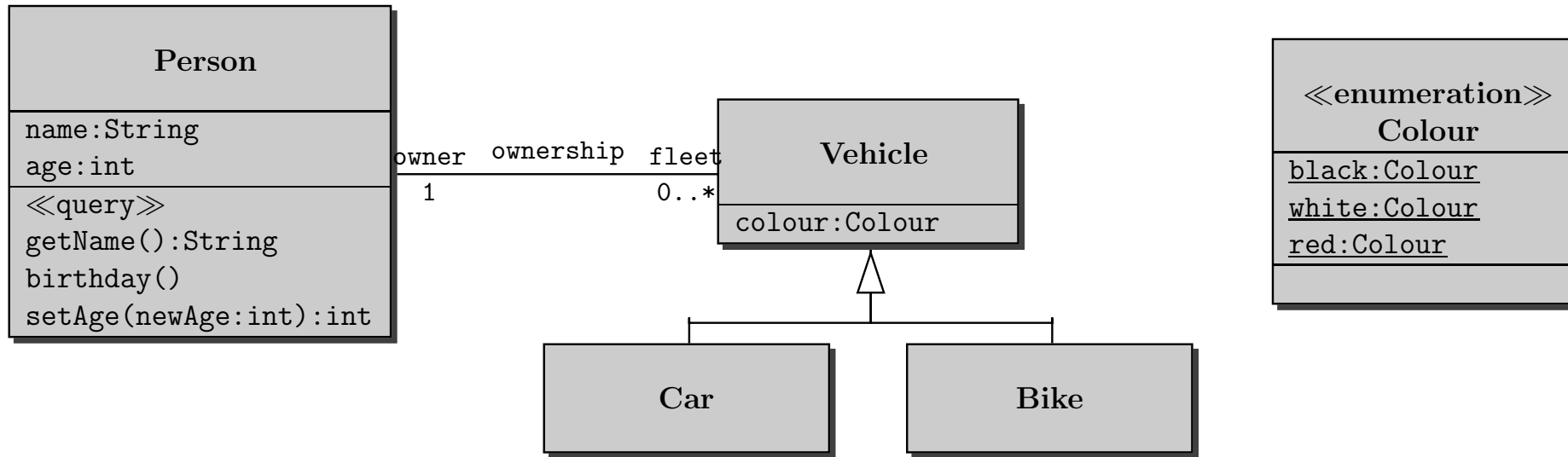
Contents

- Overview of KeY
- UML and its semantics
- **Introduction to OCL**
- Specifying requirements with OCL
- Modelling of Systems with Formal Semantics
- Propositional & First-order logic, sequent calculus
- OCL to Logic, horizontal proof obligations, using KeY
- Dynamic logic, proving program correctness
- JAVA CARD DL
- Vertical proof obligations, using KeY
- Wrap-up, trends

Object Constraint Language (OCL)

- Part of the UML standard
- Formal Specification Language
 - Standardized* formal semantics from OCL 2.0 onwards
- In this course: OCL 1.5
 - Semantics by mapping to typed FOL
 - Not all features realized, some extra features
- OCL syntax less mathematical, more programming language-oriented than Z, RSL, FOL, etc.
- **Why OCL?** UML is not expressive enough!

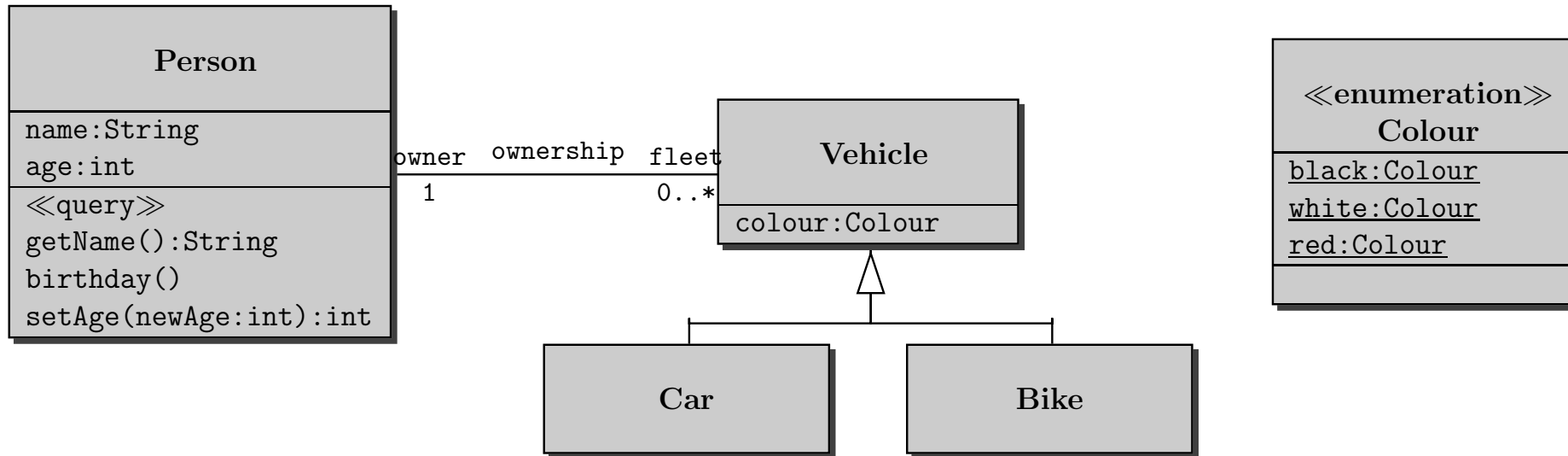
UML is not enough ...



- How old must a car owner be?
- How to express that a person can own at most one black car?
- How to specify that value of age is i after calling `setAge(i)`?

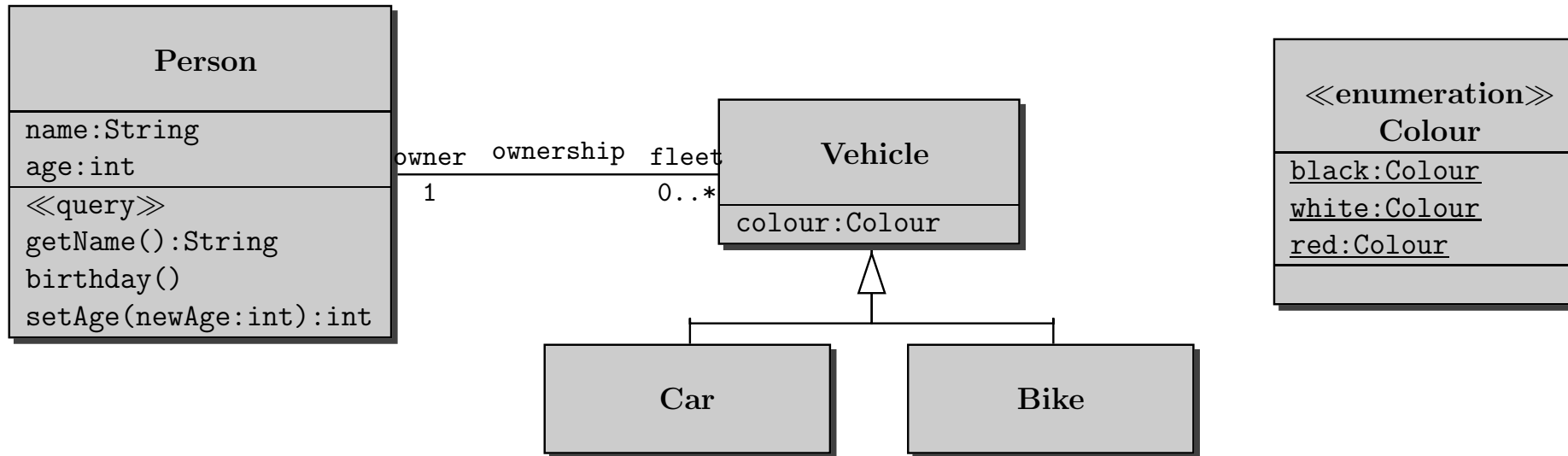
UML unsuitable to express semantics of design

Some OCL examples I



“A vehicle owner must be at least 18 years old”:

Some OCL examples I

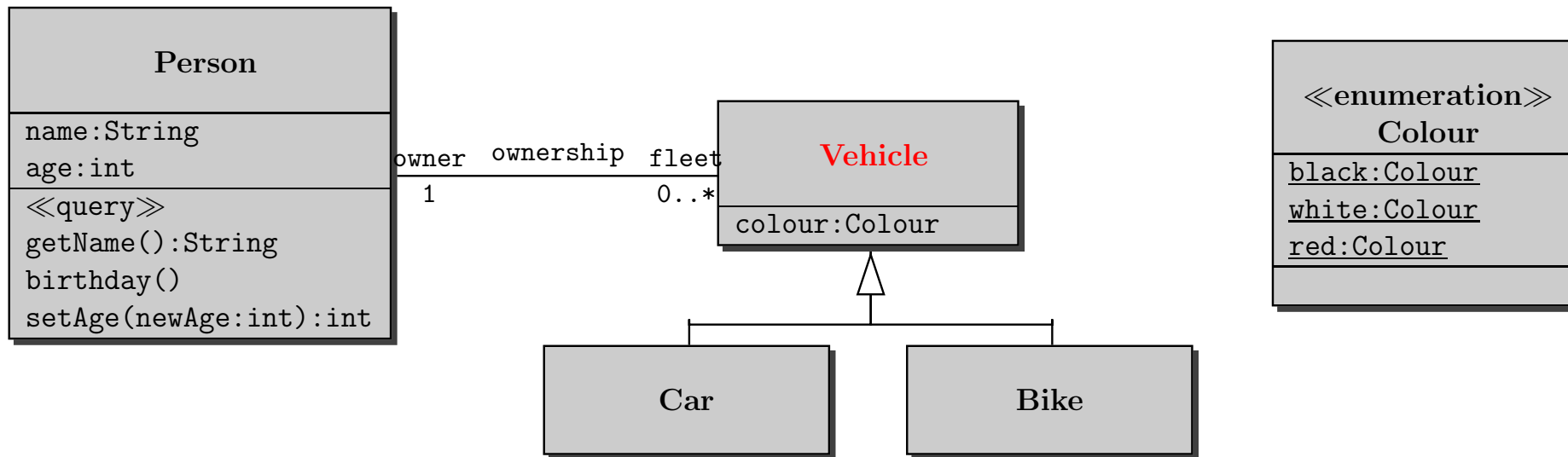


“A vehicle owner must be at least 18 years old”:

context Vehicle

inv : self.owner.age \geq 18

Some OCL examples I

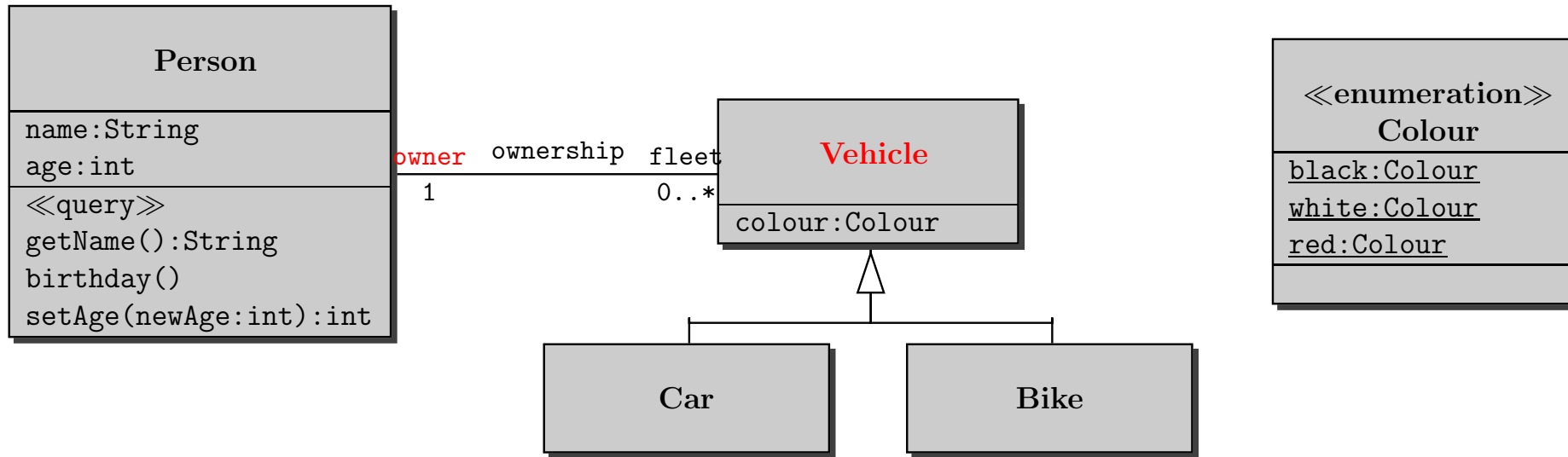


“A vehicle owner must be at least 18 years old”:

context **Vehicle** - - context declaration for all instances of this class

inv : **self**. owner. age \geq 18 - - 'self' is like JAVA's 'this'

Some OCL examples I

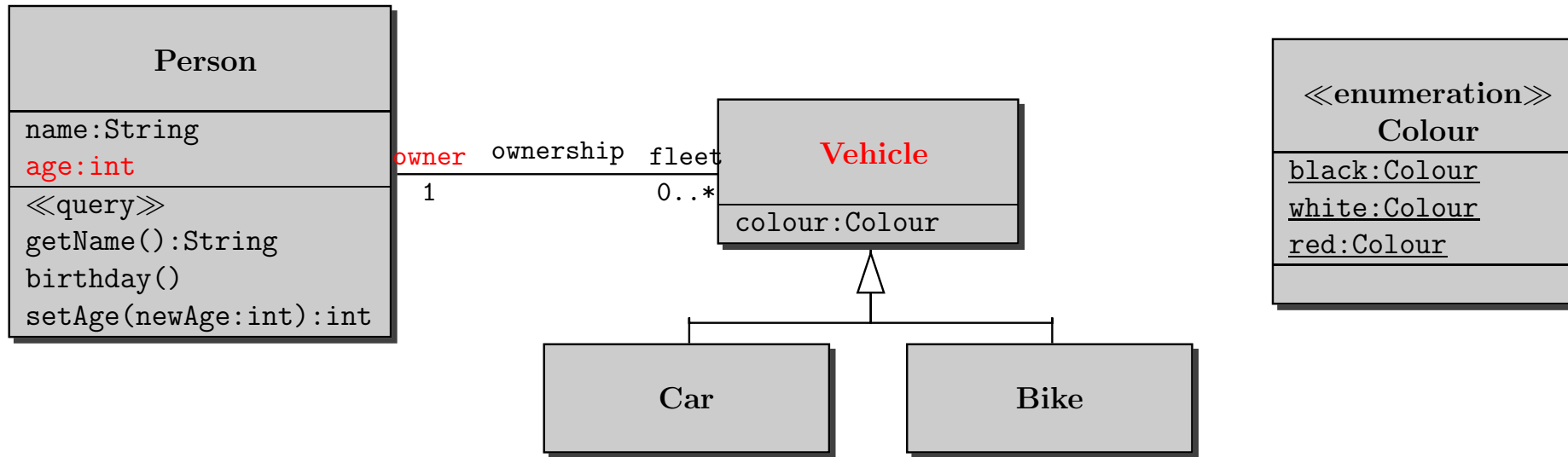


“A vehicle owner must be at least 18 years old”:

context Vehicle

inv : self. **owner**. age \geq 18 - - navigate to instance of supplier

Some OCL examples I

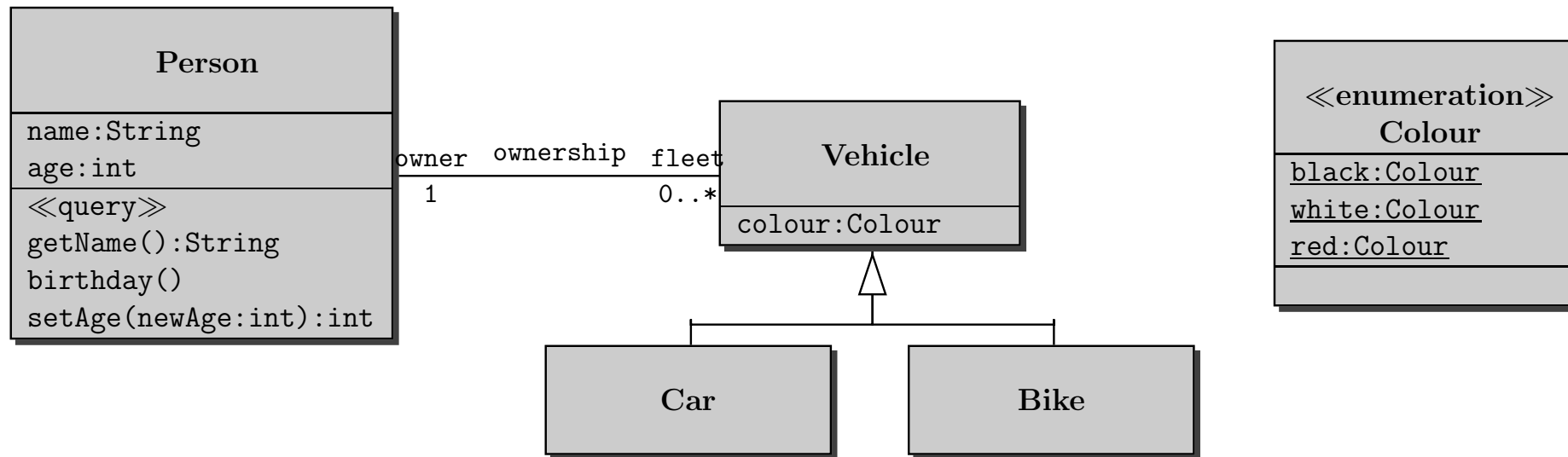


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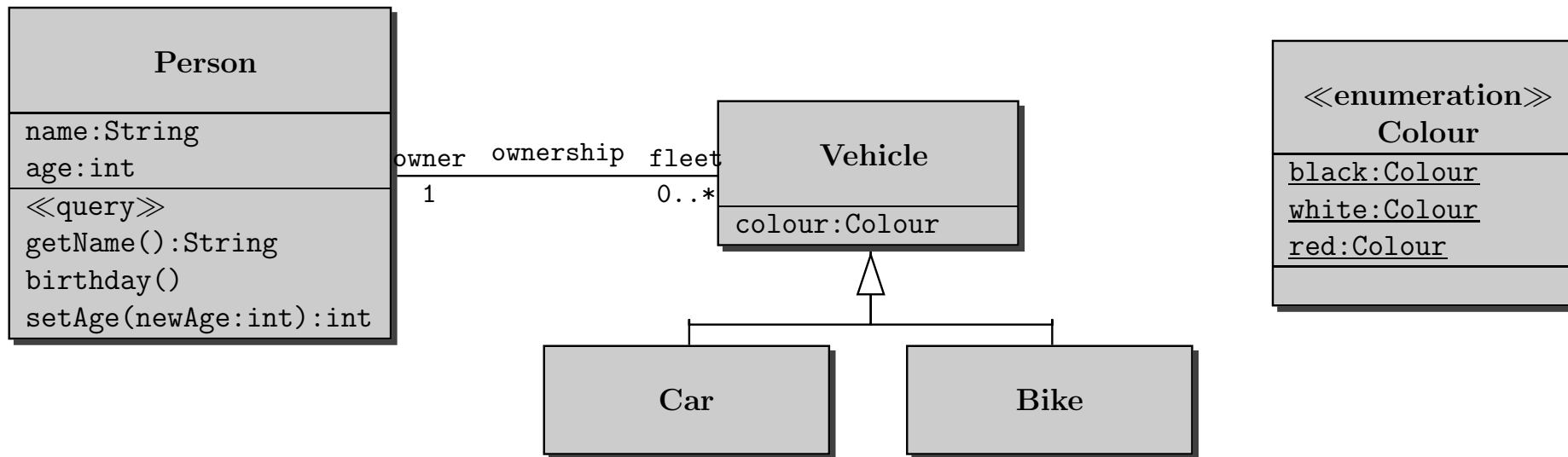


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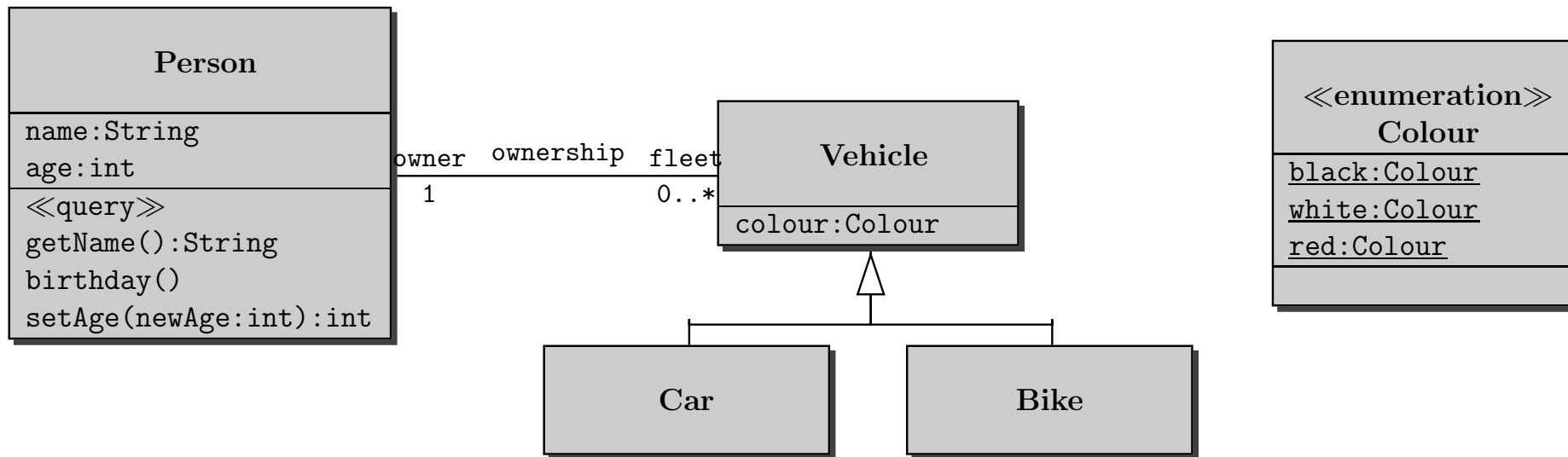
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What does that mean, instead? Relation between the constraints?

context Person

inv : self.age \geq 18

Some OCL examples I



“A vehicle owner must be at least 18 years old”:

context Vehicle

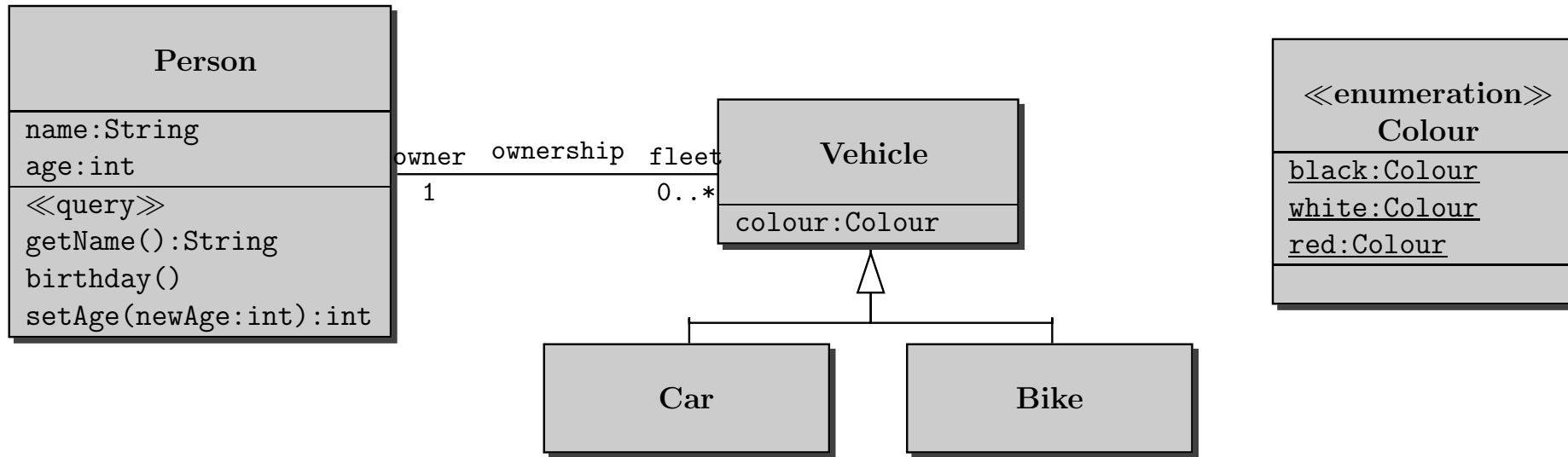
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“A car owner must be at least 18 years old”:

context Car

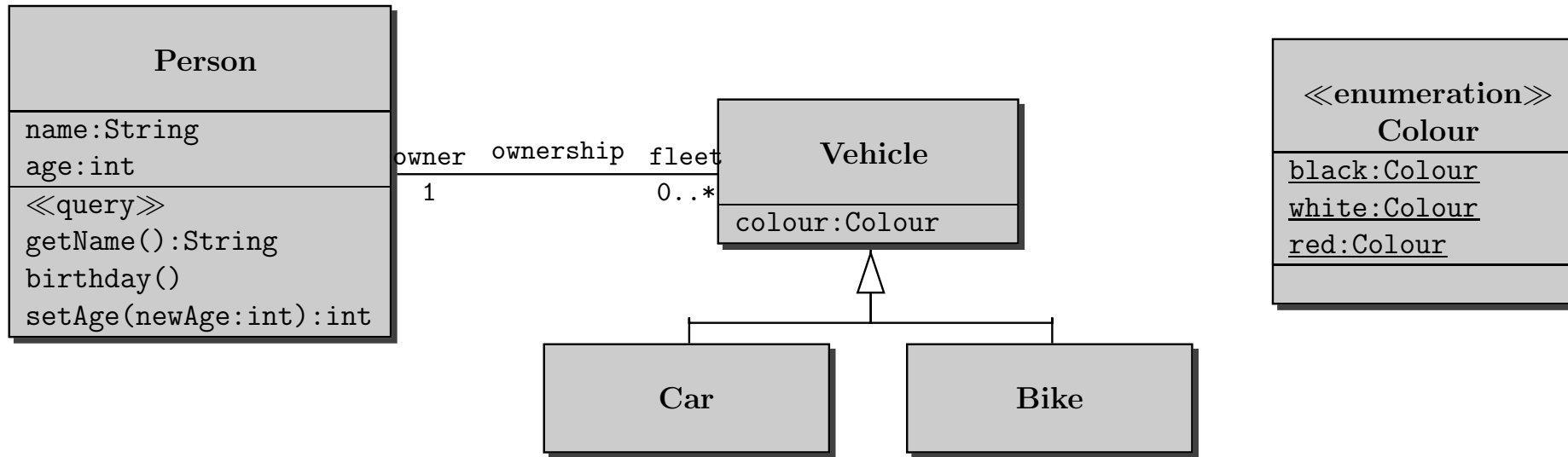
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Some OCL examples II



“No person owns more than 3 vehicles”:

Some OCL examples II



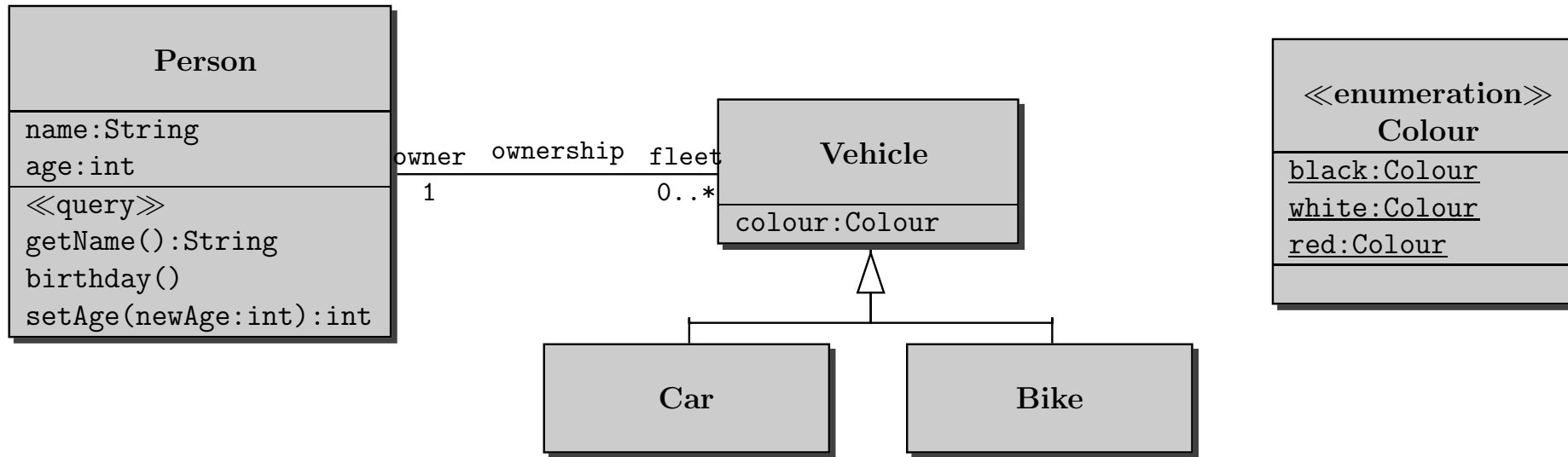
“No person owns more than 3 vehicles”:

context Person

inv : self.fleet-> size() <= 3

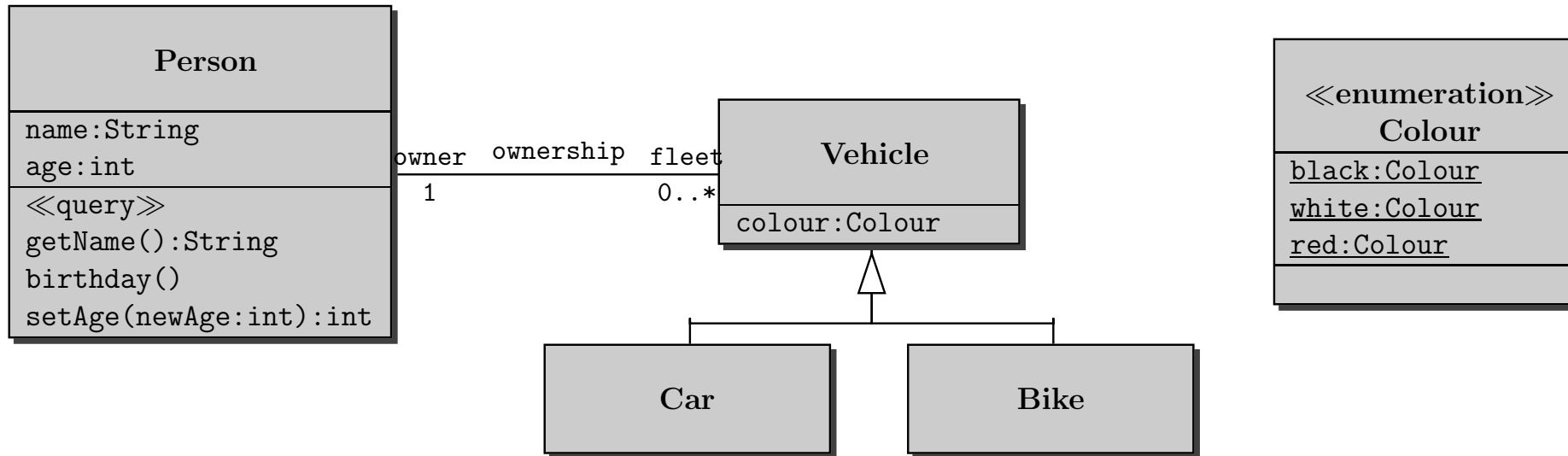
or change multiplicity

Some OCL examples II



“All vehicles of a person are black”:

Some OCL examples II

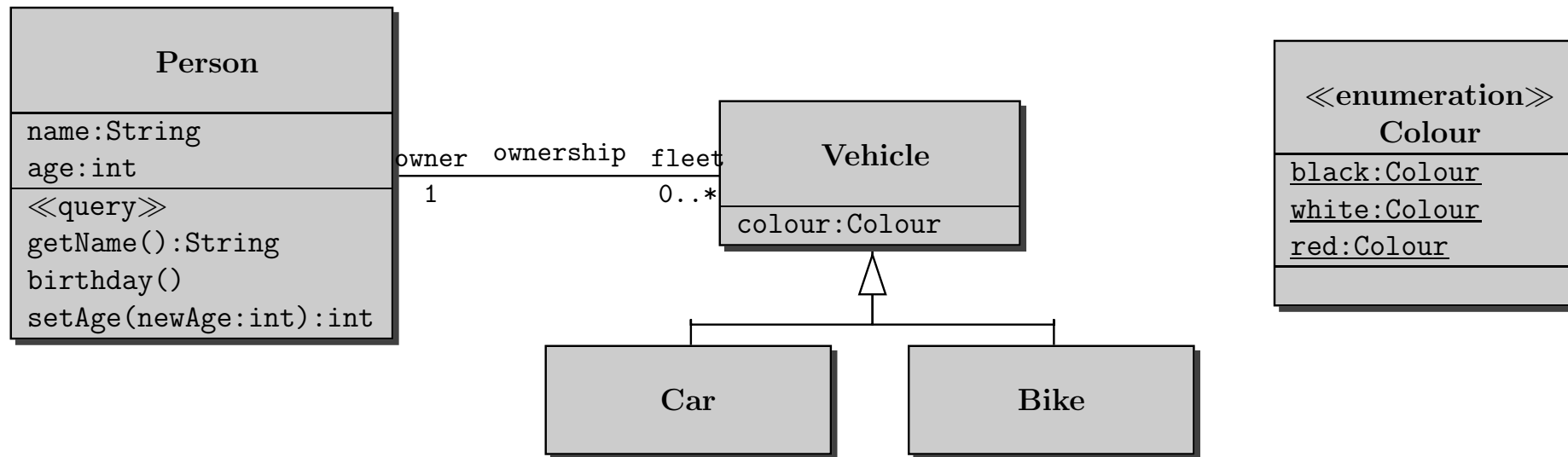


“All vehicles of a person are black”:

context Person

inv : self.fleet->forAll(v | v.colour = Colour.black)

Some OCL examples II



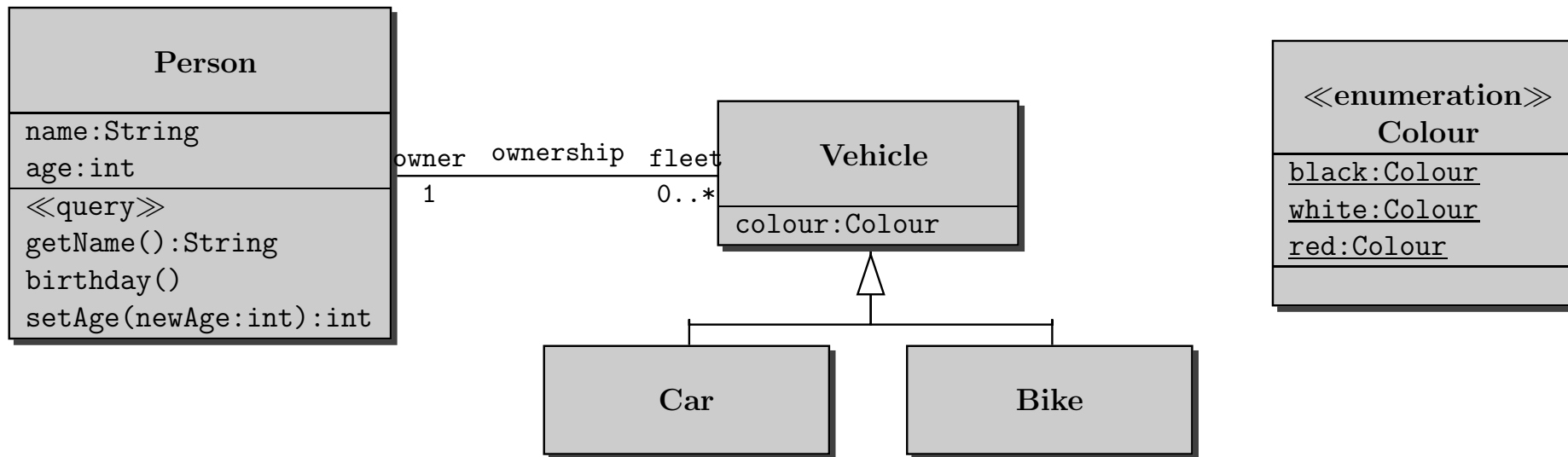
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Some OCL examples II



“All vehicles of a person are black”:

context Person

inv : self.fleet->forAll(v | v.colour = Colour.black)

“No person owns more than 3 black vehicles”:

context Person

inv : self.fleet->select(v | v.colour = Colour.black)->size() <= 3

The Classifier Context

context [instanceName :] classPath – – class from UML model

inv [invariantName] : oclExpression

context **aCar:Car**

inv **minimumAge:** aCar.owner.age \geq 18

- Class **classPath** is **context** of **invariant** constraint
- Invariant must hold for all instances of **classPath** at all times
Instances can be named **invariantName** (not in Together)
- May declare **invariantName** for the constraint (not in Together)
- Type of **oclExpression** must be Boolean

The Classifier Context

context [instanceName :] classPath – – **class from UML model**

inv [invariantName] : oclExpression

context [instanceName :] classPath

inv [invariantName₁] : oclExpression₁

...

...

inv [invariantName_{*n*}] : oclExpression_{*n*}

More than one invariant can be declared in same context

When Do Invariants Hold?

Consider `insert()` operation for `List` type with attribute `length : int`

- **Assume the invariant of `List` states that the number of nodes in a list is equal to the value of `length`**
- **During execution of `insert()` usually the invariant is violated**

Therefore, semantics of invariants in KeY and OCL:

Invariants hold at all times before and after execution of operations

How to relax this rigid requirement is topic of active research

The Operator Context: **Contract**

Specifying the semantics of operations: their **contract**

context [instanceName :]

classPath ::opName(p_1 : type₁; ... ; p_k : type_k)[:resultType]

{pre [preName] : oclExpression }

{post [postName] : oclExpression }

The Operator Context: **Contract**

Specifying the semantics of operations: their **contract**

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Example

“Calling **getName()** returns the current value of the attribute **name**”

context Person::getName():String

post : **result** = name

Special variable **result** contains return value, has type **resultType**

Together 6.2 Syntax for OCL Context Declarations

Classifiers

```
/**  
 * @invariants OCLExpression  
 */
```

Operators

```
/**  
 * @preconditions OCLExpression  
 * @postconditions OCLExpression  
 */
```

At most one may be present, connect multiple conditions with and.

Write constraints in .java file directly before feature they apply to.

Design by Contract

Pre-/postconditions like clauses in a **contract** about an operation

If the caller fulfills the precondition before the operation is called,
then the **called object** ensures the postcondition to hold
after execution of the operation

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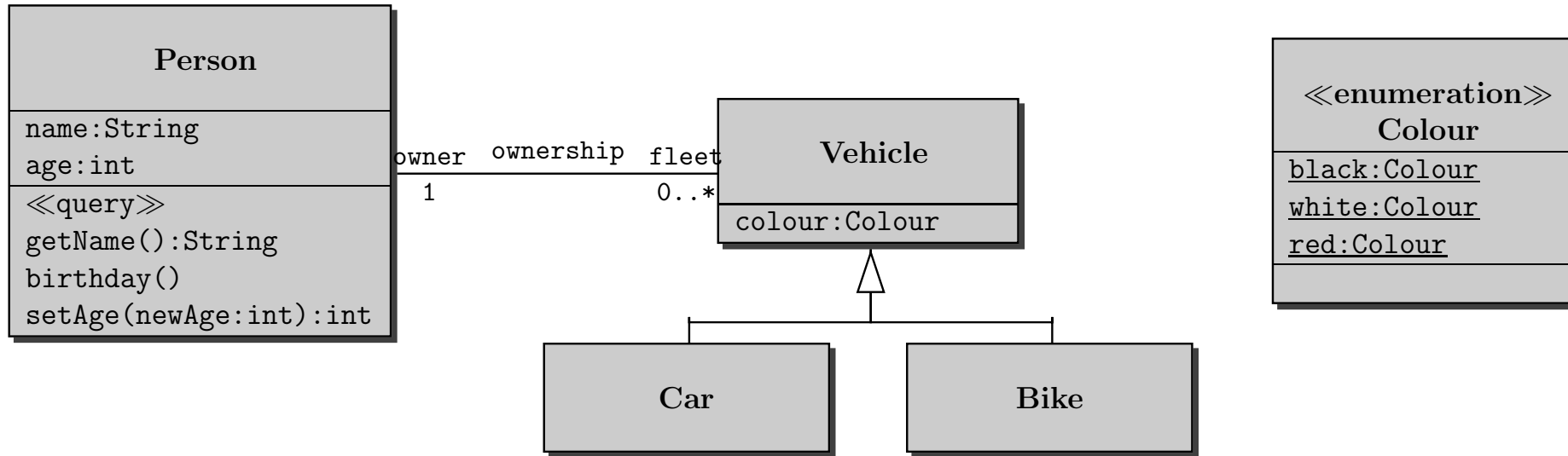
NOT

“Before executing an operation its precondition must hold”

or

“Whenever the precondition holds, the operation is called”

Constraints with Attributes



context **Person**

inv : **age** \geq 18

Equivalent notational variations

context **Person**

inv : **self.age** \geq 18

Equivalent notational variations

context **Person**

inv : **self.age** \geq 18

context **p:Person**

inv : **p.age** \geq 18

Equivalent notational variations

context **Person**

inv : **self.age** \geq 18

context **p:Person**

inv : **p.age** \geq 18

context **p:Person**

inv **minimumAge** : **p.age** \geq 18

Equivalent notational variations

context **Person**

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context **p:Person**

inv : **p.age** \geq 18

context **p:Person**

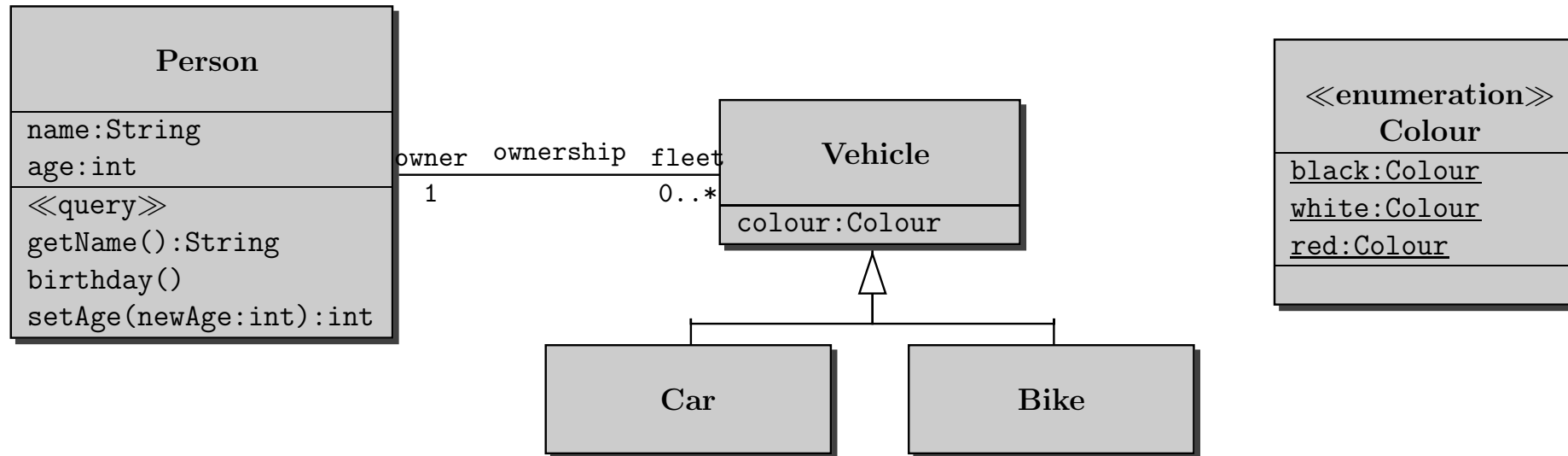
inv **minimumAge** : **p.age** \geq 18

context **Person**

inv **minimumAge** : **age** \geq 18

Beware: variants using named instances not possible in Together

Operator Constraint: Contract



context **Person::setAge(newAge: int):int**

pre : **self.age** ≥ 0 and **newAge** ≥ 0

post : **self.age** = **newAge**

Which implementation satisfies the contract?

context **Person::setAge(newAge: int):int**

pre : self.age \geq 0 and newAge \geq 0

post : self.age = newAge

```
int setAge(int newAge) {  
    if (age $\geq$ 0 && newAge $\geq$ 0) { this.age = newAge; }  
    return this.age;  
}
```

```
int setAge(int newAge) {  
    return this.age = newAge;  
}
```

```
int setAge(int newAge) {  
    this.age = newAge;  
    return -1;  
}
```

OCL Types

UML class types

User-defined classes from **context diagram** of an OCL constraint

Each **class** of UML context diagram is legal **type** in OCL constraint

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Primitive types

Integer, Real, Boolean and String (Together: int, real, boolean)

int, real not in JAVA CARD, but int, short, byte work in KeY

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Enumeration types

User-defined enumeration types (not supported in Together and KeY)

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User-defined enumeration types (not supported in Together and KeY)

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Special types

e.g. *OclAny, OclType*

Type Conformance in OCL

- *Integer* < *Real* (subtype relation)

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- $Integer < Real$ (subtype relation)
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 $T_1 < T_2$ holds exactly if T_1 is a **subclass** of T_2 in context diagram

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 $T_1 < T_2$ holds exactly if T_1 is a **subclass** of T_2 in context diagram
- For all type expressions T , not denoting a collection type:
 - *Set*(T) < *Collection*(T)
 - *Bag*(T) < *Collection*(T)
 - *Sequence*(T) < *Collection*(T)

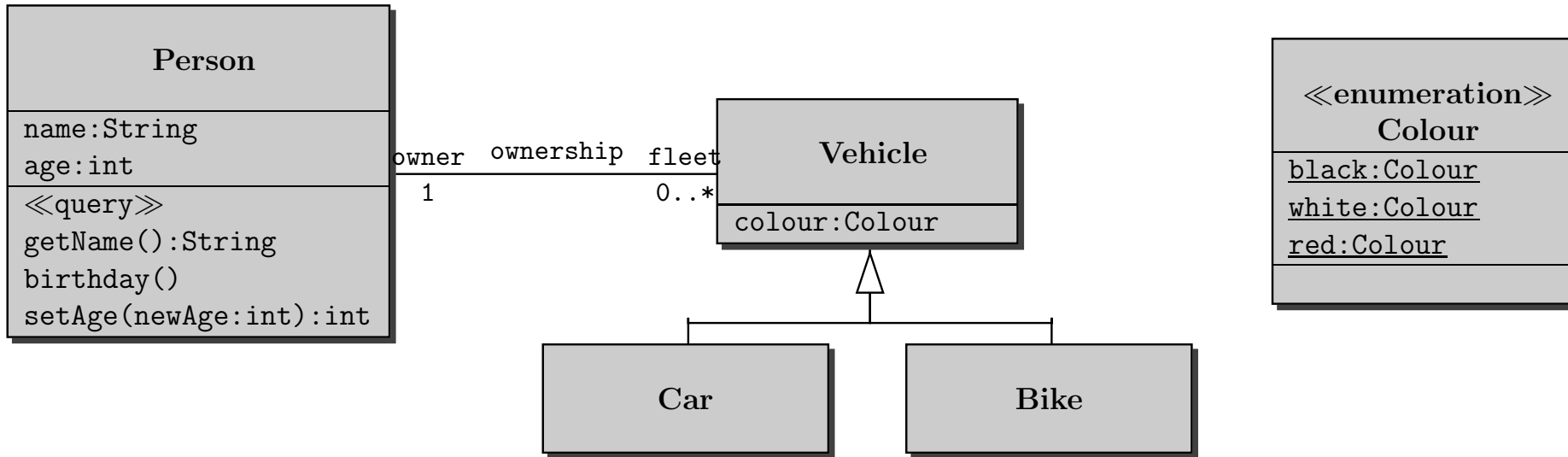
Type Conformance in OCL

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- For all type expressions T , not denoting a collection type:
 - $Set(T) < Collection(T)$
 - $Bag(T) < Collection(T)$
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- If T is not a collection type: $T < OCLAny$

Type Conformance in OCL

- *Integer* < *Real* (subtype relation)
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 - $Set(T) < Collection(T)$
 - $Bag(T) < Collection(T)$
 - $Sequence(T) < Collection(T)$
- If T is not a collection type: $T < OCLAny$
- If $T_1 < T_2$ and C is any of the type constructors *Collection*, *Set*, *Bag*, *Sequence*:
 $C(T_1) < C(T_2)$.

Typing Examples



- context **Person**
- - `self.name` has type *String*
 - - `self.age` has type *Integer*
 - - `self.fleet` has type *Set(Vehicle)*
- context **Vehicle**
- - `self.colour` has type *Colour*
- context ...
- - `Colour.black` has type *Colour*

Navigation: Accessing Properties

OCL **Properties** (functions that may occur in OCL expr)

- **Attributes from underlying UML model**
- **Association ends from underlying UML model**
- **Operations with stereotype `<<query>>` from UML model**
- **Predefined OCL properties**

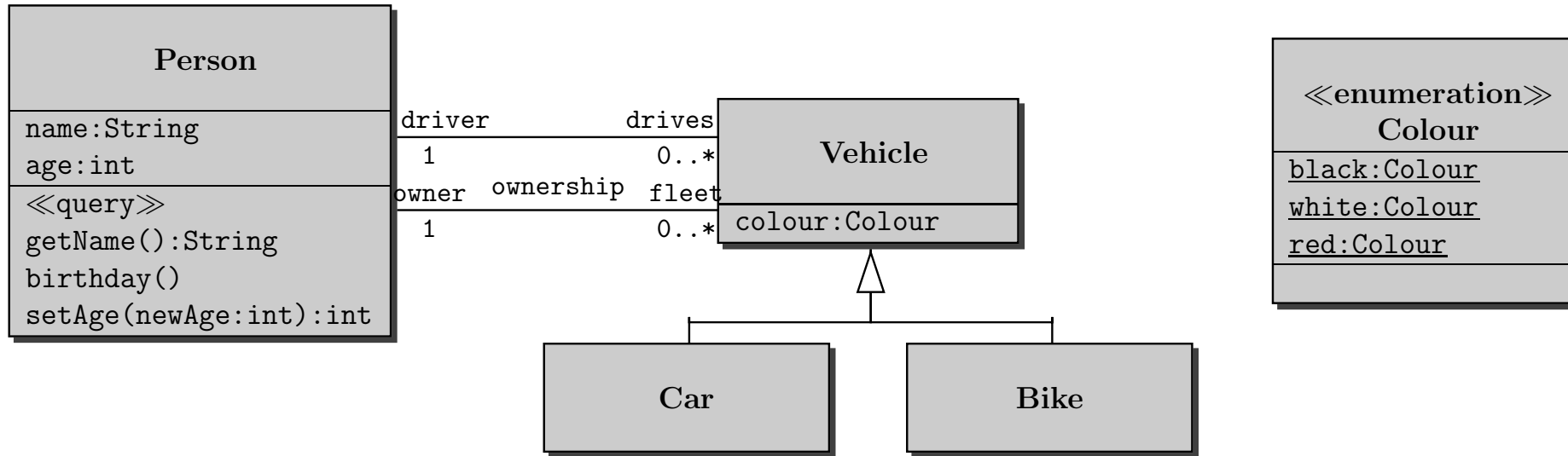
If argument has **no collection type**: dot notation (like JAVA)

If argument has **collection type**: arrow notation “`->`”

Collection type has large number of predefined properties:

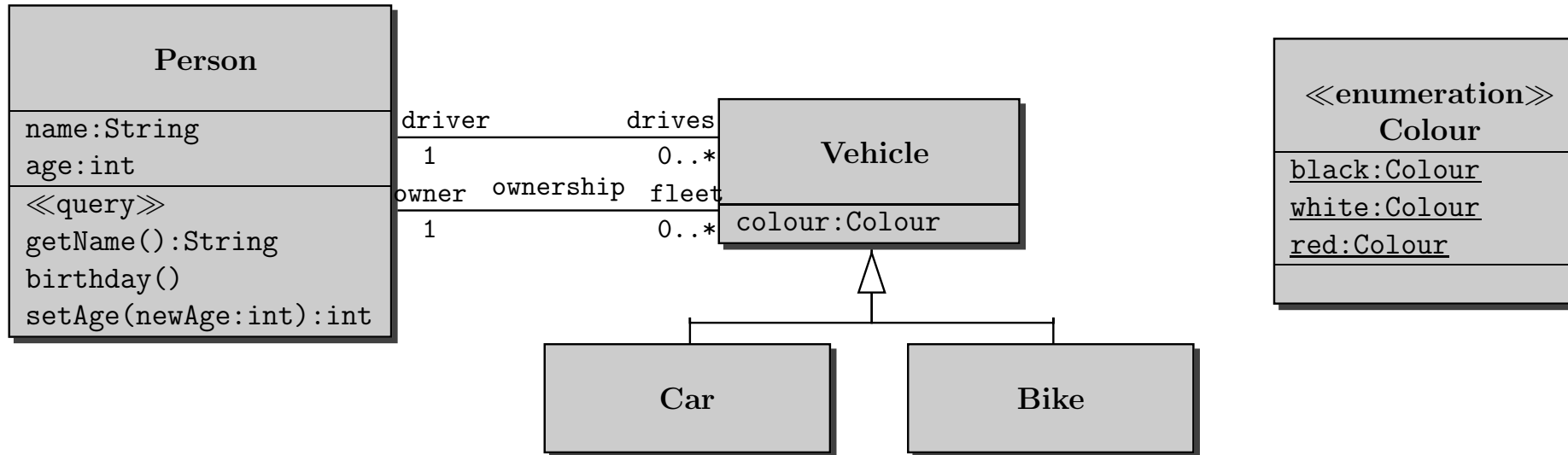
includes, intersection, forAll, **etc.**

User-Defined Operations within Constraints



Only `<<query>>` operations allowed to occur within OCL expressions

User-Defined Operations within Constraints



Only `<<query>>` operations allowed to occur within OCL expressions

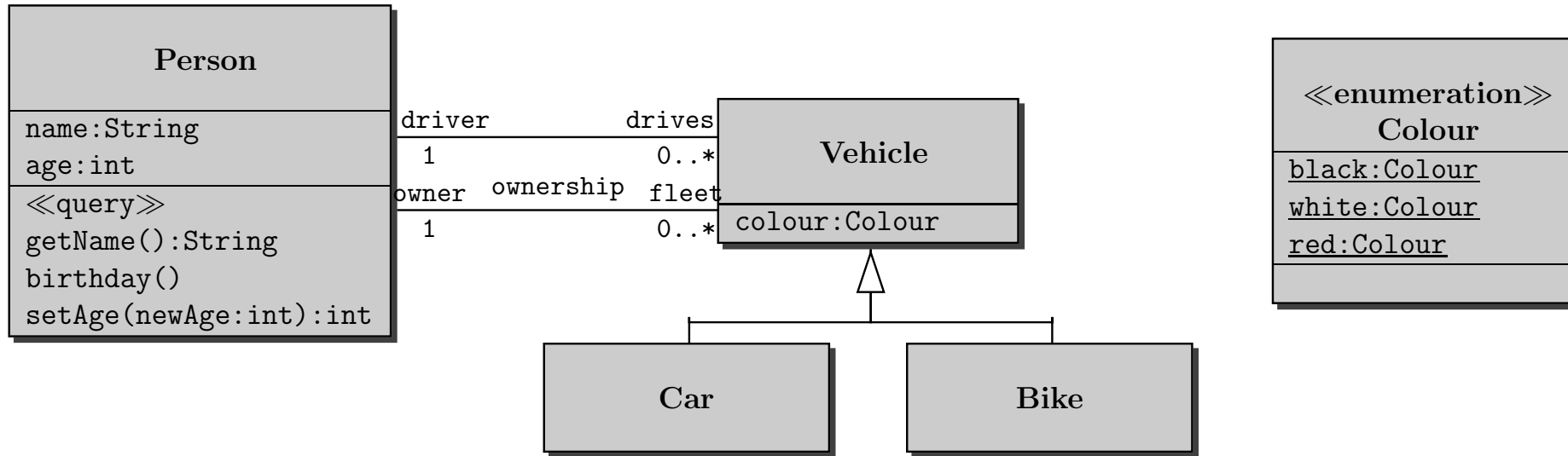
context **Person**

inv **self.name = self.getName()**

Beware: parameterless properties with brackets, eg:

Set{1, 2, 3} \rightarrow sum()

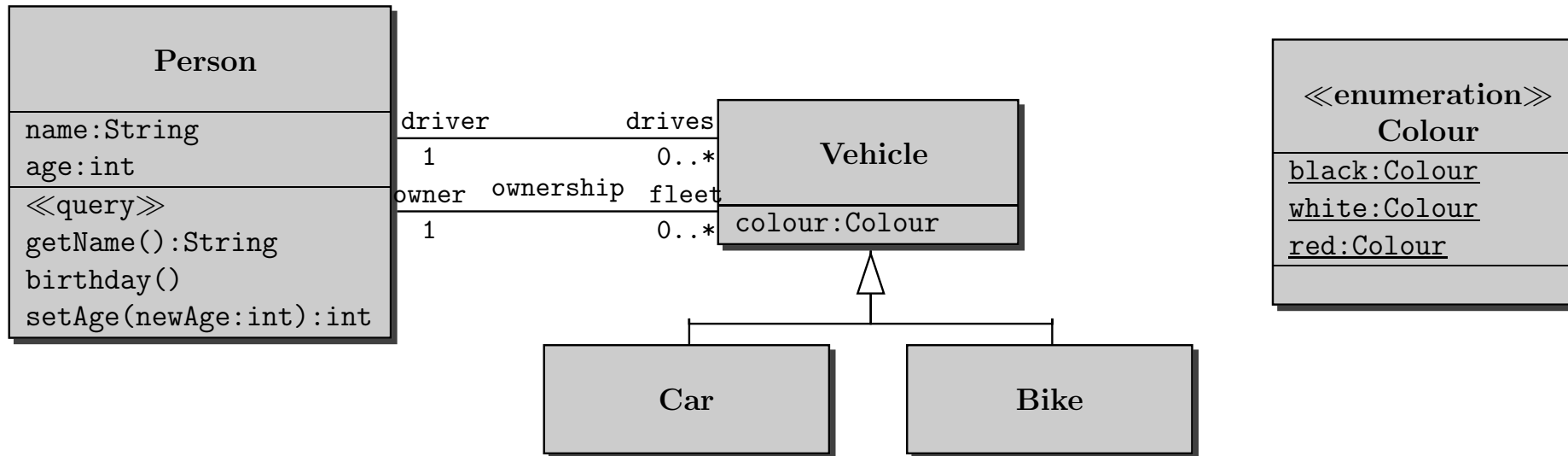
Constraints that use Associations



context **Vehicle**

inv **owner <> driver** - - 'self' implicit!

Constraints that use Associations



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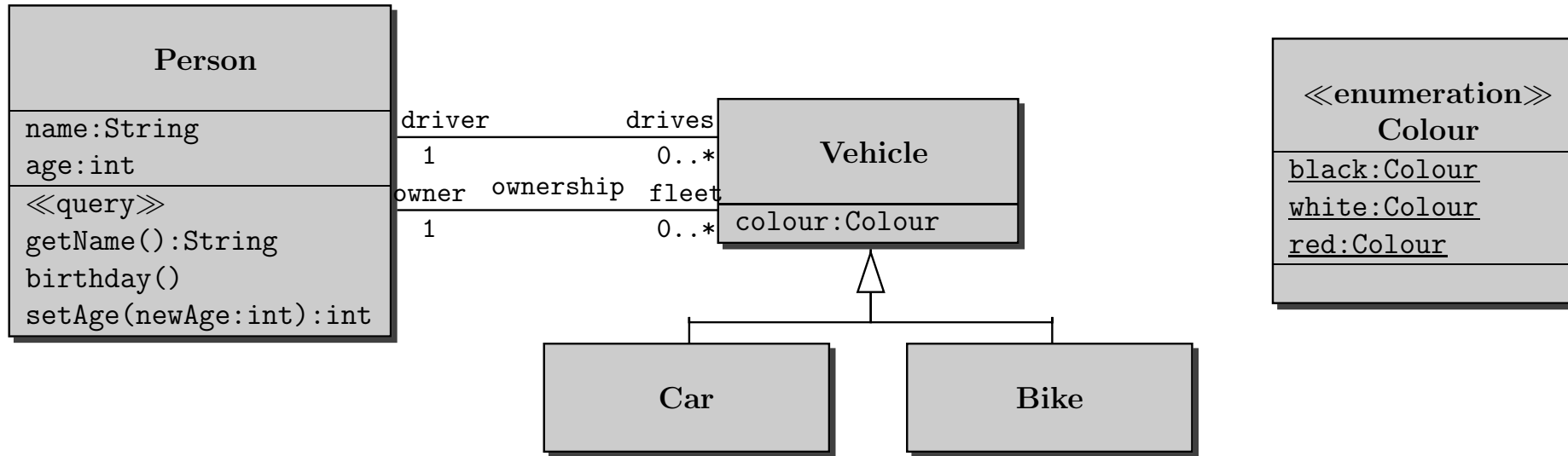
inv owner <> driver - - 'self' implicit!

context Person

inv fleet -> intersection(drives) -> isEmpty()

inv self.fleet -> intersection(self.drives) -> isEmpty()

Notational Variants of Collection Properties



context **Person** - - all constraints are equivalent

inv **fleet** \rightarrow collect(v:Vehicle | v.colour) \rightarrow size() = 1

inv **fleet** \rightarrow collect(v | v.colour) \rightarrow size() = 1

inv **fleet** \rightarrow collect(colour) \rightarrow size() = 1

inv **fleet.colour** \rightarrow size() = 1 - - shorthand for 'collect' in Together

The type OclType

What is the type of UML model types (eg, Person)?

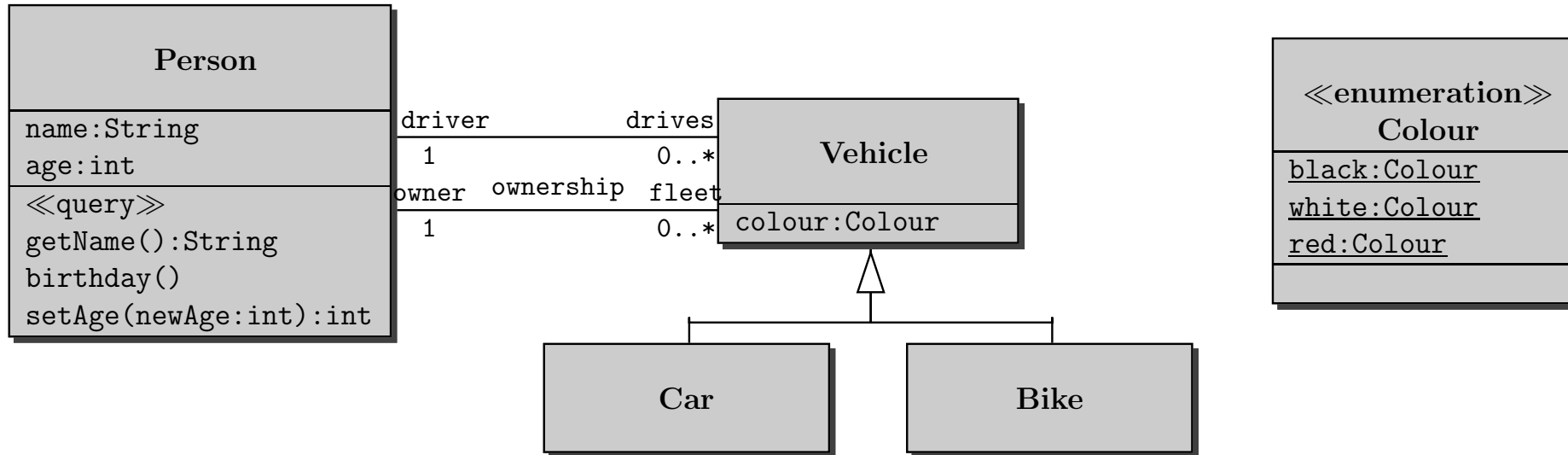
OclType

OclType is **metatype** with predefined properties:

- **aType.name()** gives name string of aType
- Similar are **attributes()**, **operations()**, **associationEnds()**
- **aType.allInstances()** gives all instances of aType in current snapshot

allInstances needed to express properties relating to all currently existing objects

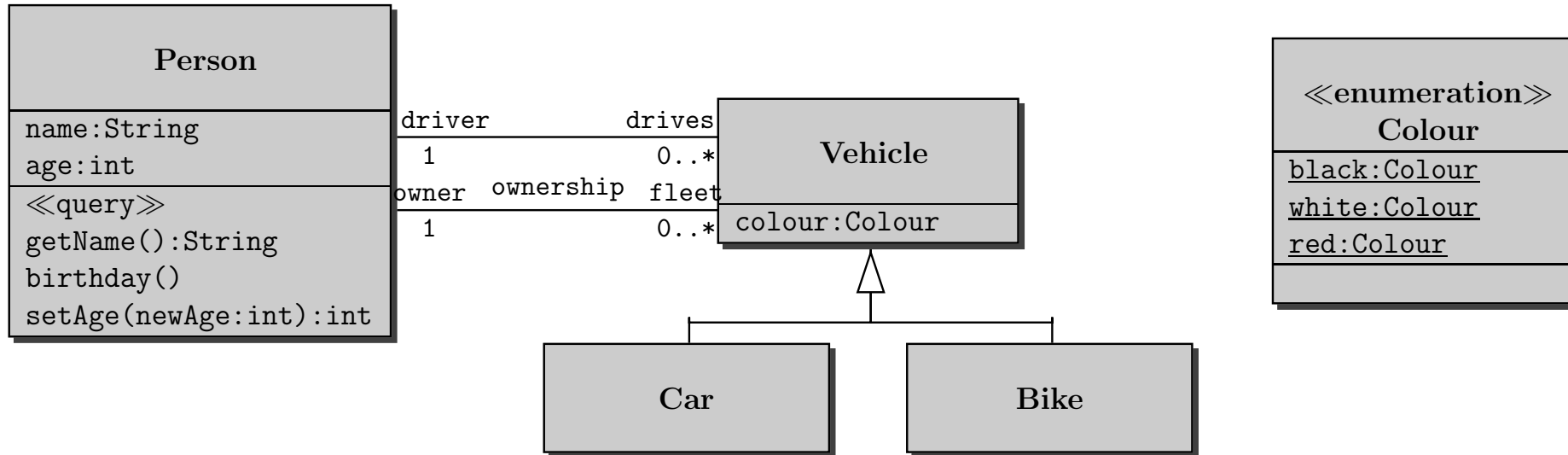
Using allInstances



context **Person**

inv **Person.allInstances** \rightarrow **forall(p | p.age \geq 0)**

Using allInstances



context **Person**

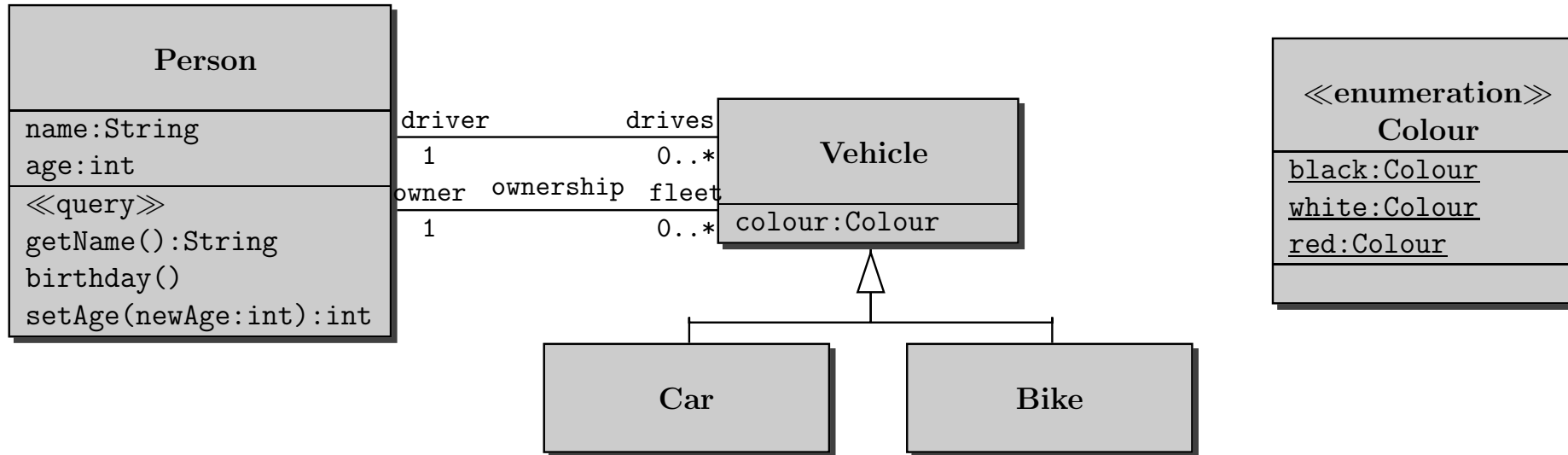
inv **Person.allInstances** \rightarrow `forall(p | p.age \geq 0)`

Constraint is independent of model context — equivalent:

context **Vehicle**

inv **Person.allInstances** \rightarrow `forall(p | p.age \geq 0)`

Using allInstances



context **Person**

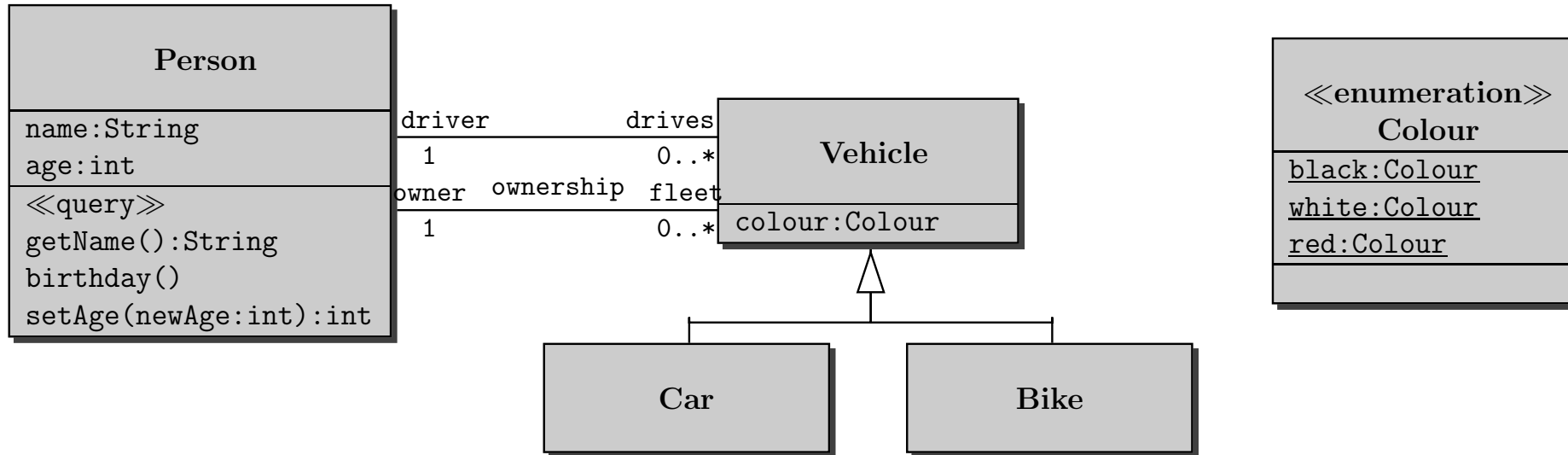
inv **Person.allInstances \rightarrow forAll(p | p.age \geq 0)**

Context declaration of invariant has implicit allInstances/forAll:

context **Person** - - **equivalent to constraint above**

inv **self.age \geq 0**

Avoiding allInstances



context **Person**

inv **Person.allInstances** →

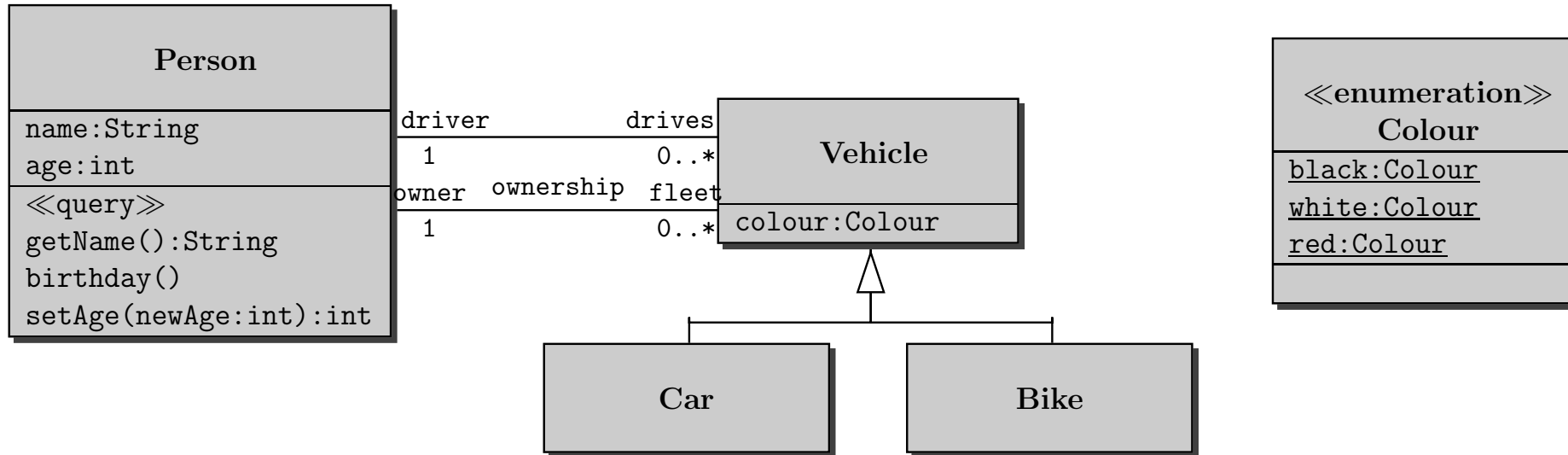
forAll(p1, p2 | p1.name = p2.name implies p1 = p2)

allInstances

... tends to make constraint difficult to read

... can give rise to unnecessarily difficult verification task

Avoiding allInstances



context **Person**

inv **Person.allInstances** →

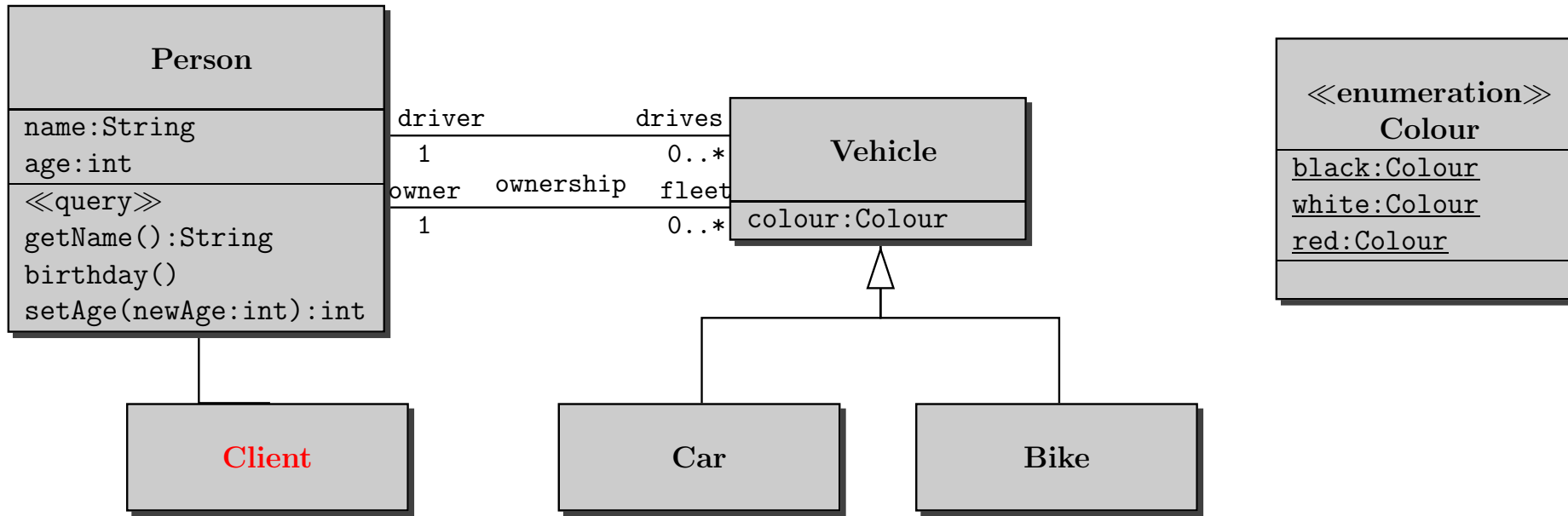
forAll(p1, p2 | p1.name = p2.name implies p1 = p2)

Can be equivalently replaced with: **(not in Together!)**

context **p1,p2:Person**

inv **p1.name = p2.name implies p1 = p2**

Avoiding allInstances



context **Person**

inv **Person.allInstances** →

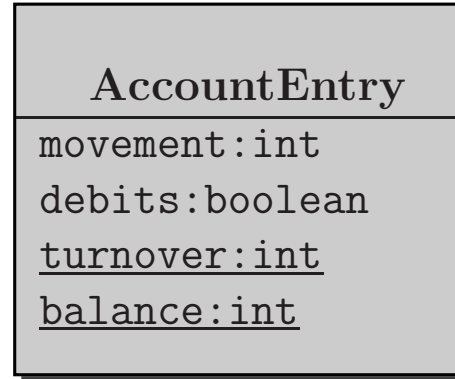
forAll(p1, p2 | p1.name = p2.name implies p1 = p2)

Often, collection of objects available via suitable association:

context **Client**

inv : person → forAll(p1, p2 | p1.name = p2.name implies p1 = p2)

The iterate Property

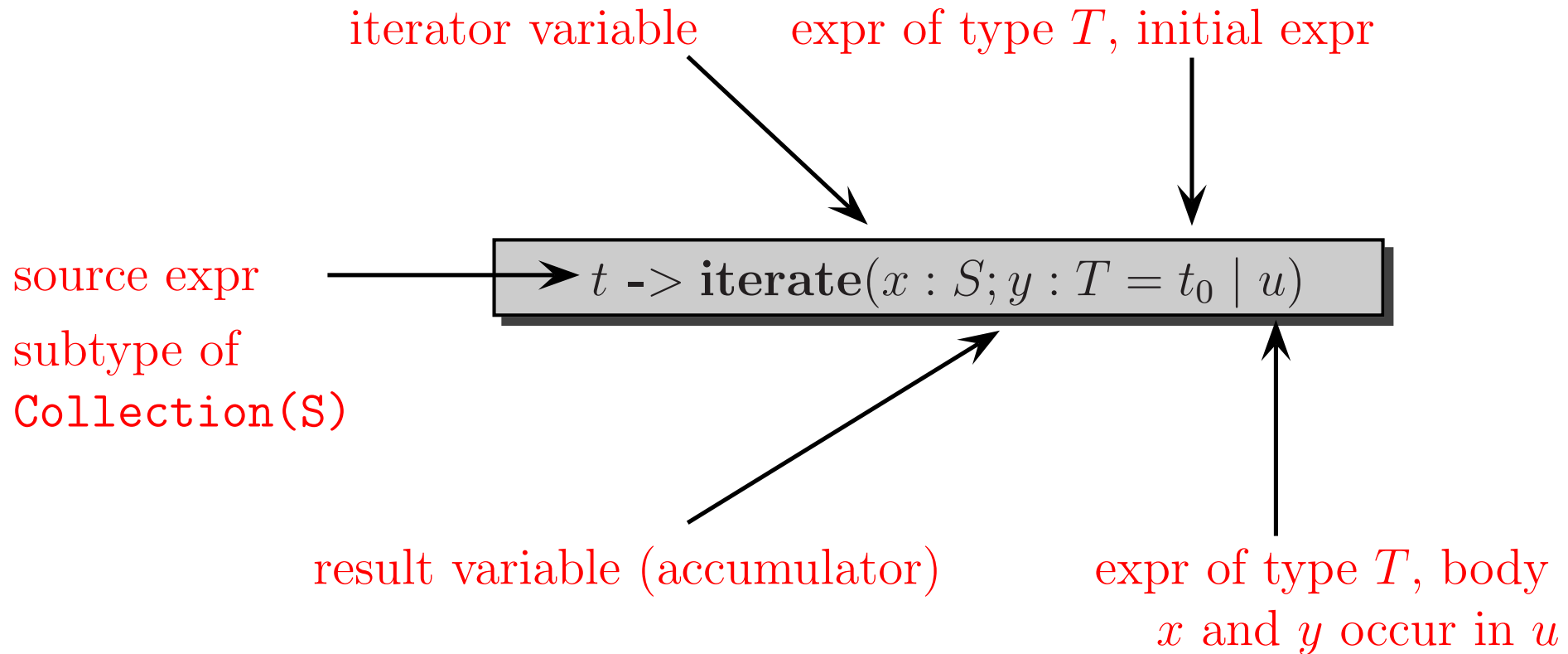


context **AccountEntry**

inv **AccountEntry.allInstances** →

**iterate(a:AccountEntry ; m:Integer=0 | m+a.movement) =
AccountEntry.turnover**

Syntax of the *iterate* Property



Java Pseudocode of *iterate*

$t \rightarrow \text{iterate}(x:S; y:T=t_0 \mid u)$

```
S x;
```

```
T y = t0;
```

```
for (Enumeration e = t.elements(); e.hasMoreElements() ) {  
    x = e.nextElement();  
    y = u(x,y);  
}
```

Type of x and y can be inferred from t and u

OCL's *iterate* is also similar to the *accumulate* function of the C++ STL

Quantifiers

$t \rightarrow \text{iterate}(x:S; y:\text{Boolean}=\text{true} \mid y \text{ and } a(x))$

... where $a(x)$ is an expression of type Boolean (with occurrence of x)

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Can be equivalently expressed by

$t \rightarrow \text{forAll}(x \mid a(x))$

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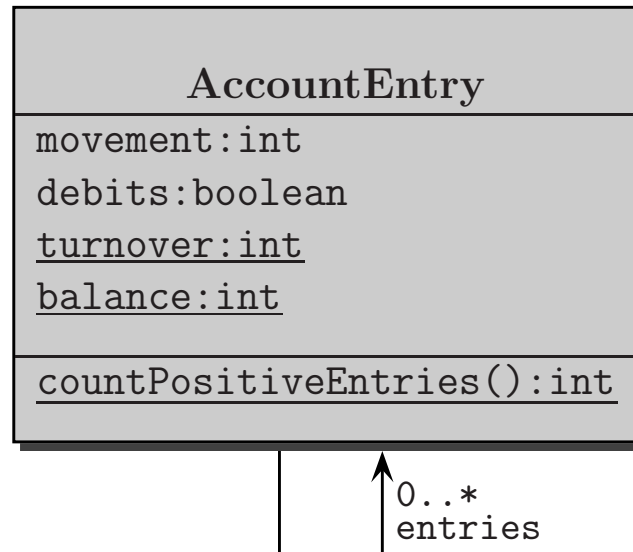
Can be equivalently expressed by

$t \rightarrow \text{forAll}(x \mid a(x))$

Similar:

$t \rightarrow \text{exists}(x \mid a)$

Selecting Elements

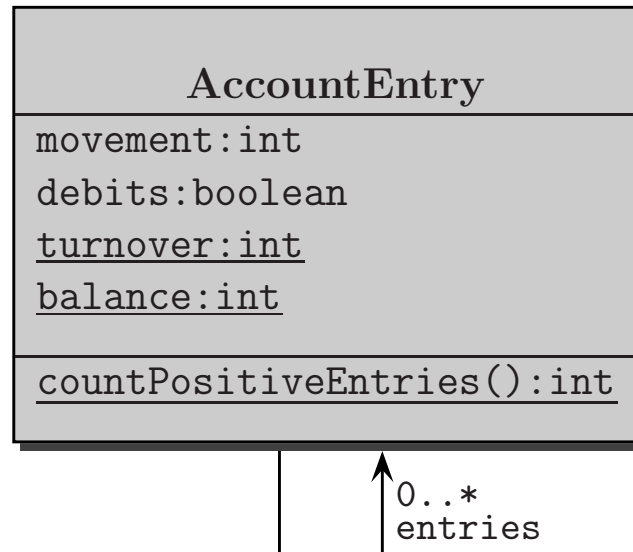


context `AccountEntry::countPositiveEntries():int`

pre : `true`

post : `result = AccountEntry.allInstances ->`
`select(e | not e.debits) -> size()`

Selecting Elements



context `AccountEntry::countPositiveEntries():int`

pre : `true`

post : `result = AccountEntry.allInstances -> select(e | not e.debits) -> size()`

Alternative notation using self-association:

post : `result = entries -> select(not debits) -> size()`

Reducing *select* to *iterate*

Like all other collection properties *select* definable with *iterate*

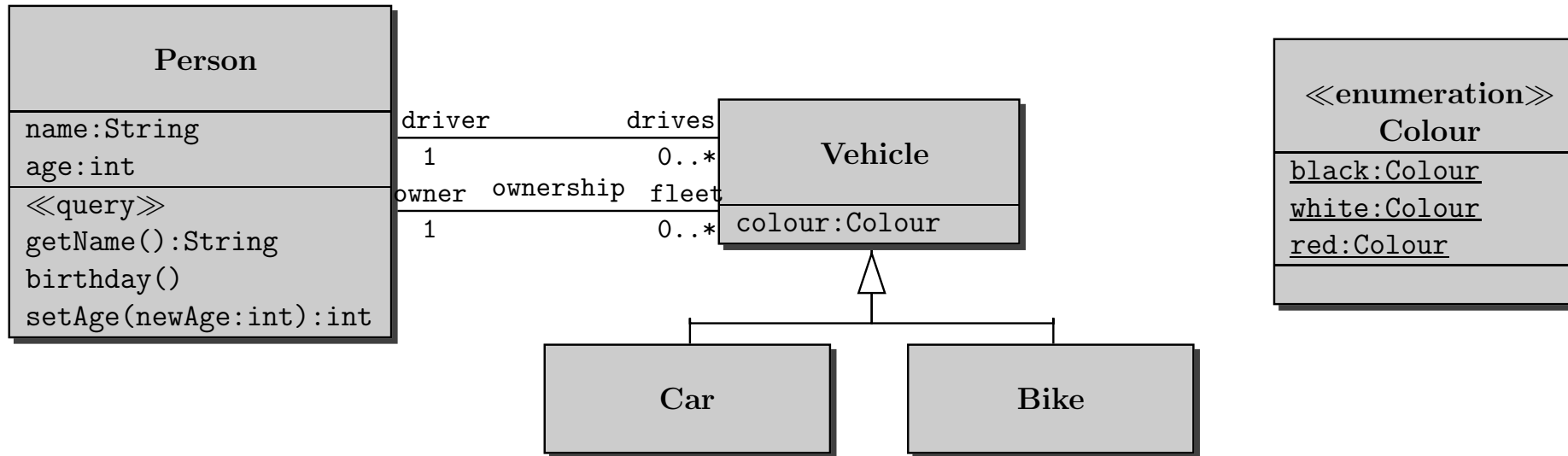
$s \rightarrow \text{select}(x:T \mid e) =$

$\text{iterate}(x:T; \text{acc: Set}(T) = \text{Set}\{\} \mid$

$\text{if } e \text{ then acc} \rightarrow \text{including}(x) \text{ else acc})$

- s is of type $\text{Set}(T)$
- e is an OCL expression of type Boolean
- including in turn is definable with *iterate*
- all built-in collection properties definable with *iterate* and includes

Referring to Previous Values



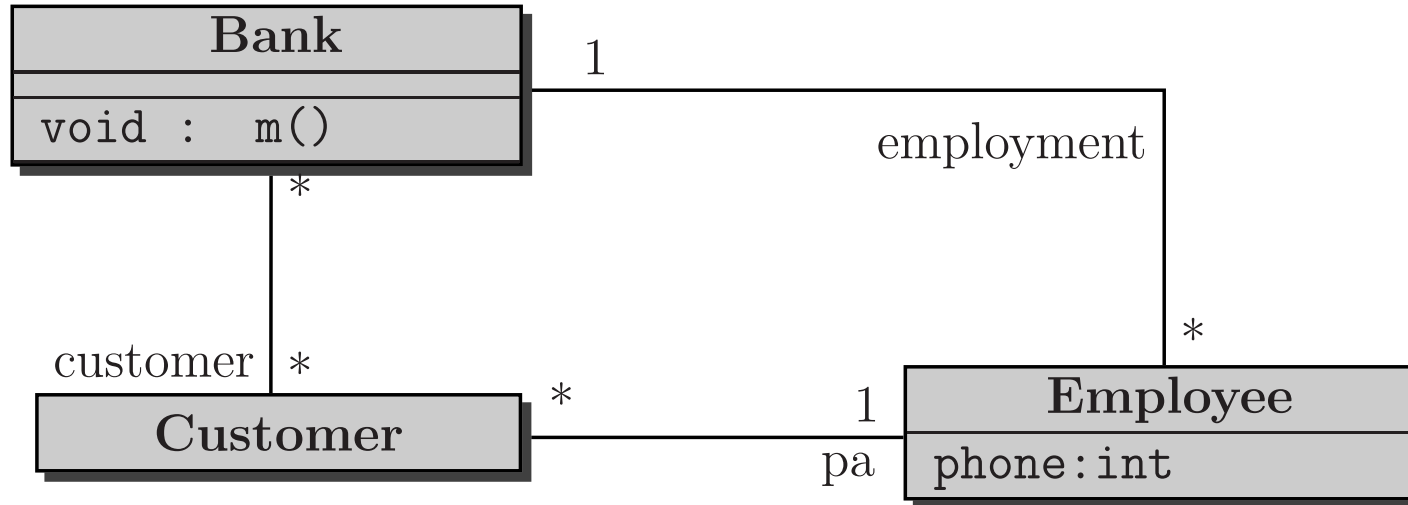
context **Person::birthday()**

pre **age \geq 0**

post **age = age@pre + 1**

User-defined properties qualified with **@pre** refer to value in prestate

Multiple Occurrences of @pre



aCustomer.pa.phone

**new phone number
of current p.a.**

aCustomer.pa@pre.phone

**new phone number
of previous p.a.**

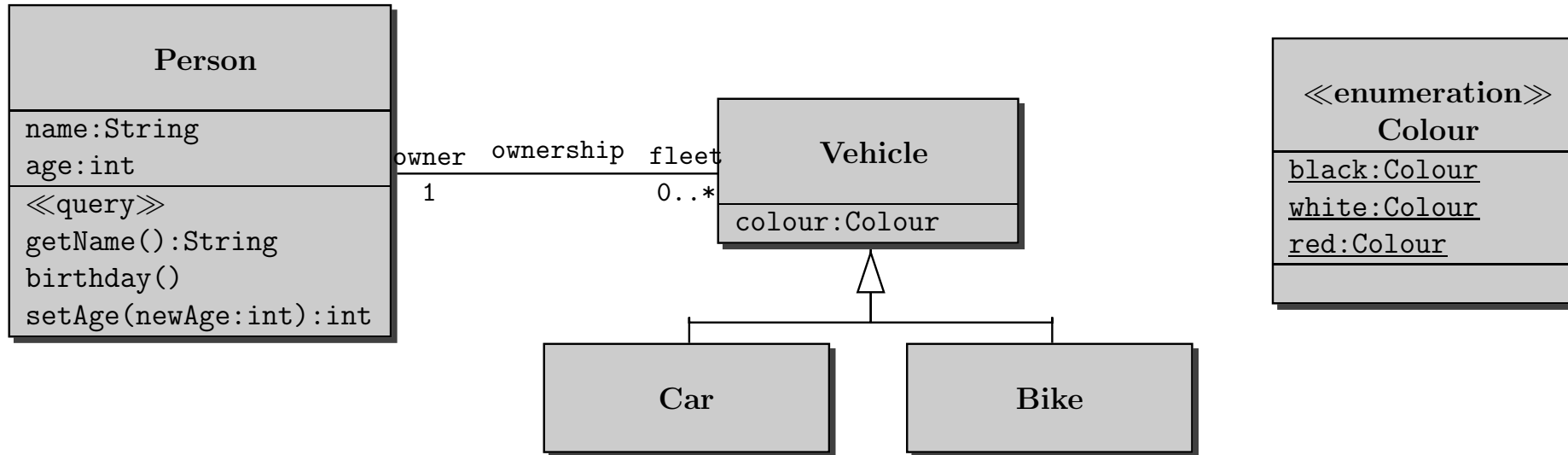
aCustomer.pa.phone@pre

**old phone number
of current p.a.**

aCustomer.pa@pre.phone@pre

**old phone number
of previous p.a.**

A Method Does More Than It Should



context **Person::setAge(newAge: int):int**

pre : **self.age** \geq 0 and **newAge** \geq 0

post : **self.age** = **newAge**

```
int setAge(int newAge) { // correct implementation?!  
    name = "Jabberwocky";  
    return this.age = newAge;  
}
```

The Frame Problem

How to express that nothing else is changed than what is specified?

Known in AI as the **Frame Problem**

The Frame Problem

How to express that nothing else is changed than what is specified?

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First Solution

context **Person::setAge(newAge: int):int**

pre : **self.age** ≥ 0 and **newAge** ≥ 0

post : **self.age = newAge** and **name = name@pre**

Done for all attributes visible for context class: very tedious!

The Frame Problem

How to express that nothing else is changed than what is specified?

Known in AI as the **Frame Problem**

Second Solution

context **Person::setAge(newAge: int):int**

pre : **self.age** ≥ 0 and **newAge** ≥ 0

post : **self.age** = **newAge**

modifies: **self.age**

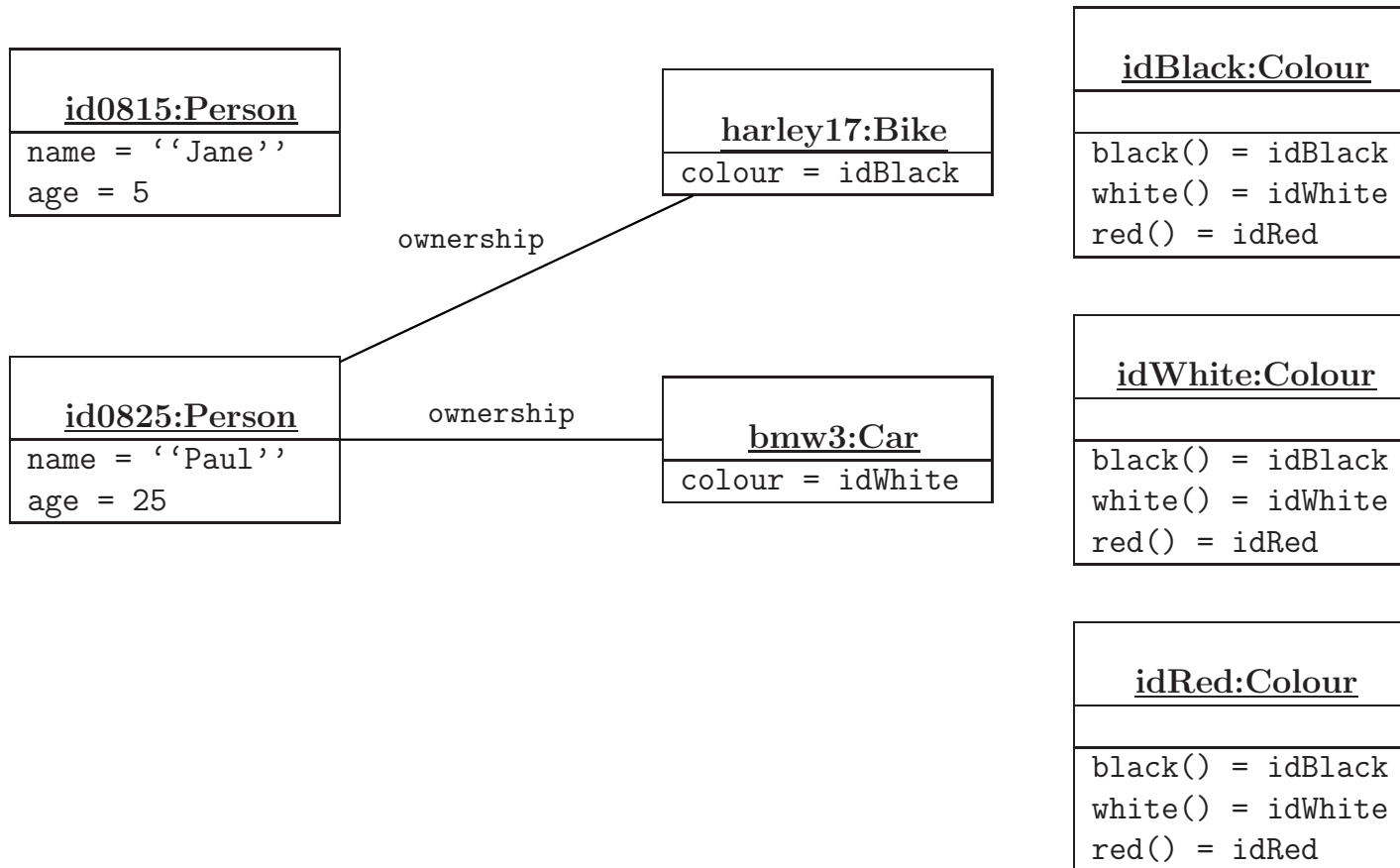
The OCL to FOL compiler creates an efficient representation

KeY extension to OCL, not in the standard

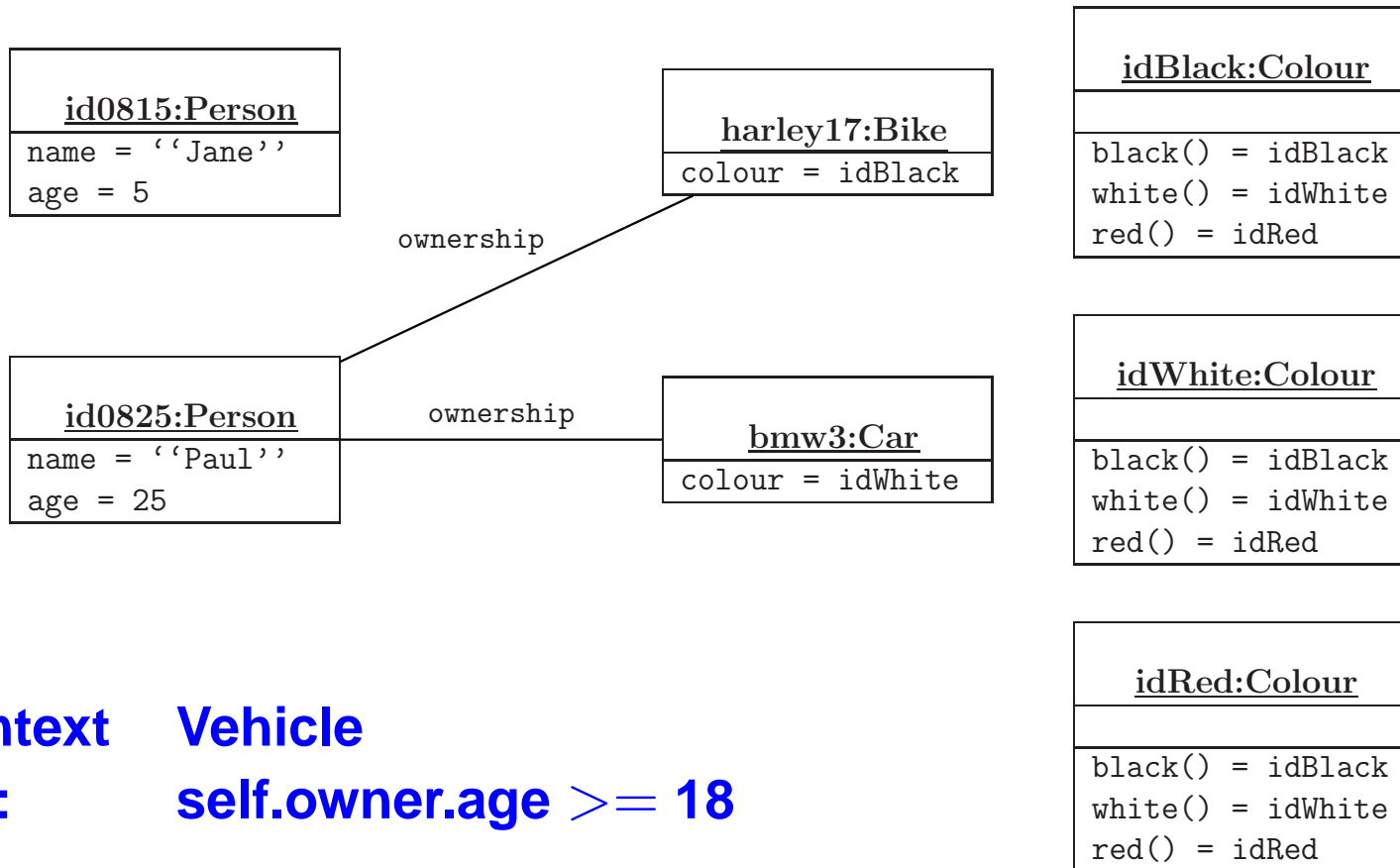
Snapshots and OCL Constraints

- OCL constraints evaluated relative to a snapshot I
(Recall that snapshot determines an object diagram)
- OCL expressions have type **Boolean** \Rightarrow they are true or false wrt I
- OCL constraints restrict legal snapshots of UML diagram
Possibility to express intended semantics of diagram
- OCL expressions can be evaluated and checked wrt given snapshot
- Don't give formal semantics of OCL in terms of snapshots
Tell later how UML/OCL is translated into FOL/DL

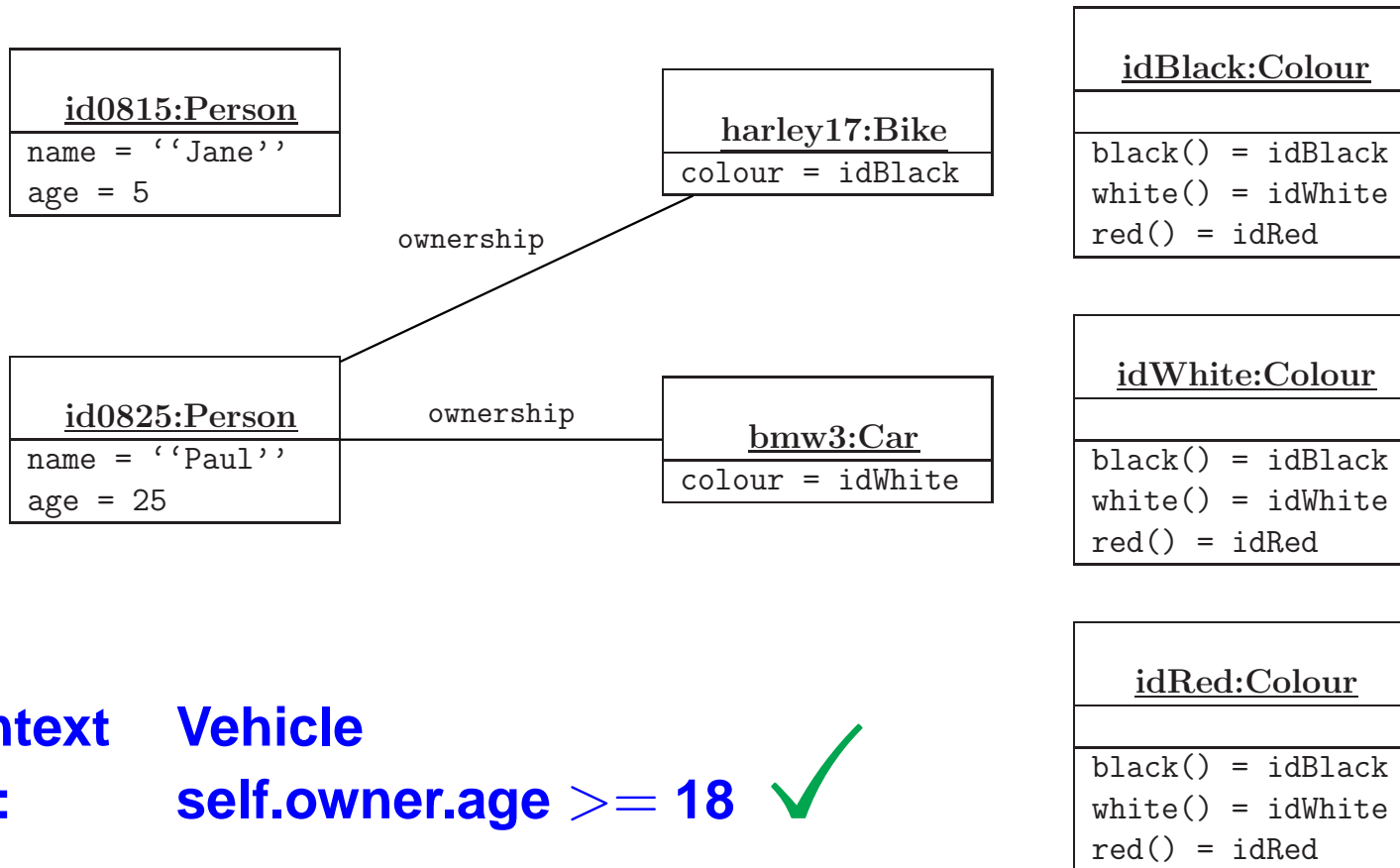
Object Diagrams and OCL Constraints



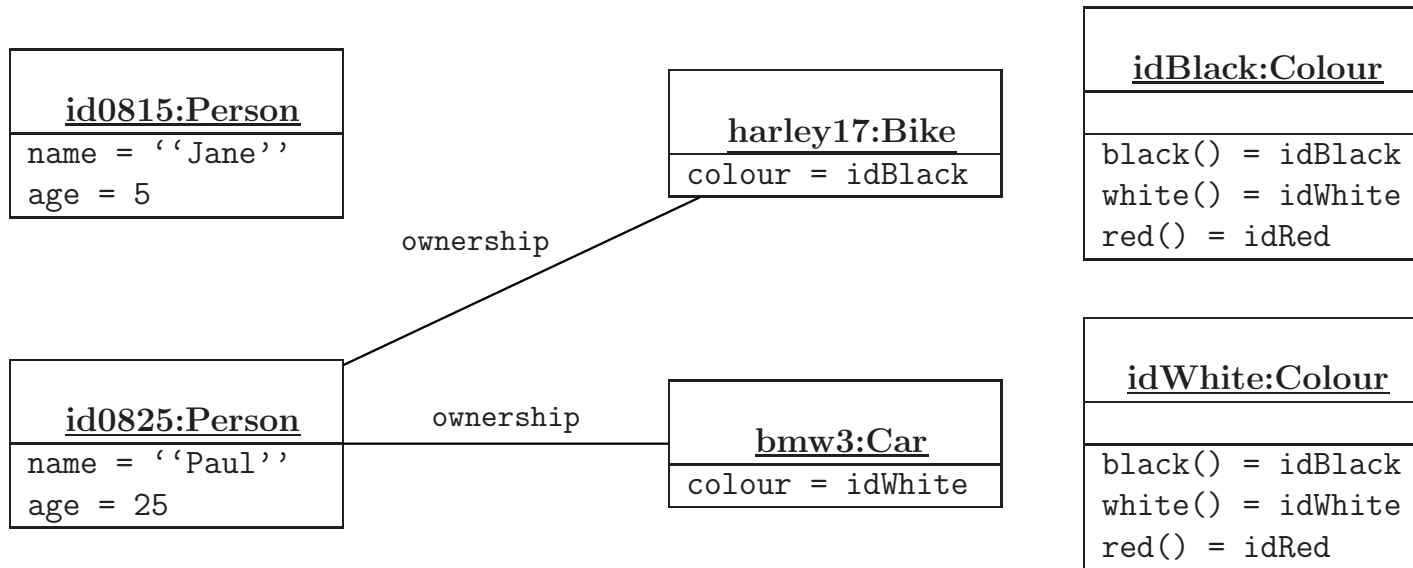
Object Diagrams and OCL Constraints



Object Diagrams and OCL Constraints



Object Diagrams and OCL Constraints



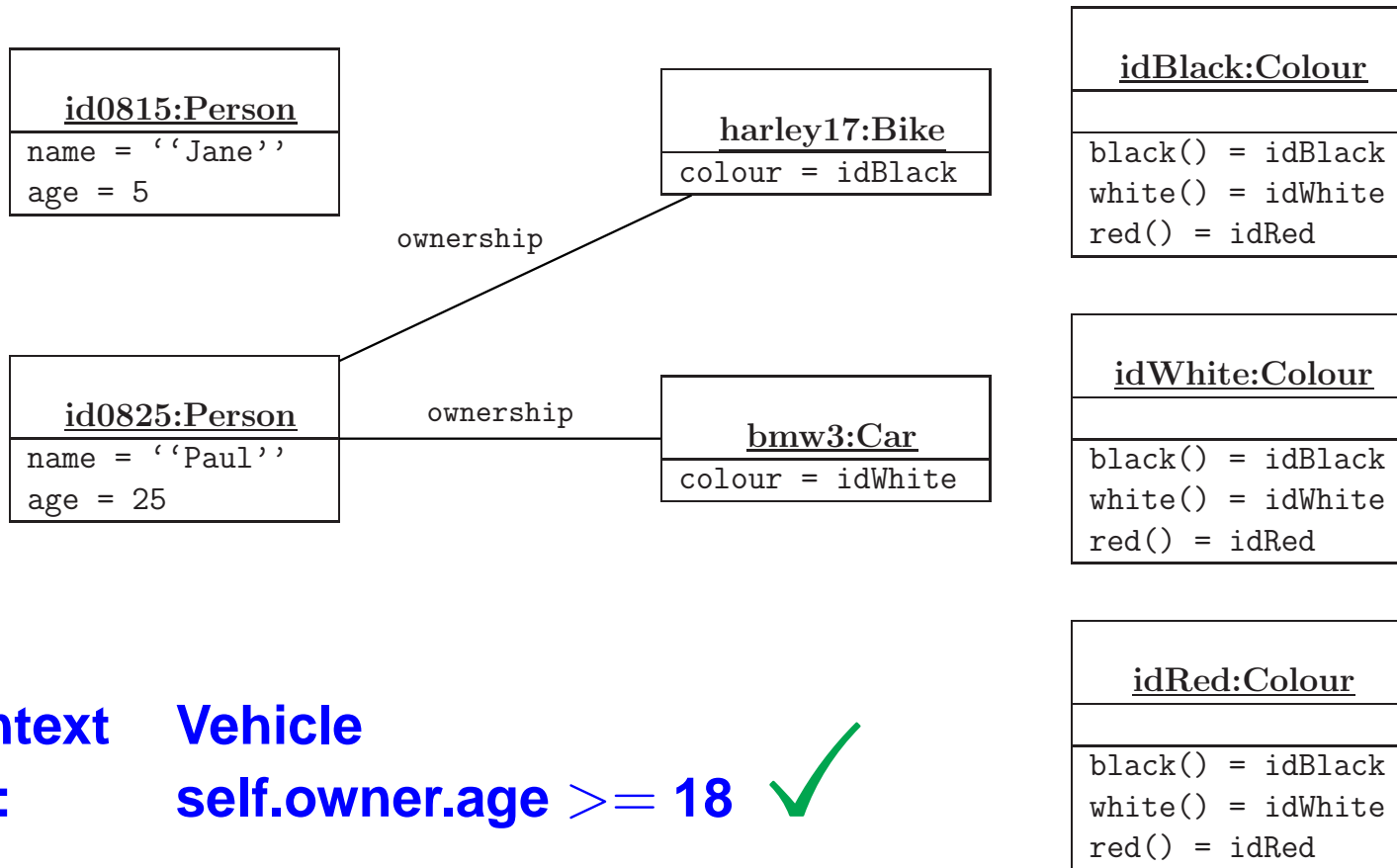
context Vehicle

inv: self.owner.age \geq 18 ✓

context Person

inv: fleet \rightarrow forAll(colour = Colour.black)

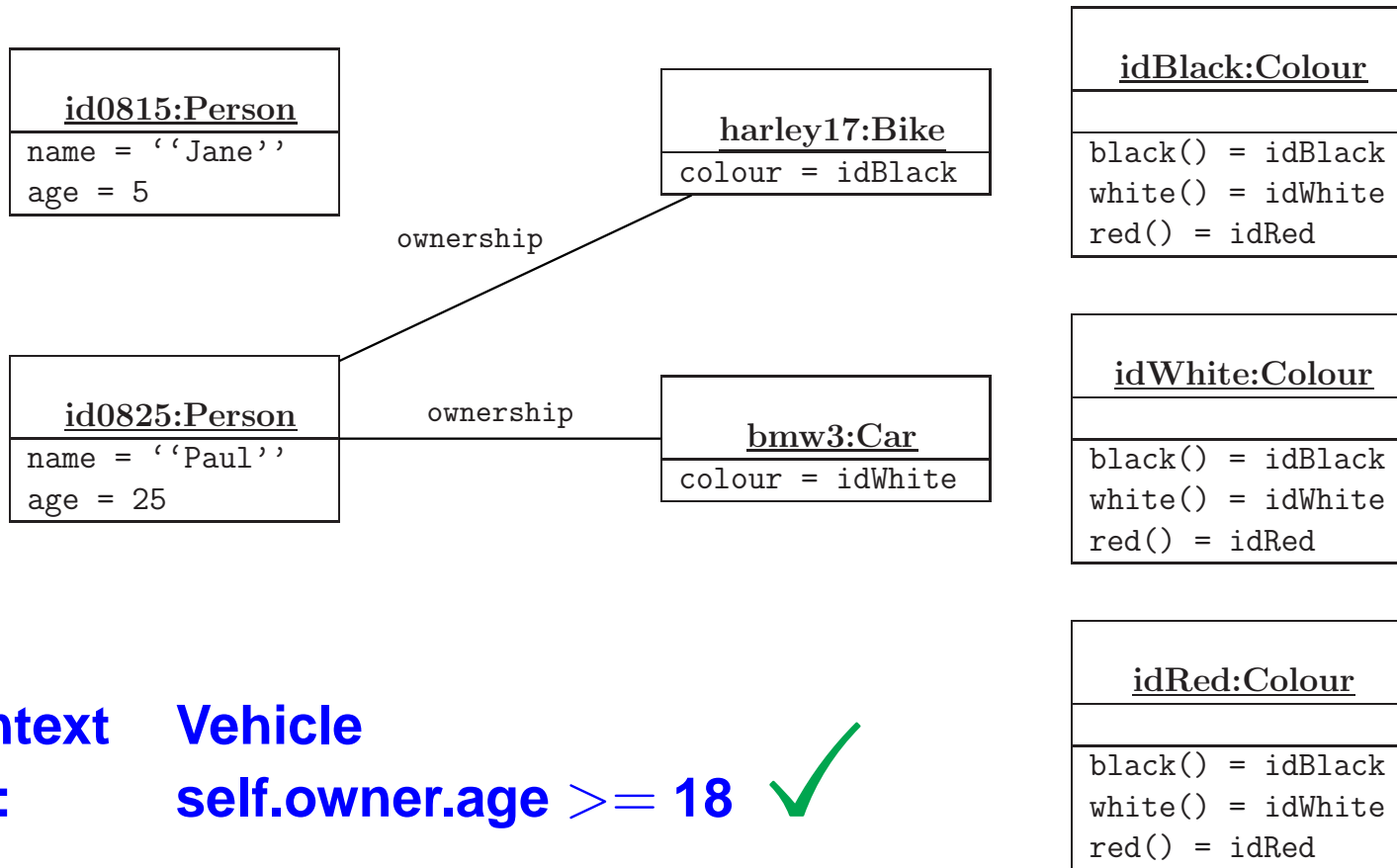
Object Diagrams and OCL Constraints



context Vehicle
inv: self.owner.age >= 18 ✓

context Person
inv: fleet->forAll(colour = Colour.black) ✗

Object Diagrams and OCL Constraints



context Vehicle

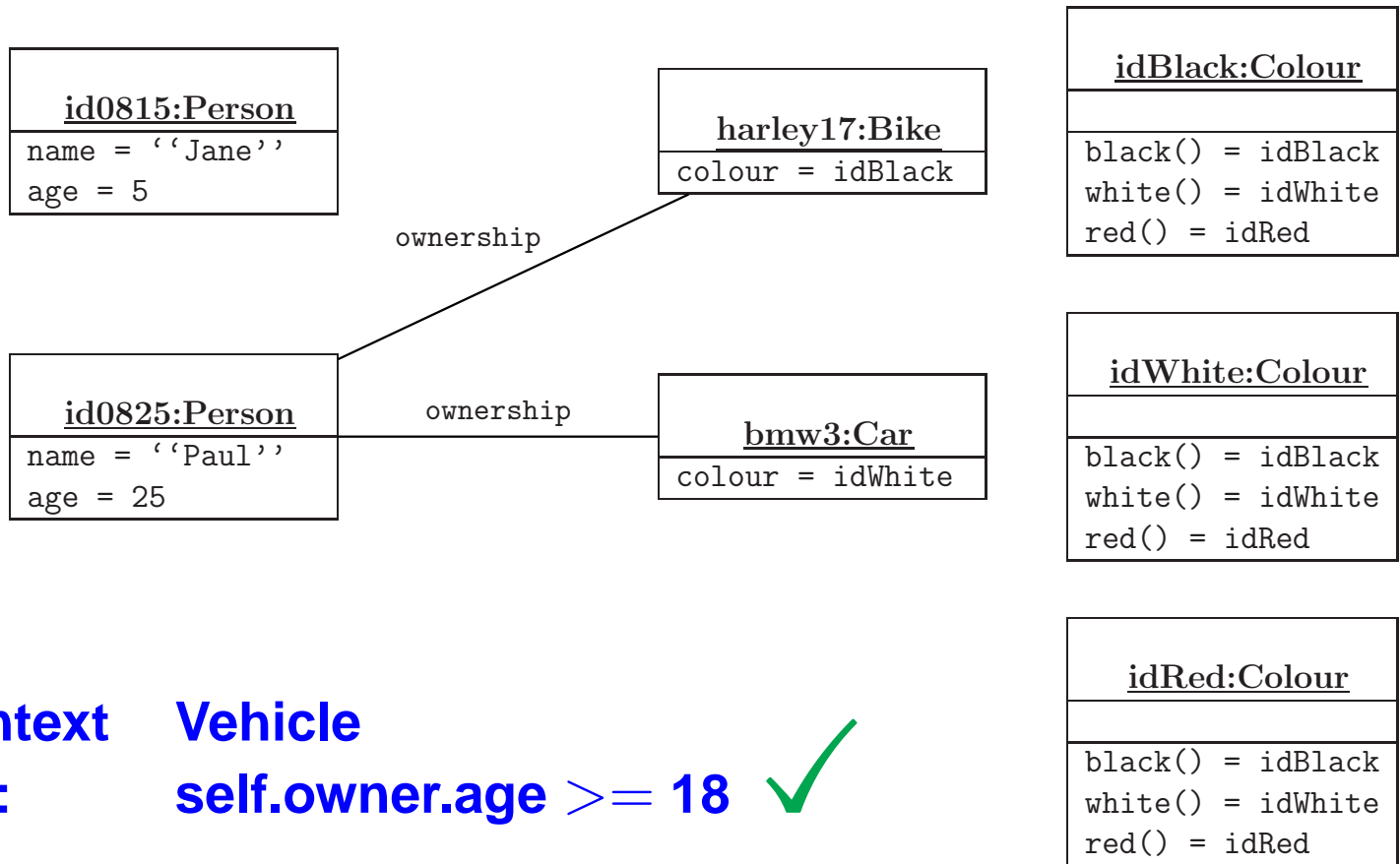
inv: self.owner.age \geq 18 ✓

context Person

inv: fleet \rightarrow forAll(colour = Colour.black) ✗

inv: fleet \rightarrow select(colour = Colour.black) \rightarrow size() \leq 3

Object Diagrams and OCL Constraints



context Vehicle

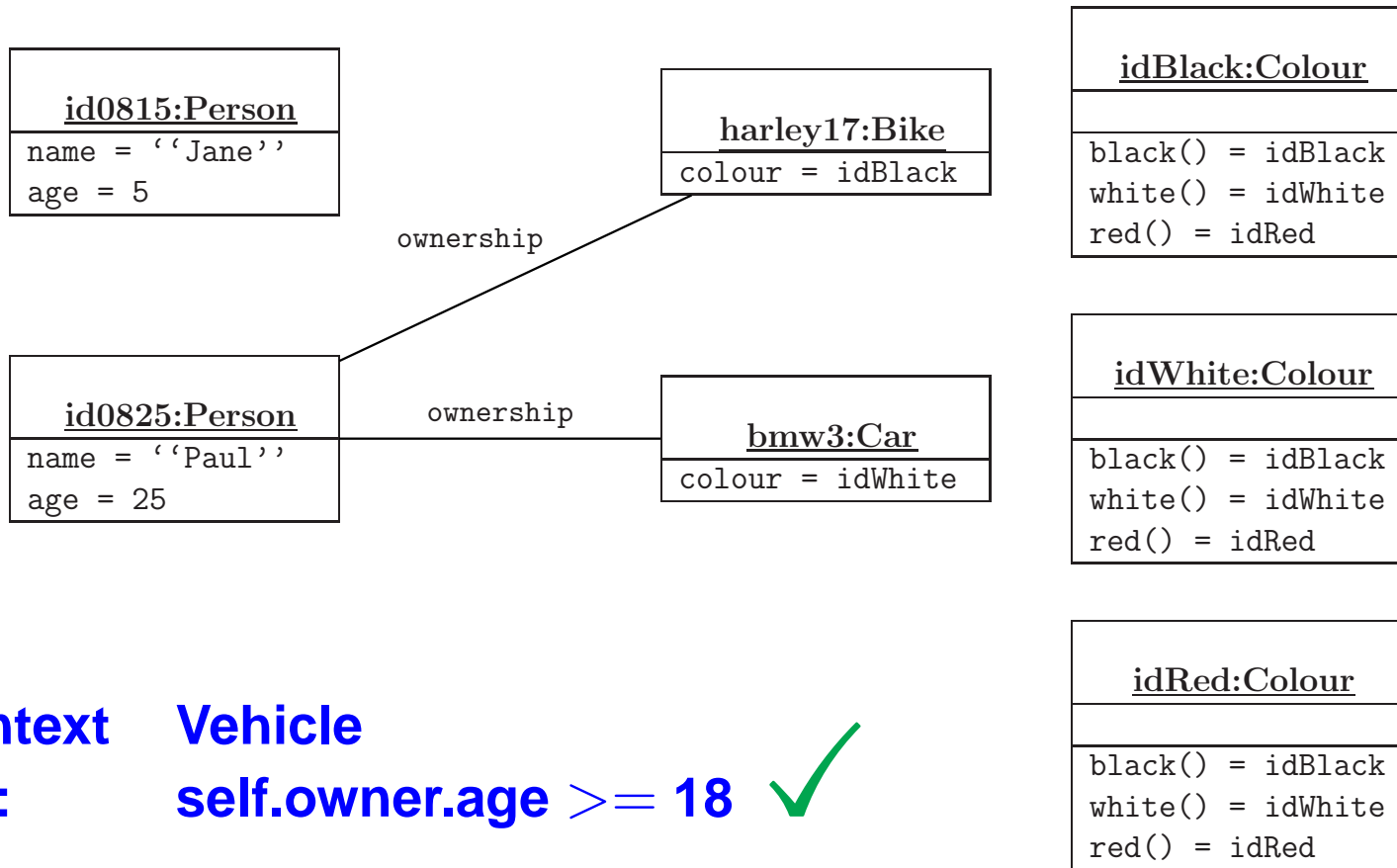
inv: self.owner.age \geq 18 ✓

context Person

inv: fleet \rightarrow forAll(colour = Colour.black) ✗

inv: fleet \rightarrow select(colour = Colour.black) \rightarrow size() \leq 3 ✓

Object Diagrams and OCL Constraints



context Vehicle

inv: self.owner.age >= 18 ✓

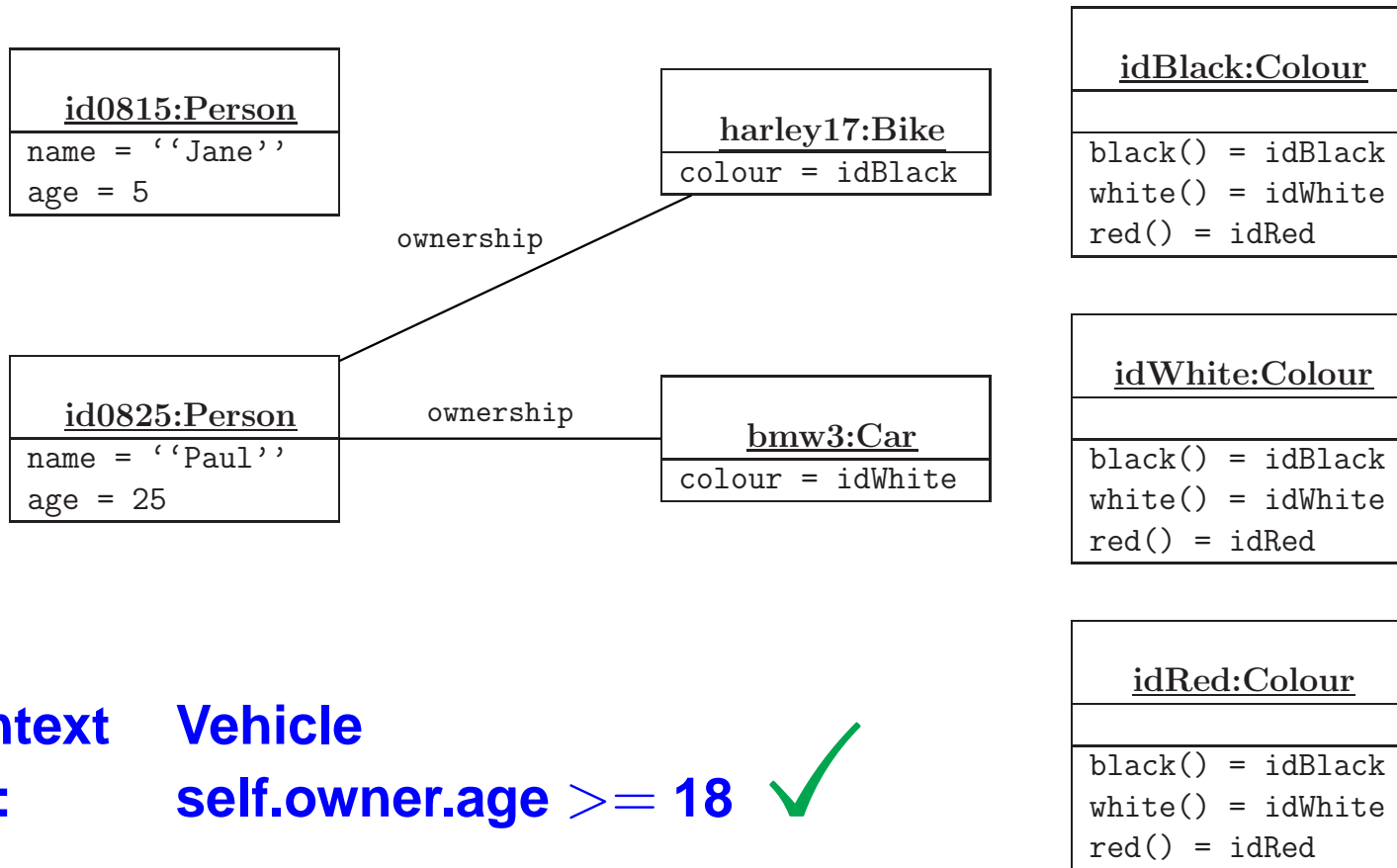
context Person

inv: fleet->forAll(colour = Colour.black) ✗

inv: fleet->select(colour = Colour.black) ->size() <= 3 ✓

inv: Car.allInstances ->exists(colour = Colour.red)

Object Diagrams and OCL Constraints



context Vehicle

inv: self.owner.age \geq 18 ✓

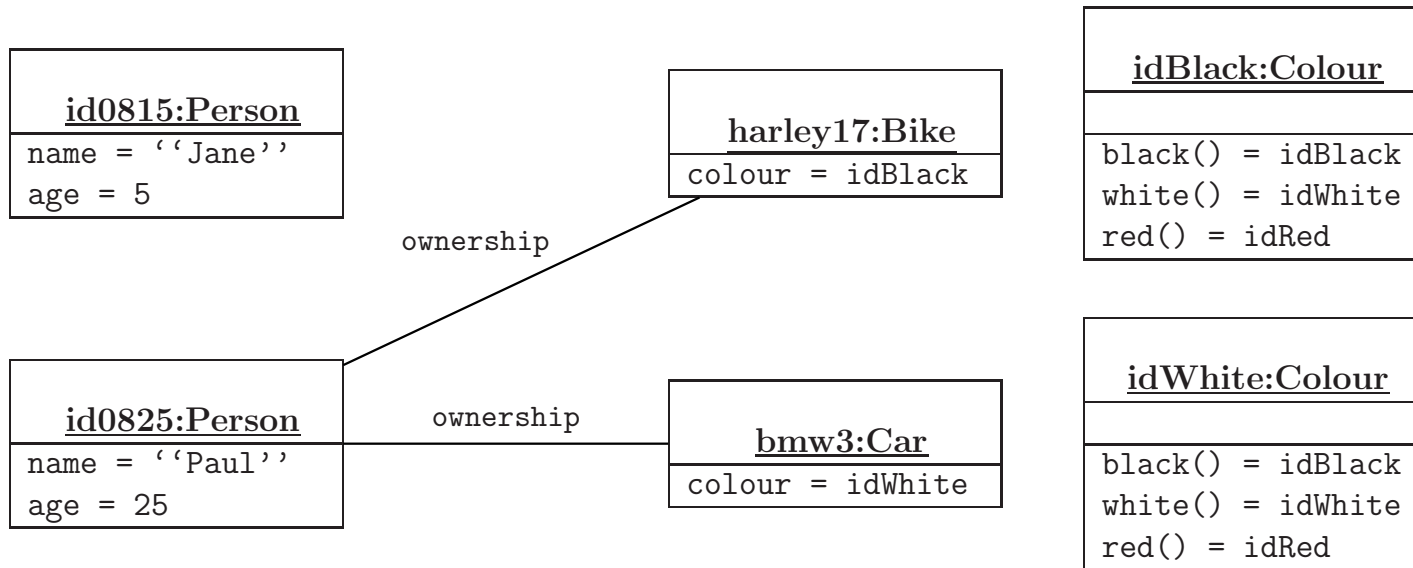
context Person

inv: fleet \rightarrow forAll(colour = Colour.black) ✗

inv: fleet \rightarrow select(colour = Colour.black) \rightarrow size() \leq 3 ✓

inv: Car.allInstances \rightarrow exists(colour = Colour.red) ✗

Object Diagrams and OCL Constraints



context Person::getName()
post: result = name ?

context Person::birthDay()
pre: age \geq 0
post: age = age@pre + 1 ?

Why (Formal) Specification?

Importance of Requirements Specification

Advantages of formal requirements spec **before** implementation:

- No need to decide on algorithm, but sufficient to describe result
- Parts of behaviour can be left open (**underspecification**)
- Possibility of code generation, platform/technology independency
model-driven development
- Formalisation exhibits bugs & missing requirements in early stage

Two independent **formal** models (specification, code):

- Possibility of formal verification
- Find more bugs
- More trust in resulting system