

The University of Iowa

Fall 2020

CS:5810

Formal Methods in Software Engineering

# Introduction

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## A TRUISM

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### Software has become critical to modern life

- **Communication** (internet, voice, video, ...)
- **Transportation** (air traffic control, avionics, cars, ...)
- **Health Care** (patient monitoring, device control, ...)
- **Finance** (automatic trading, banking, ...)
- **Defense** (intelligence, weapons control, ...)
- **Manufacturing** (precision milling, assembly, ...)
- **Process Control** (oil, gas, water, ...)
- ...

# EMBEDDED SOFTWARE

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Software is now embedded everywhere



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Some of it is **critical**



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**Failing software costs money and life!**

# SOFTWARE SYSTEMS ARE GROWING VERY LARGE

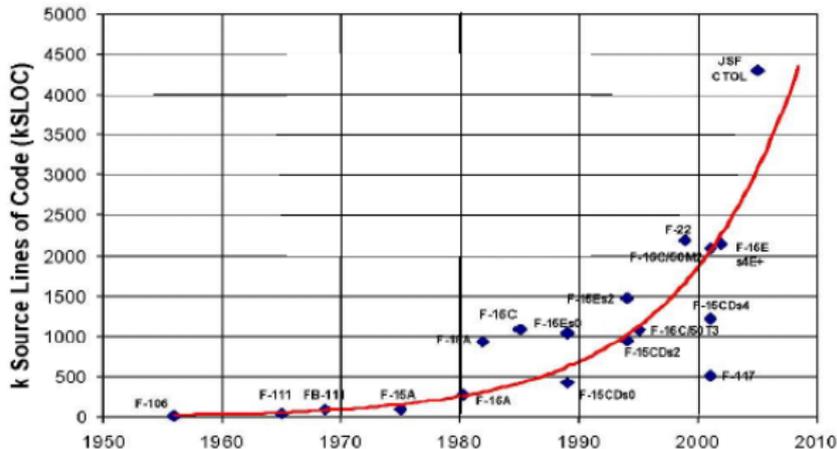


U.S. AIR FORCE

DoD software is growing in size and complexity



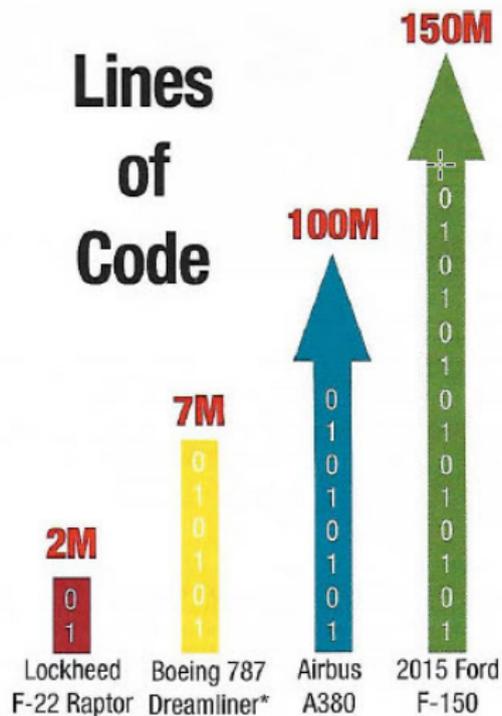
Total Onboard Computer Capacity (OFP)



Source: "Avionics Acquisition, Production, and Sustainment: Lessons Learned -- The Hard Way", NDIA Systems Engineering Conference, Mr. D. Gary Van Oss, October 2002.

Robert Gold, OSD

# SOFTWARE SYSTEMS ARE GROWING VERY LARGE



\* Avionics and online support systems only.

# SOFTWARE SYSTEMS ARE GROWING VERY LARGE

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## Automotive Software

- A typical 2017 car model contains  $\sim 100\text{M}$  lines of code:  
how do you verify that?
- Current cars admit hundreds of onboard functions:  
how do you cover their combination?  
  
E.g., does braking when changing the radio station and starting the  
windscreen wiper, affect air conditioning?

## FAILING SOFTWARE COSTS MONEY

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- Expensive recalls of products with embedded software
- Lawsuits for loss of life or property damage
  - Car crashes (e.g., Toyota Camry 2005)
- Thousands of dollars for each minute of down-time
  - (e.g., Denver Airport Luggage Handling System)
- Huge losses of monetary and intellectual investment
  - Rocket boost failure (e.g., Ariane 5)
- Business failures associated with buggy software
  - (e.g., Ashton-Tate dBase)

## FAILING SOFTWARE COSTS LIVES

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- Potential problems are obvious:
  - Software used to control nuclear power plants
  - Air-traffic control systems
  - Spacecraft launch vehicle control
  - Embedded software in cars
  
- A well-known and tragic example:  
Therac-25 radiation machine failures

# THE PECULIARITY OF SOFTWARE SYSTEMS

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Software seems particularly prone to **faults**

Tiny faults can have **catastrophic** consequences

- Ariane 5
- Mars Climate Orbiter, Mars Sojourner
- Pentium-Bug
- ...

Rare bugs **can occur**

- avg. lifetime of a passenger plane: 30 years
- avg. lifetime of a car:  $< 10$  years, but already  $> 1.2\text{B}$  cars in 2014

Logic and implementation errors represent **security exploits**

- (too many to mention)

## OBSERVATION

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### **Building software is what most of you will do after graduation**

- You'll be developing systems in the context above
- Given the increasing importance of software,
  - you may be liable for errors
  - your job may depend on your ability to produce reliable systems

**What are the challenges in building reliable and secure software?**

## ACHIEVING RELIABILITY IN ENGINEERING

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### **Some well-known strategies from civil/mechanical engineering:**

- Precise calculations/estimations of forces, stress, etc.
- Hardware redundancy (“make it a bit stronger than necessary”)
- Robust design (single fault not catastrophic)
- Clear separation of subsystems (any airplane flies with dozens of known and minor defects)
- Design follows patterns that are proven to work

## WHY THIS DOES NOT WORK FOR SOFTWARE

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Single bit-flip may change behaviour completely

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- Software designs have very high logic **complexity**
- Most SW engineers are **untrained** in correctness
- **Cost efficiency** more important than reliability
- Design practice for reliable software is **not yet mature**

# HOW TO ENSURE SOFTWARE CORRECTNESS?

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## A Central Strategy: **Testing**

(others: SW processes, reviews, libraries, ...)

## **Testing against inherent SW errors (“bugs”)**

- Design test configurations that hopefully are representative and
- ensure that the system behaves as intended on them

## **Testing against external faults**

- Inject faults (memory, communication) by simulation or radiation

## LIMITATIONS OF TESTING

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- Testing can show the **presence** of errors, but **not** their *absence*  
(exhaustive testing viable only for trivial systems)
- *Representativeness* of test cases/injected faults is **subjective**  
How to test for the unexpected? Rare cases?
- Testing is **labor intensive**, hence **expensive**

# COMPLEMENTING TESTING: FORMAL VERIFICATION

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A Sorting Program:

```
int* sort(int* a) {  
    ...  
}
```

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## A Sorting Program:

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int* sort(int* a) {  
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}
```

## Testing sort:

- $\text{sort}(\{3, 2, 5\}) == \{2, 3, 5\}$  ✓
- $\text{sort}(\{\}) == \{\}$  ✓
- $\text{sort}(\{17\}) == \{17\}$  ✓

## COMPLEMENTING TESTING: FORMAL VERIFICATION

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### A Sorting Program:

```
int* sort(int* a) {  
    ...  
}
```

### Testing `sort`:

- `sort({3,2,5}) == {2,3,5}` ✓
- `sort({}) == {}` ✓
- `sort({17}) == {17}` ✓

### Typically missed test cases

- `sort({2,1,2}) == {1,2,2}` ☒
- `sort(null) == exception` ☒
- `isPermutation(sort(a),a)` ☒

## FORMAL VERIFICATION AS THEOREM PROVING

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**Theorem (Correctness of `sort`)** For any given non-null int array `a`, calling the program `sort(a)` returns an int array that is sorted wrt  $\leq$  *and is a permutation of* `a`.

## FORMAL VERIFICATION AS THEOREM PROVING

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**Theorem (Correctness of `sort`)** For any given non-null int array  $a$ , calling the program `sort(a)` returns an int array that is sorted wrt  $\leq$  and is a permutation of  $a$ .

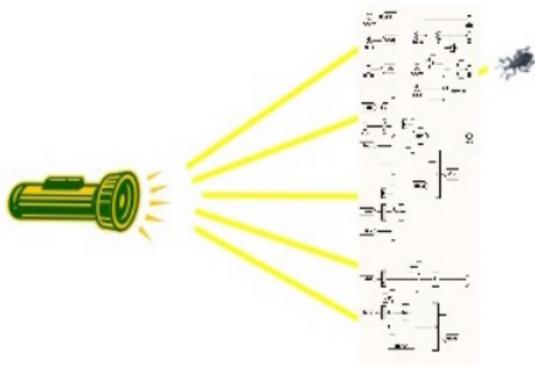
However, methodology differs from mathematics:

1. **Formalize** the expected property in a **logical language**
2. **Prove** the property with the help of an **(semi-)automated tool**

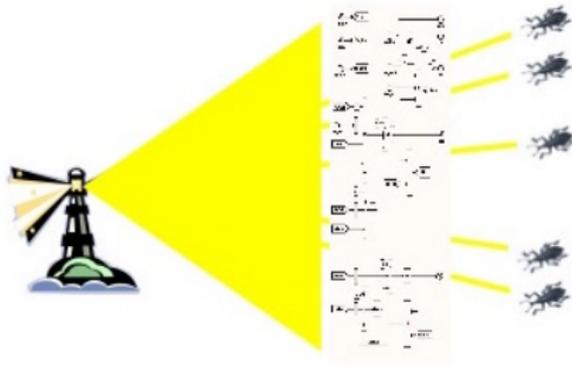
# CONTRASTING TESTING WITH FORMAL VERIFICATION

**Testing Checks Only the Values We Select**

**Formal Verification Checks Every Possible Value!**



**Even Small Systems Have Trillions  
(of Trillions) of Possible Tests!**



**Finds every exception to the  
property being checked!**

## FORMAL METHODS

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**Rigorous** techniques and tools for the **development and analysis** of computational (hardware/software) systems

- Applied at various stages of the development cycle
- Also used in reverse engineering to model and analyze existing systems
- Based on **mathematics and symbolic logic** (formal)

# MAIN ARTIFACTS IN FORMAL METHODS

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1. System requirements
2. System implementation

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Formal methods rely on

- a. some formal specification of (1)
- b. some formal execution model of (2)

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1. System **requirements**
2. System **implementation**

Formal methods rely on

- a. some **formal specification** of (1)
- b. some **formal execution model** of (2)

They use tools to verify **mechanically** that implementation satisfies (a) according to (b)

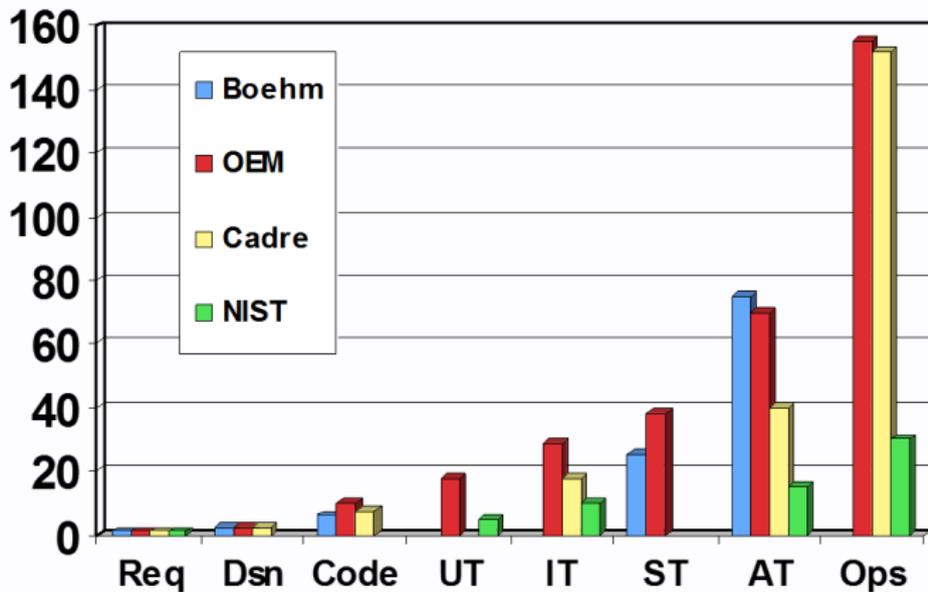
## WHY USE FORMAL METHODS

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- **Contribute to the overall quality** of the final product thanks to mathematical modeling and formal analysis
- **Increase confidence** in the correctness/robustness/security of a system
- **Find more flaws** and **earlier** (i.e., during specification and design vs. testing and maintenance)

## WHY USE FORMAL METHODS

Relative cost to fix an error, by development phase



Finding errors earlier reduces development costs

## FORMAL METHODS: THE VISION

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- **Complement** other analysis and design methods
- Help **find bugs** in code **and** specification
- **Reduce** development, and testing, **cost**
- **Ensure** certain **properties** of the formal system model
- Should be highly automated

## FORMAL METHODS AND TESTING

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- Run the system at chosen inputs and observe its behavior
  - Randomly chosen
  - Intelligently chosen (by hand: **expensive!**)
  - Automatically chosen (need **formalized spec**)
- What about other inputs? (test **coverage**)
- What about the observation? (test **oracle**)

Challenges can be addressed by/require formal methods

## A WARNING

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- The notion of “formality” is often misunderstood (formal vs. rigorous)
- The effectiveness of FMs is still debated
- There are persistent myths about their practicality and cost
- FMs are not yet as widespread in industry as they could be
- They are mostly used in the development of safety-, business-, or mission-critical software, where the cost of faults is high

## THE MAIN POINT OF FORMAL METHODS IS NOT

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- To show “correctness” of entire systems
  - What **is** correctness? Go for specific properties!
- To replace testing entirely
  - Formal methods do not go below byte code level
  - Some properties are not formalizable
- To replace good design practices

There is no silver bullet!

No correct system w/o clear requirements & good design

## OVERALL BENEFITS OF USING FORMAL METHODS

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- Forces developers to think systematically about issues
- Improves the quality of specifications, even without formal verification
- Leads to better design
- Provides a precise reference to check requirements against
- Provides documentation within a team of developers
- Gives direction to latter development phases
- Provides a basis for reuse via specification matching
- Can replace (infinitely) many test cases
- Facilitates automatic test case generation

## SPECIFICATIONS: WHAT THE SYSTEM SHOULD DO

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- Individual properties
  - Safety properties: something bad will never happen
  - Liveness properties: something good will happen eventually
  - Non-functional properties: runtime, memory, usability, . . .
- “Complete” behaviour specification
  - Equivalence check
  - Refinement
  - Data consistency
  - . . .

## FORMAL SPECIFICATION

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*The expression in some **formal language** and at some level of **abstraction** of a collection of **properties** that some system should **satisfy** [van Lamsweerde]*

- **formal language:**
  - syntax can be mechanically processed and checked
  - semantics is defined unambiguously by mathematical means
- **abstraction:**
  - above the level of source code
  - several levels possible

## FORMAL SPECIFICATION

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*The expression in some **formal language** and at some level of **abstraction** of a collection of **properties** that some system should **satisfy** [van Lamsweerde]*

- **properties:**
  - expressed in some formal logic
  - have a well-defined semantics
- **satisfaction:**
  - ideally (but not always) decided mechanically
  - based on automated deduction and/or model checking techniques

## FORMALIZATION HELPS TO FIND BUGS IN SPECS

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- Well-formedness and consistency of formal specs are checkable with tools
- Fixed signature (set of symbols) helps spot incomplete specs
- Failed verification of implementation against spec gives feedback on errors
  - in the implementation or
  - in the (formalization of the) spec

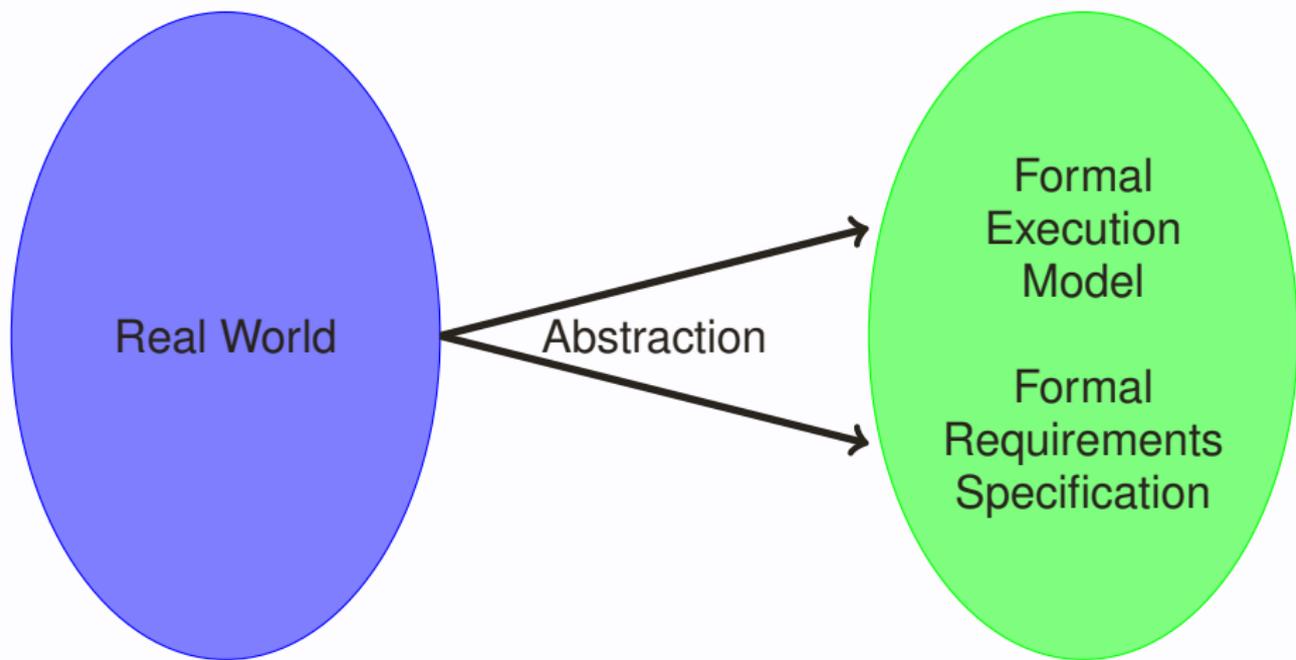
## A FUNDAMENTAL FACT

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Formalisation of system requirements is hard

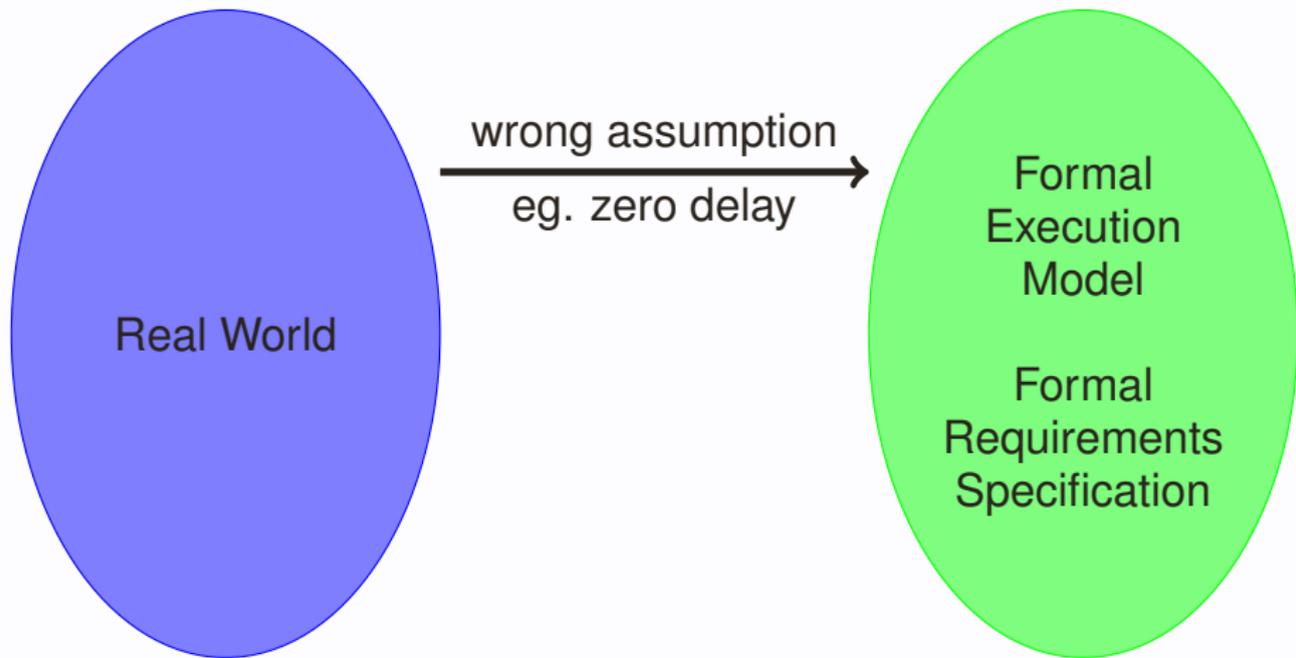
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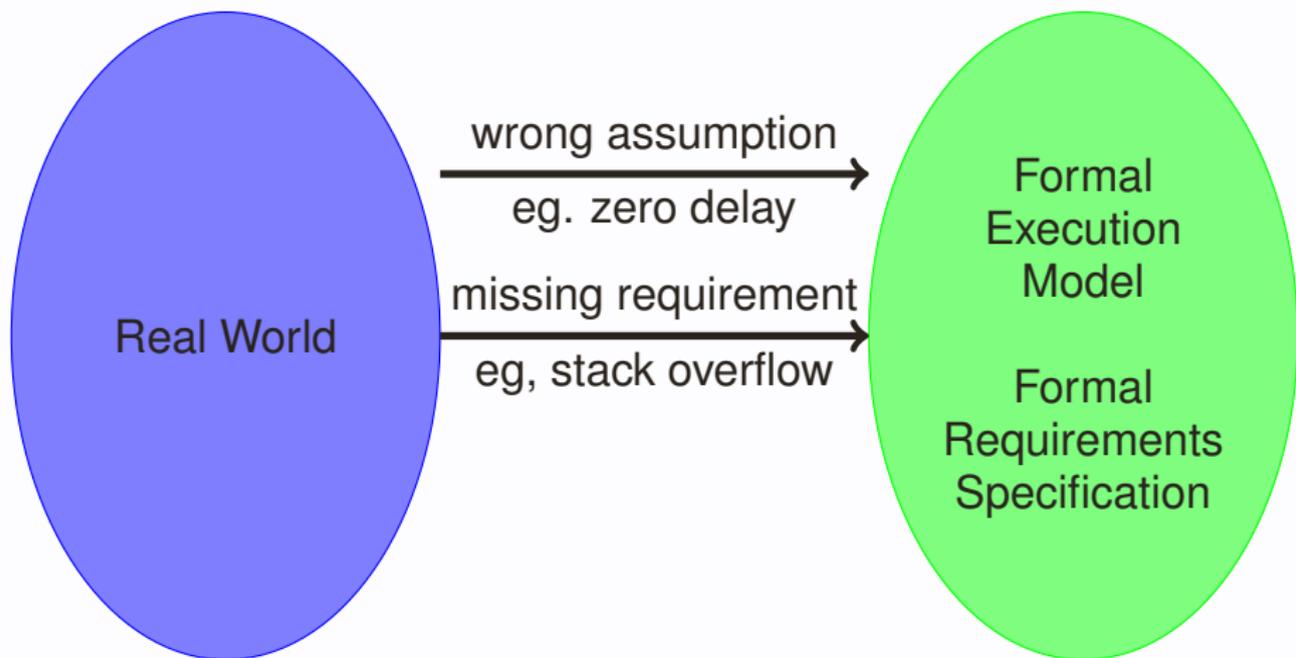
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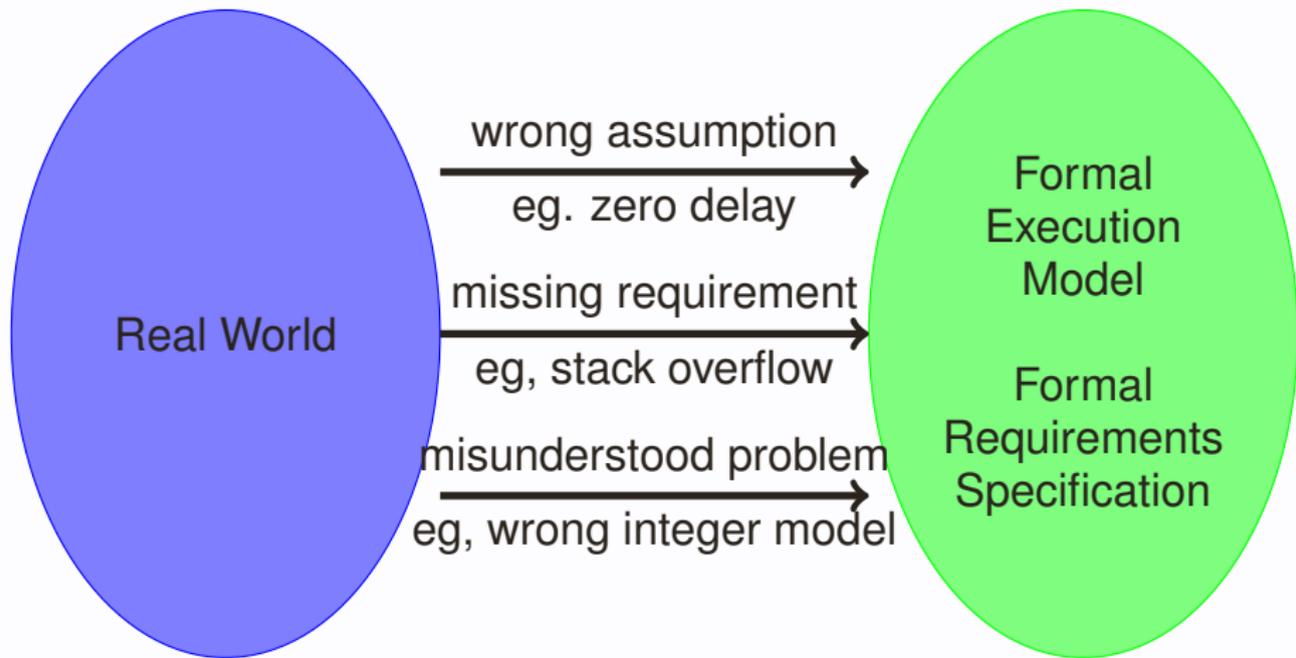
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## ANOTHER FUNDAMENTAL FACT

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Proving properties of systems can be hard

## LEVEL OF SYSTEM DESCRIPTION

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### High level (modeling/programming language level)

- Complex datatypes and control structures, general programs
- Easier to program
- Automatic proofs (in general) impossible!

⋮

### Low level (machine level)

- Finitely many states
- Tedious to program, worse to maintain
- Automatic proofs are (in principle) possible



## EXPRESSIVENESS OF SPECIFICATION

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### High

- General properties
- High precision, tight modeling
- Automatic proofs (in general) impossible!

⋮

### Low

- Finitely many cases
- Approximation, low precision
- Automatic proofs are (in principle) possible



## CURRENT AND FUTURE TRENDS

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Slowly but surely formal methods are finding increased use in industry.

- Designing for formal verification
- Combining semi-automatic methods with SAT/SMT solvers, theorem provers
- Combining static analysis of programs with automatic methods and with theorem provers
- Combining test and formal verification
- Integration of formal methods into SW development process

## CURRENT AND FUTURE TRENDS

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Need for **secure systems** is increasing the use of FMs

- **Security** is intrinsically **hard**
- "Security is to safety as Lucifer is to Murphy"
- Redundant **fault-tolerant** systems are often used to meet safety requirements
- Fault-tolerance depends on the **independence** of component failures
- **Security attacks** are **intelligent, coordinated and malicious**
- Formal methods provides a systematic way to meet stringent security requirements

## SUMMARY

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- Software is becoming pervasive and very complex
- Current development techniques are inadequate
- Formal methods . . .
  - are not a panacea, but will be increasingly necessary
  - are (more and more) used in practice
  - can shorten development time
  - can push the limits of feasible complexity
  - can increase product quality
  - can improve system security
- We will learn to use several different formal methods, for different development stages