HOMEWORK PROB. AND STAT. FOR ENG. (STAT:2020; BOGNAR)

1. A sociologist collected a random sample of 13 statistics majors and 14 sociology majors. The students were asked about how many hours per week they spend socializing. The results are summarized in the following table. Assume that the amount of socialization for statistics majors X_1 follows a normal distribution with mean μ_1 and standard deviation σ_1 (i.e. $X_1 \sim N(\mu_1, \sigma_1)$), while the amount of socialization for sociology majors X_2 follows a normal distribution with mean μ_2 and standard deviation σ_2 (i.e. $X_2 \sim N(\mu_2, \sigma_2)$). Because the sample standard deviations s_1 and s_2 are quite similar, lets make the reasonable assumption that $\sigma_1 = \sigma_2$.

- (a) Find a 95% confidence interval for $\mu_1 \mu_2$.
- (b) Based upon your answer in (1a), is there a significant difference in the mean time spent socializing between statistics and sociology majors? Why?
- (c) Suppose we wish to test $H_0: \mu_1 = \mu_2$ versus $H_a: \mu_1 \neq \mu_2$ at the $\alpha = 0.05$ significance level. Based upon your answer in (1a), will H_0 be rejected? Why?
- (d) Based upon your answer in (1c), will the p-value be less than 0.05 or greater than 0.05? Why?
- (e) Test $H_0: \mu_1 = \mu_2$ versus $H_a: \mu_1 \neq \mu_2$ at the $\alpha = 0.05$ significance level. Find the test statistic and critical value, plot the rejection region, and state your decision and final conclusion.
- (f) Based upon your answer in (1e), is there a significant difference between the average socialization times? Why?
- (g) Approximate the p-value for the test in (1e) using the t-table.
- (h) Use the t-Probability Applet at

http://www.stat.uiowa.edu/~mbognar/applets/t.html

to precisely determine the p-value for the test in (1e).

- (i) Consider the test $H_0: \mu_1 = \mu_2$ versus $H_a: \mu_1 \neq \mu_2$ at the $\alpha = 0.01$ significance level. Based upon your answer in (1g) and (1h), do you reject H_0 ? Why?
- (j) Could we do the above analysis if the study times were not normally distributed? Why?
- 2. The level of iodine in Company A's table salt follows a $N(\mu_1, \sigma_1)$ distribution, while the level in Company B's salt follows a $N(\mu_2, \sigma_2)$ distribution. A random sample of each companies' product yielded

Company A: $n_1 = 16$ $\bar{x}_1 = 22.4$ $s_1 = 1.0$ Company B: $n_2 = 9$ $\bar{x}_2 = 27.5$ $s_2 = 1.4$

Assume that $\sigma_1 = \sigma_2$.

- (a) Test $H_0: \mu_1 = \mu_2$ versus $H_a: \mu_1 < \mu_2$ at the $\alpha = 0.01$ significance level. Find the test statistic and critical value, plot the rejection region, and state your decision and final conclusion.
- (b) Based upon your answer in (2a), is the mean iodine level for Company A significantly lower than Company B? Why?
- (c) Approximate the p-value for the test in (2a) using the t-table.
- (d) Based upon your answer in (2c), is the mean iodine level for Company A significantly lower than Company B? Why?