Assignment Hw2fall14 due 09/11/2014 at 11:59pm CDT

$\begin{array}{lll} \textbf{1.} & (1 & pt) & Library/WHFreeman/Holt_linear_algebra/Chaps_1-4-\\ \textit{/2.2.17.pg} \end{array}$

Find an equation involving vectors that corresponds to the given linear system.

$$2x_1 + 1x_2 + 4x_3 = 8$$

$$\begin{bmatrix} 9x_1 + 8x_2 + 5x_3 = 1 \\ - - \end{bmatrix} x_1 + \begin{bmatrix} - - \\ - - \end{bmatrix} x_2 + \begin{bmatrix} - - \\ - - \end{bmatrix} x_3 = \begin{bmatrix} - - - \\ - - \end{bmatrix}$$

Solution: (Instructor solution preview: show the student solution after due date.)

SOLUTION

$$x_1 \begin{bmatrix} 2 \\ 9 \end{bmatrix} + x_2 \begin{bmatrix} 1 \\ 8 \end{bmatrix} + x_3 \begin{bmatrix} 4 \\ 5 \end{bmatrix} = \begin{bmatrix} 8 \\ 1 \end{bmatrix}$$

Correct Answers:

- 2
- 9
- 1
- 1
- 5
- 8
- 0

2. (1 pt) Library/WHFreeman/Holt_linear_algebra/Chaps_1-4/2.1.7.pg

Express the following vector equation as a system of linear equations.

$$x_1 \begin{bmatrix} 4 \\ 7 \end{bmatrix} + x_2 \begin{bmatrix} 6 \\ 4 \end{bmatrix} = \begin{bmatrix} -9 \\ -6 \end{bmatrix}$$

(Keep the equations in order.)

$$x_1 + x_2 = x_1 + x_2 = x_1 + x_2 = x_2 = x_2 = x_2 = x_2 = x_2 = x_1 + x_2 = x_2$$

Solution: (Instructor solution preview: show the student solution after due date.)

SOLUTION

$$4x_1 + 6x_2 = -9$$
$$7x_1 + 4x_2 = -6$$

Correct Answers:

- 4
- 6
- −9
- 7

- 4
- -6

3. (1 pt) Library/Rochester/setLinearAlgebra3Matrices/ur_la_3_15.pg Find a and b such that

$$\begin{bmatrix} 30 \\ 2 \\ 4 \end{bmatrix} = a \begin{bmatrix} 1 \\ 1 \\ -2 \end{bmatrix} + b \begin{bmatrix} 8 \\ 1 \\ 0 \end{bmatrix}.$$

a = _____

 $b = \underline{\hspace{1cm}}$

Correct Answers:

- −2
- 4

4. (1 pt) Library/Rochester/setLinearAlgebra3Matrices/ur_la_3_15.pg Find a and b such that

$$\begin{bmatrix} -15 \\ -24 \\ -11 \end{bmatrix} = a \begin{bmatrix} 1 \\ 4 \\ 1 \end{bmatrix} + b \begin{bmatrix} 11 \\ 8 \\ 7 \end{bmatrix}.$$

a = _____

b =_____

Correct Answers:

- −4
- −1

$\begin{tabular}{ll} 5. & (1 & pt) & Library/WHFreeman/Holt_linear_algebra/Chaps_1-4-/2.1.23.pg \end{tabular}$

Solve for the unknowns in the vector equation below.

$$1 \begin{bmatrix} a \\ -9 \end{bmatrix} - 3 \begin{bmatrix} 8 \\ b \end{bmatrix} = \begin{bmatrix} -5 \\ -8 \end{bmatrix}$$

 $b = _{---}$

Solution: (Instructor solution preview: show the student solution after due date.)

SOLUTION

$$a = (-5 + 3 * 8)/1 = 19$$

- 19

6. (1 pt) Library/Rochester/setLinearAlgebra3Matrices/ur_la_3_15.pg Find a and b such that

$$\begin{bmatrix} 0 \\ 5 \\ 10 \end{bmatrix} = a \begin{bmatrix} 1 \\ -1 \\ -1 \end{bmatrix} + b \begin{bmatrix} 3 \\ 2 \\ 7 \end{bmatrix}.$$

$$a = \underline{\hspace{1cm}}$$

 $b = \underline{\hspace{1cm}}$

Correct Answers:

- -3
- 1

7. (1 pt) Library/WHFreeman/Holt_linear_algebra/Chaps_1-4/2.1.8.pg

Consider the following vector equation.

$$x_1 \begin{bmatrix} 1 \\ 7 \\ -4 \end{bmatrix} + x_2 \begin{bmatrix} -9 \\ 1 \\ 5 \end{bmatrix} = \begin{bmatrix} 0 \\ 8 \\ 6 \end{bmatrix}.$$

Express the vector equation as a system of linear equations. (Order your equations from the top.)

The first equation is $\underline{\hspace{1cm}} x_1 + \underline{\hspace{1cm}} x_2 \underline{\hspace{1cm}}$.

The second equation is $\underline{\hspace{1cm}} x_1 + \underline{\hspace{1cm}} x_2 \underline{\hspace{1cm}}$.

The third equation is $\underline{\hspace{1cm}} x_1 + \underline{\hspace{1cm}} x_2 \underline{\hspace{1cm}}$.

Solution: (Instructor solution preview: show the student solution after due date.)

SOLUTION

Each row of the vector equation becomes a linear equation. *Correct Answers:*

- 1
- -5
- 0
- /
- 8
- -1
- 5
- 6

$8. \hspace{1.5cm} (1 \hspace{1.5cm} pt) \hspace{1.5cm} Library/WHFreeman/Holt_linear_algebra/Chaps_1-4-/2.1.12.pg \\$

Express the following system of linear equations as a vector equation.

$$9x_1 - 9x_2 - 6x_3 = 3$$

$$2x_1 + 5x_2 - 3x_3 = -6$$

$$5x_1 + 8x_2 + 1x_3 = -1$$

$$\begin{bmatrix} -- \\ -- \end{bmatrix} x_1 + \begin{bmatrix} -- \\ -- \end{bmatrix} x_2 + \begin{bmatrix} -- \\ -- \end{bmatrix} x_3 = \begin{bmatrix} -- \\ -- \end{bmatrix}$$

Solution: (Instructor solution preview: show the student solution after due date.)

SOLUTION

$$\begin{bmatrix} 9 \\ 2 \\ 5 \end{bmatrix} x_1 + \begin{bmatrix} -9 \\ 5 \\ 8 \end{bmatrix} x_2 + \begin{bmatrix} -6 \\ -3 \\ 1 \end{bmatrix} x_3 = \begin{bmatrix} 3 \\ -6 \\ -1 \end{bmatrix}$$

Correct Answers:

- 9
- 2
- 5
- −9
- 5
- 0
- 3
- 1
- 3
- - (
- −1

$9. \hspace{1.5cm} (1 \hspace{1.5cm} pt) \hspace{1.5cm} Library/WHFreeman/Holt_linear_algebra/Chaps_1-4-/2.2.13.pg \\$

Find A, and \mathbf{b} such that $A\mathbf{x} = \mathbf{b}$ corresponds to the given linear system.

$$2x_1 + 1x_2 - 2x_3 = -9$$

$$8x_1 + 5x_2 + 0x_3 = 2$$

$$\left[\begin{array}{ccc} - & - & - \\ - & - & - \end{array}\right] \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = \left[\begin{array}{c} - \\ - \end{array}\right]$$

Solution: (Instructor solution preview: show the student solution after due date.)

SOLUTION

$$\begin{bmatrix} 2 & 1 & -2 \\ 8 & 5 & 0 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = \begin{bmatrix} -9 \\ 2 \end{bmatrix}$$

- 2
- 1
- _ _
- _ _ _
- 5
- -9
- 2

10. (1 pt) Library/TCNJ/TCNJ_MatrixEquations/problem11.pg

The vector
$$\begin{bmatrix} 10 \\ -16 \\ 3 \end{bmatrix}$$
 is a linear combination of the vectors $\begin{bmatrix} -4 \\ 3 \\ 2 \end{bmatrix}$ and $\begin{bmatrix} -6 \\ 8 \\ -8 \end{bmatrix}$ if and only if the matrix equation $A\vec{x} = \vec{b}$ has a solution \vec{x} , where

Correct Answers:

$$\begin{bmatrix} -4 & -6 \\ 3 & 8 \\ 2 & -8 \end{bmatrix}$$

$$\begin{bmatrix} 10 \\ -16 \\ 3 \end{bmatrix}$$

11. (1 pt) local/Library/UI/LinearSystems/mforms.pg

Determine the following equivalent representations of the following system of equations:

$$10x + 6y = 48$$
$$-8x + 8y = -64$$

a. Find the augmented matrix of the system.

b. Find the matrix form of the system.

$$\left[\begin{array}{cc} - & - \\ - & - \end{array}\right] \left[\begin{array}{c} x \\ y \end{array}\right] = \left[\begin{array}{c} - \\ - \end{array}\right]$$

c. Find matrices that satisfy the following matrix equation.

$$x \begin{bmatrix} - \\ - \end{bmatrix} + y \begin{bmatrix} - \\ - \end{bmatrix} = \begin{bmatrix} - \\ - \end{bmatrix}$$

d. The graph below shows the lines determined by the two equations in our system:



Find the coordinates of

$$P = (__,__)$$

Find the coordinates of y-intercept of the red line.

$$A = (0, __)$$

Find the coordinates of x-intercept of the green line.

$$B = (__,0)$$

Correct Answers:

$$\begin{bmatrix} 10 & 6 \\ -8 & 8 \end{bmatrix}$$

$$\begin{bmatrix} 48 \\ -64 \end{bmatrix}$$

$$\left[\begin{array}{c} 10 \\ -8 \end{array} \right]$$

$$\begin{bmatrix} 6 \\ 8 \end{bmatrix}$$

$$\begin{bmatrix} 48 \\ -64 \end{bmatrix}$$

- 6
- -2
- 8
- 8

12. (1 pt) Library/TCNJ/TCNJ_MatrixEquations/problem12.pg

The vector $\begin{bmatrix} 4 \\ -19 \end{bmatrix}$ is a linear combination of the vectors $\begin{bmatrix} -2 \\ -3 \end{bmatrix}$ and $\begin{bmatrix} 6 \\ -8 \end{bmatrix}$ if and only if the matrix equation $A\vec{x} = \vec{b}$ has a solution \vec{x} , where

$$A = \begin{bmatrix} --- & -- \\ -- & -- \end{bmatrix}$$
 and $\vec{b} \begin{bmatrix} --- \\ -- \end{bmatrix}$.

$$\begin{bmatrix} -2 & 6 \\ -3 & -8 \end{bmatrix}$$

$$\begin{bmatrix} 4 \\ -19 \end{bmatrix}$$

$\begin{tabular}{ll} \bf 13. & (1 \ pt) \ Library/WHFreeman/Holt_linear_algebra/Chaps_1-4-/2.2.16.pg \end{tabular}$

Find *A* and **b** such that $A\mathbf{x} = \mathbf{b}$ corresponds to the given linear system.

$$1x_1 - 5x_2 = -6$$

$$-6x_1 + 6x_2 = 2$$

$$\begin{bmatrix} - & - \\ - & - \\ - & - \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = \begin{bmatrix} - \\ - \\ - \end{bmatrix}$$

Solution: (Instructor solution preview: show the student solution after due date.)

SOLUTION

$$\begin{bmatrix} 1 & -5 \\ -6 & 6 \\ 1 & -2 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = \begin{bmatrix} -6 \\ 2 \\ 2 \end{bmatrix}$$

Correct Answers:

- 1
- −5
- -6
- 6
- -
- _ _
- ^
- 2

14. (1 pt) Library/TCNJ/TCNJ_VectorEquations/problem2.pg Write a vector equation

$$\begin{bmatrix} - \\ - \\ - \end{bmatrix} x + \begin{bmatrix} - \\ - \\ - \end{bmatrix} y + \begin{bmatrix} - \\ - \\ - \end{bmatrix} z = \begin{bmatrix} - \\ - \\ - \end{bmatrix}$$

that is equivalent to the system of equations:

$$\begin{cases}
-7x - 3y - 8z &= -9, \\
-x - y + z &= 4, \\
y - 5x - 3z &= 5.
\end{cases}$$

Correct Answers:

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$$\begin{bmatrix} -7 \\ -1 \\ -5 \end{bmatrix}$$

$$\begin{bmatrix} -3 \\ -1 \\ 1 \end{bmatrix}$$

$$\begin{bmatrix} -8 \\ 1 \\ -3 \end{bmatrix}$$

$$\begin{bmatrix} -9 \\ 4 \\ 5 \end{bmatrix}$$

${\bf 15.} \qquad (1\ pt)\ Library/WHFreeman/Holt_linear_algebra/Chaps_1-4-/2.2.20.pg$

Find an equation involving vectors the corresponds to the given linear system.

$$1x_1 + 5x_2 = 9$$

$$-3x_1 + 8x_2 = -2$$

$$\begin{bmatrix} \dots \\ \dots \\ x_1 + \begin{bmatrix} \dots \\ \dots \end{bmatrix} x_2 = \begin{bmatrix} \dots \\ \dots \\ \dots \end{bmatrix}$$

Solution: (Instructor solution preview: show the student solution after due date.)

SOLUTION

$$x_1 \begin{bmatrix} 1 \\ -3 \\ 3 \end{bmatrix} + x_2 \begin{bmatrix} 5 \\ 8 \\ 4 \end{bmatrix} = \begin{bmatrix} 9 \\ -2 \\ 4 \end{bmatrix}$$

- 1
- -3
- 5
- 0
- 4
- ,
- 4