

1. (1 pt) Library/Rochester/setLinearAlgebra17DotProductRn-ur_la_17.6.pg

Find a vector v perpendicular to the vector $u = \begin{bmatrix} 2 \\ -1 \end{bmatrix}$.

$$v = \begin{bmatrix} ______ \\ ______ \end{bmatrix}.$$

2. (1 pt) Library/Rochester/setLinearAlgebra17DotProductRn-ur_la_17.7.pg

Find the value of k for which the vectors

$$x = \begin{bmatrix} -5 \\ -1 \\ -1 \\ 2 \end{bmatrix} \text{ and } y = \begin{bmatrix} 4 \\ 2 \\ -5 \\ k \end{bmatrix} \text{ are orthogonal.}$$

$$k = ______.$$

3. (1 pt) Library/TCNJ/TCNJ_OrthogonalSets/problem9.pg

Given $v = \begin{bmatrix} -9 \\ -5 \end{bmatrix}$, find the coordinates for v in the subspace W spanned by $u_1 = \begin{bmatrix} 6 \\ -1 \end{bmatrix}$ and $u_2 = \begin{bmatrix} -6 \\ -36 \end{bmatrix}$. Note that u_1 and u_2 are orthogonal.

$$v = ______ u_1 + ______ u_2$$

4. (1 pt) Library/Rochester/setLinearAlgebra14TransfOfRn-ur_la_14.18.pg

Let L be the line in \mathbb{R}^3 that consists of all scalar multiples of the

vector $\begin{bmatrix} 1 \\ 2 \\ -2 \end{bmatrix}$. Find the orthogonal projection of the vector

$$v = \begin{bmatrix} 9 \\ 8 \\ 6 \end{bmatrix} \text{ onto } L.$$

$$\text{proj}_L v = \begin{bmatrix} ______ \\ ______ \\ ______ \end{bmatrix}.$$

5. (1 pt) Library/Rochester/setLinearAlgebra18OrthogonalBases-ur_la_18.4.pg

$$\text{Let } x = \begin{bmatrix} 8 \\ 6 \\ 8 \\ 0 \end{bmatrix} \text{ and } y = \begin{bmatrix} 4 \\ -6 \\ -20 \\ 9 \end{bmatrix}.$$

Use the Gram-Schmidt process to determine an orthonormal basis for the subspace of \mathbb{R}^4 spanned by x and y .

$$\begin{bmatrix} ______ \\ ______ \\ ______ \\ ______ \end{bmatrix}, \begin{bmatrix} ______ \\ ______ \\ ______ \\ ______ \end{bmatrix}.$$

6. (1 pt) Library/Rochester/setLinearAlgebra17DotProductRn-ur_la_17.21.pg

$$\text{Let } v_1 = \begin{bmatrix} -0.5 \\ -0.5 \\ 0.5 \\ 0.5 \end{bmatrix}, v_2 = \begin{bmatrix} 0.5 \\ -0.5 \\ 0.5 \\ -0.5 \end{bmatrix}, \text{ and } v_3 = \begin{bmatrix} 0.5 \\ -0.5 \\ -0.5 \\ 0.5 \end{bmatrix}.$$

Find a vector v_4 in \mathbb{R}^4 such that the vectors v_1, v_2, v_3 , and v_4 are orthonormal.

$$v_4 = \begin{bmatrix} ______ \\ ______ \\ ______ \\ ______ \end{bmatrix}.$$

7. (1 pt) Library/Rochester/setLinearAlgebra12Diagonalization-ur_la_12.2.pg

$$\text{Let } M = \begin{bmatrix} 10 & -10 \\ 5 & -5 \end{bmatrix}.$$

Find formulas for the entries of M^n , where n is a positive integer.

$$M^n = \begin{bmatrix} ______ & ______ \\ ______ & ______ \end{bmatrix}.$$

8. (1 pt) Library/Rochester/setLinearAlgebra22SymmetricMatrices-ur_la_22.3.pg

Find the eigenvalues and associated unit eigenvectors of the (symmetric) matrix

$$A = \begin{bmatrix} -3 & -6 \\ -6 & -12 \end{bmatrix}.$$

smaller eigenvalue = $______$,

$$\text{associated unit eigenvector} = \begin{bmatrix} ______ \\ ______ \end{bmatrix},$$

larger eigenvalue = $______$,

$$\text{associated unit eigenvector} = \begin{bmatrix} ______ \\ ______ \end{bmatrix}.$$

The above eigenvectors form an orthonormal eigenbasis for A .