

$g = g_1 g_2 g_3 g_4$

$g = (\alpha_0 g_1 \bar{\alpha}_1)(\alpha_1 g_2 \bar{\alpha}_2)(\alpha_2 g_3 \bar{\alpha}_3)(\alpha_3 g_4 \bar{\alpha}_4)$
 where α_0 and α_4 are constant maps.

$g = (\alpha_0 g_1 \bar{\alpha}_1)(\alpha_1 g_2 \bar{\alpha}_2)(\alpha_2 g_3 \bar{\alpha}_3)(\alpha_3 g_4 \bar{\alpha}_4)$
 where $(\alpha_0 g_1 \bar{\alpha}_1), (\alpha_1 g_2 \bar{\alpha}_2)$ in $\pi_1(U)$ and $(\alpha_2 g_3 \bar{\alpha}_3), (\alpha_3 g_4 \bar{\alpha}_4)$ in $\pi_1(V)$

$g = (\alpha_0 g_1 \bar{\alpha}_1)(\alpha_1 g_2 \bar{\alpha}_2)(\alpha_2 g_3 \bar{\alpha}_3)(\alpha_3 g_4 \bar{\alpha}_4)$
 where $(\alpha_0 g_1 \bar{\alpha}_1)$ in $\pi_1(U)$ and $(\alpha_1 g_2 \bar{\alpha}_2), (\alpha_2 g_3 \bar{\alpha}_3), (\alpha_3 g_4 \bar{\alpha}_4)$ in $\pi_1(V)$

$g = (\alpha_0 g_1 \bar{\alpha}_1)(\alpha_1 g_2 \bar{\alpha}_2)(\alpha_2 g_3 \bar{\alpha}_3)(\alpha_3 g_4 \bar{\alpha}_4)$
 where $(\alpha_0 g_1 \bar{\alpha}_1 \alpha_1 g_2 \bar{\alpha}_2) = (\alpha_0 g_1 g_2 \bar{\alpha}_2)$ in $\pi_1(U)$ and $(\alpha_2 g_3 \bar{\alpha}_3 \alpha_3 g_4 \bar{\alpha}_4)$ in $\pi_1(V)$

$g = (\alpha_0 g_1 \bar{\alpha}_1)(\alpha_1 g_2 \bar{\alpha}_2)(\alpha_2 g_3 \bar{\alpha}_3)(\alpha_3 g_4 \bar{\alpha}_4)$
 where $(\alpha_0 g_1 \bar{\alpha}_1)$ in $\pi_1(U)$ and $(\alpha_1 g_2 g_3 g_4 \bar{\alpha}_4)$ in $\pi_1(V)$

$g = (\alpha_0 g_1 \bar{\beta}_1)(\beta_1 g_2 \bar{\alpha}_2)(\alpha_2 g_3 \bar{\alpha}_3)(\alpha_3 g_4 \bar{\alpha}_4)$
 where $(\alpha_0 g_1 \bar{\beta}_1)$ in $\pi_1(U)$ and $(\beta_1 g_2 g_3 g_4 \bar{\alpha}_4)$ in $\pi_1(V)$

$\pi_1(U) = \langle a, b \rangle$ $[g]_U = b$
 $\pi_1(V) = \{e\}$ $[g]_V = e$ $[g]_{U \cup V} = e$
 $\pi_1(U \cap V) = \langle b \rangle$ $[g]_{U \cap V} = b$

$\pi_1(U \cap V) \xrightarrow{i_U} \pi_1(U)$ $[g]_U = b$
 $\pi_1(U \cap V) \xrightarrow{i_V} \pi_1(V)$ $[g]_V = e$ $[g]_{U \cup V} = e$
 $\pi_1(U \cap V) \xrightarrow{inclusion} \pi_1(X)$ $[g]_{U \cap V} = b$