

**Let  $G$  be a connected graph.**

If  $G =$   $=$  , then  $\lambda(G) =$

In all other cases:

$\lambda(G) =$  the size of a minimal edge cut

$=$  the minimum number of edges one can remove such that the resulting subgraph is disconnected.

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Thm 2.4:  $\lambda(G) \leq \min\{\delta(v) \mid v \in V(G)\}$

Choose  $w \in V(G)$  such that

$$\delta(w) \leq \delta(v) \text{ for all } v \in V(G).$$

I.e., choose  $w \in V(G)$  such that

$$\delta(w) = \min\{\delta(v) \mid v \in V(G)\}$$

Case 1:

Case 2: Let  $E^* = \{e \mid e \text{ is incident to } w\}$

$$= \{\langle w, v \rangle \mid \langle w, v \rangle \in E(G)\}$$

$$= \{\langle w, v \rangle \mid v \in N(w)\}$$

= the set of all edges having  $w$  as one  
of its vertices.

Note  $|E^*| = \delta(w)$ .

Note  $(\{w\}, \emptyset)$  is a component of  $G - E^*$ .

Thus  $G - E^*$  is disconnected since

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$G = (V, E)$  is *k-edge-connected* if removing any set of  $k - 1$  edges in  $G$  does not disconnect it and  $|V| \geq 2$ .

$k$  edge connected implies  $k - 1$  edge connected if  $k > 1$

connected = 1-edge connected

$\lambda(G)$  = edge connectivity of  $G$   
 $= \max\{k \mid G \text{ } k\text{-edge-connected}\}$