

$$f : \mathbf{R} \rightarrow \mathbf{R}$$
$$f(x) = x^2$$

$$g : [0, \infty) \rightarrow \mathbf{R}$$
$$g(x) = x^2$$

$$h : [0, \infty) \rightarrow [0, \infty)$$
$$h(x) = x^2$$

1 : 1

$$x_1 \neq x_2$$

then

$$f(x_1) \neq f(x_2)$$

not 1 : 1

there exists

$$x_1 \neq x_2$$

such that

$$f(x_1) = f(x_2)$$

onto

range = codomain

not onto

range \neq codomain

invertible

Defn: Suppose $f : A \rightarrow B$ is 1:1 function where $A = \text{domain}$, $B = \text{range}$, then its inverse function $f^{-1} : B \rightarrow A$ exists and is defined by

$$f^{-1}(b) = a \text{ if and only if } f(a) = b.$$