

Vertical asymptotes occur when

Horizontal asymptotes occur when

Give an example of a function with two vertical asymptotes

Give an example of a function with a horizontal asymptote.

Draw the graph of a function with the following properties:

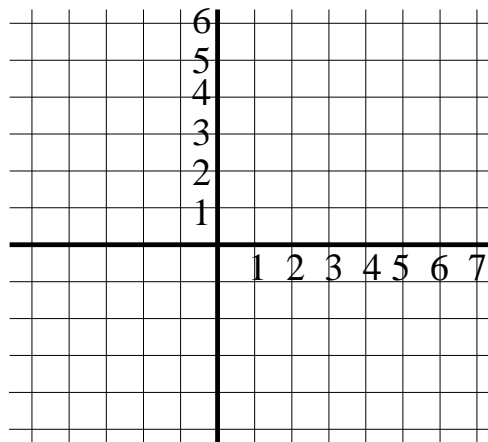
domain =  $(-5, \infty)$ , range =  $(-4, \infty)$

$f$  is continuous everywhere except at 0, 5

$f$  is differentiable everywhere except at 0, 5, 7

$f(0) = 4$ ,  $f'(x) = \frac{2}{3}$  if  $x \in \{-1\} \cup [2, 4]$

$f'(1) = 0$ ,  $f'(x) < 0$  if  $x < -3$ .



Calculate the following limit. Show all steps.

$$\lim_{x \rightarrow -\infty} \frac{x-1}{\sqrt{2-3x^2}}$$

Express the given quantity as a single log:  $3\ln(2x) - \ln(x+1) + \ln(10x^2)$

Find the exact value of  $\ln(\sqrt{e}) + \ln(3e) - \ln(3)$

FYI: derive quotient rule from product and chain rule:

$$\left(\frac{f}{g}\right)' = (fg^{-1})' = f'g^{-1} - fg^{-2}g' = \frac{f'g - fg'}{g^2}$$