

Suppose  $c \in \mathcal{R}$  and suppose  $\lim_{x \rightarrow a} f(x)$  and  $\lim_{x \rightarrow a} g(x)$  exist.

Then

$$\lim_{x \rightarrow a} [f(x) + g(x)] = \lim_{x \rightarrow a} f(x) + \lim_{x \rightarrow a} g(x)$$

$$\lim_{x \rightarrow a} [cf(x)] = c \lim_{x \rightarrow a} f(x)$$

$$\lim_{x \rightarrow a} [f(x)g(x)] = \lim_{x \rightarrow a} f(x) \lim_{x \rightarrow a} g(x)$$

$$\lim_{x \rightarrow a} \frac{f(x)}{g(x)} = \frac{\lim_{x \rightarrow a} f(x)}{\lim_{x \rightarrow a} g(x)} \text{ if } \lim_{x \rightarrow a} g(x) \neq 0$$

Defn:  $f$  is continuous at  $a$

iff  $\lim_{x \rightarrow a} f(x) = f(\lim_{x \rightarrow a} x) =$

If  $f$  is continuous implies

$$\lim_{x \rightarrow a} f(g(x)) = f(\lim_{x \rightarrow a} g(x))$$

Ex:  $\lim_{x \rightarrow 9} e^{\sqrt{x}} - 2\sqrt{x} + 4$

$$\lim_{x \rightarrow 3} \frac{x^2 - 1}{x + 3}$$

$$\lim_{x \rightarrow 3} \frac{x^2 - 1}{x - 3}$$

$$\lim_{x \rightarrow 3} \frac{(x^2 - 1)(x - 3)}{x - 3}$$

$$\lim_{x \rightarrow 3} \frac{x - 3}{x^2 - 1}$$

$$\lim_{x \rightarrow 3} \frac{(x - 4)^2}{x^5 (x - 8)^9 (x - 3)^3}$$

$$\lim_{x \rightarrow 3} \frac{(x - 4)^2 (x - 3)}{x^5 (x - 8)^9 (x - 3)^3}$$

Suppose  $f(x) = \sqrt{x}$ . Find  $\lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$  where  $x > 0$