

Quiz 2 Form A
Sept 15, 2016

[10] 1i. Suppose \$75 is invested at an annual rate of return r compounded continuously. State the initial value problem describing the amount of money after t years.

Differential equation: $y' = ry$ 3 points

Initial Value: $y(0) = 75$ 2 points

1ii. Circle the general solution to the differential equation in problem 1:

D.) $y = Ce^{rt}$ 3 points

1iii. Circle the solution to the initial value problem in problem 1:

D.) $y = 75e^{rt}$ 2 points

[10] 2.) Suppose water containing 3 lbs of salt per gallon enters and leaves a tank at a rate of 8 gallons/hour. Suppose the tank originally contains 7 lbs of salt in 500 gallons of water. State the initial value problem describing the amount of salt in the tank at time t . Do NOT solve.

Differential equation: $Q' = 24 - \frac{8Q}{500}$ or $Q' = 24 - \frac{2Q}{125}$ 7 points

Initial Value: $Q(0) = 7$ 3 points

Let $Q(t)$ = amount of salt (in pounds) in the tanke at time t .

$$\frac{dQ}{dt} = \text{Rate in} - \text{rate out} = \left(\frac{3\text{lbs}}{1\text{gallon}}\right)\left(\frac{8\text{gallons}}{1\text{hour}}\right) - \left(\frac{Q(t)\text{lbs}}{500\text{gallon}}\right)\left(\frac{8\text{gallons}}{1\text{hour}}\right)$$

$$Q' = 24 - \frac{8Q}{500} = 24 - \frac{4Q}{250} = 24 - \frac{2Q}{125}$$