

Quiz 1 Form B

Sept 1, 2017

1.) Determine the order of the given differential equations and also state whether the equation is linear or nonlinear:

[3] 1a.) $ty + y' = 1$ is a first order linear differential equation.

[3] 1b.) $t + yy' = 1$ is a first order nonlinear differential equation.

[14] 2.) Solve and state where the solution is defined: $t^5y' + 5t^4y = \frac{1}{t}$

$$t^5y' + 5t^4y = \frac{1}{t}$$

$$(t^5y)' = \frac{1}{t}$$

$$\int (t^5y)' dt = \int \frac{1}{t} dt$$

$$t^5y = \ln|t| + C$$

$$y = t^{-5}(\ln|t| + c)$$

Solution: $y = t^{-5}(\ln|t| + c)$

Domain: $t \neq 0$ or equivalently $(-\infty, 0) \cup (0, \infty)$