If possible without solving, determine where the solution exists for the following initial value problems:

If not possible without solving, state where in the $t y$-plane, the hypothesis of theorem 2.4.2 is satisfied. In other words, use theorm 2.4.2 to determine where for some interval about $t_{0}$, a solution to IVP, $y^{\prime}=$ $f(t, y), y\left(t_{0}\right)=y_{0}$ exists and is unique.

Example 1: $y^{\prime}=y^{\frac{1}{3}}, y\left(t_{0}\right)=y_{0}$

Example 2: $t y^{\prime}-y=1, y\left(t_{0}\right)=y_{0}$

Example 3: $y^{\prime}=\ln \left|\frac{t}{y}\right|, y(3)=6$

Example 4: $\left(t^{2}-1\right) y^{\prime}-\frac{t^{3} y}{t-4}=\ln |t|, y(3)=6$

