

## Homework II

### 1. [20 points]

Provide the (partial) correctness proof of the program fragment below using the proof rules in chapter 14 of Diller.

```
{INCH ≥ 0}
FOOT := INCH * 12;
YARD := FOOT * 3;
MILE := YARD * 1760
{INCH ≥ 0 ∧ FOOT = INCH * 12 ∧ YARD = INCH * 36 ∧ MILE = INCH * 63360}
```

### 2. [20 points]

Provide the (partial) correctness proof of the program fragment below for absolute value using the proof rules in chapter 14 of Diller.

```
{true}
B := A;
if A < 0 then B := -B else skip
{(A ≥ 0 ∧ B = A) (A < 0 ∧ B = -A)}
```

### 3. [30 points]

Write a program fragment in Diller's language to compute the minimum  $M$  of the four Integer variables  $A$ ,  $B$ ,  $C$ , and  $D$ , and prove its partial correctness using the proof rules in chapter 14. The pre-condition is **true**, and the post-condition is

$$(M = A \ \wedge \ M = B \ \wedge \ M = C \ \wedge \ M = D) \ \wedge \ M \leq A \ \wedge \ M \leq B \ \wedge \ M \leq C \ \wedge \ M \leq D.$$

Of course, your program should not change  $A$ ,  $B$ ,  $C$ , or  $D$ .