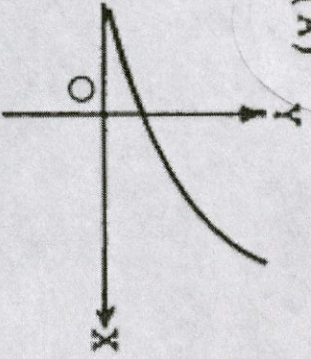
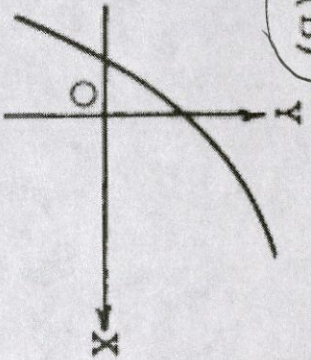


If  $y$  is a function of  $x$  such that  $y' > 0$  for all  $x$  and  $y'' < 0$  for all  $x$ , which of the following could be part of the graph of  $y = f(x)$ ? (A)

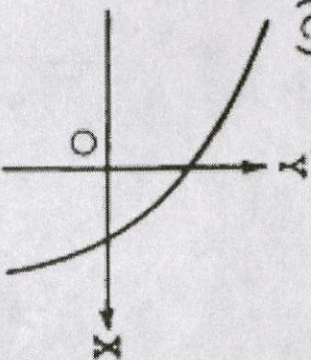
(A)



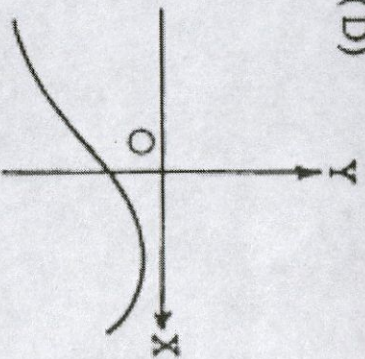
(B)



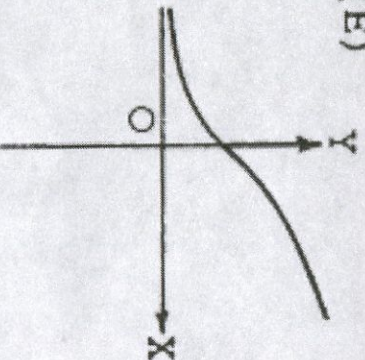
(C)



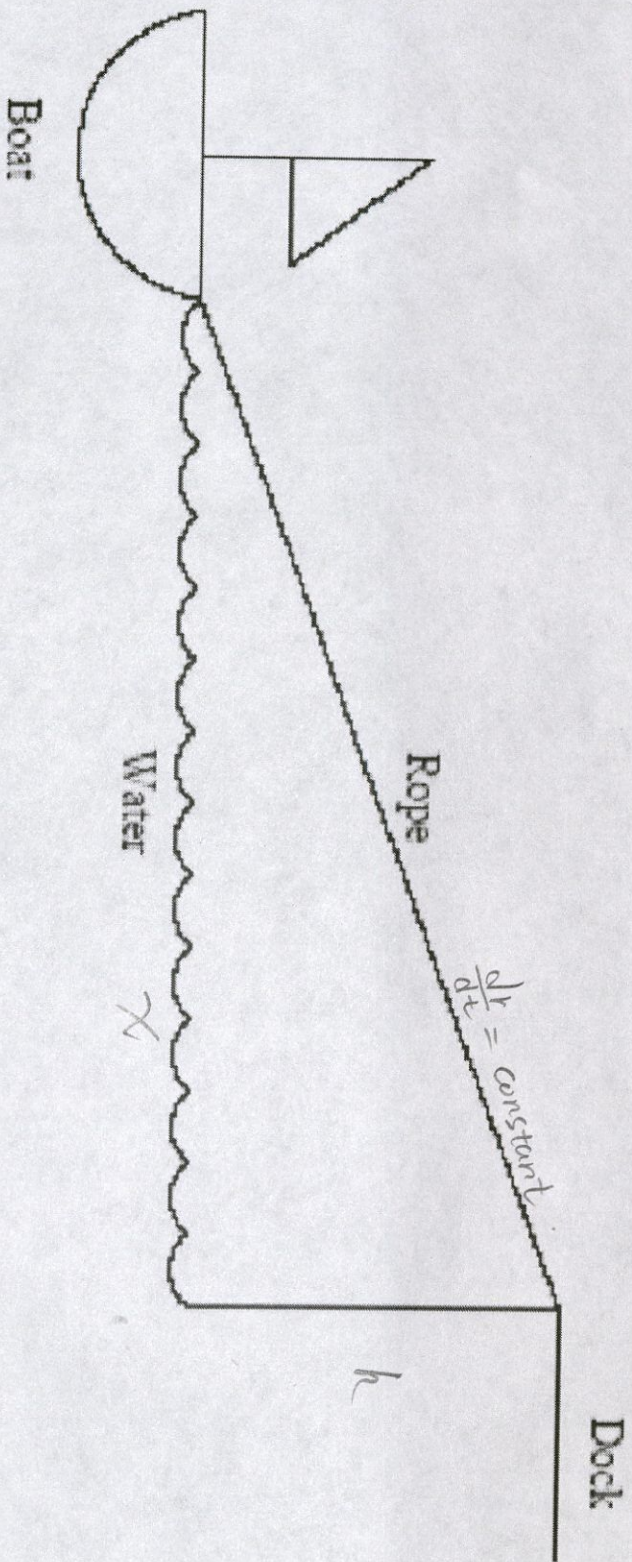
(D)



(E)



4.1.3 [P] A boat is drawn close to a dock by pulling in the rope at a constant rate.  
**True or False.** The closer the boat gets to the dock, the faster it is moving.



$$\sqrt{x^2 + h^2} = r$$

$$\frac{2x}{2\sqrt{x^2 + h^2}} \frac{dx}{dt} = \frac{dr}{dt}$$

$$\Rightarrow \frac{dx}{dt} = \frac{dr}{dt} \cdot \frac{\sqrt{x^2 + h^2}}{x} = \text{constant} \cdot \sqrt{1 + \frac{h^2}{x^2}}$$

$x$  gets smaller,  $\frac{dx}{dt}$  gets bigger.

From: <http://www.ilearnmath.net/help/index.php?page=apexamsmcgoodquestionscalculus>

True or False.  $\frac{d}{dx} \ln(\pi) = \frac{1}{\pi}$

(F)

4.2.1 [Q] True or False. If  $f(x)$  is continuous on a closed interval, then it is enough to look at the points where  $f'(x) = 0$  in order to find its absolute maxima and minima. Be prepared to justify your answer.

(F)

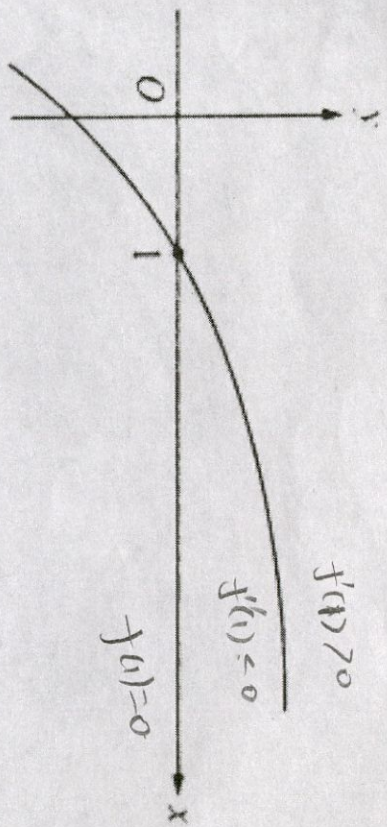
hint: check endpoints and where  $f'(x) = 0$

4.3.3 [Q] If  $f''(a) = 0$ , then  $f$  has an inflection point at  $a$ .

(F)

the concavity should also change.

eg:  $y = x^4$  at  $x = 0$



17. The graph of a twice-differentiable function  $f$  is shown in the figure above. Which of the following is true?

- (A)  $f(1) < f'(1) < f''(1)$
- (B)  $f(1) < f''(1) < f'(1)$
- (C)  $f'(1) < f(1) < f''(1)$
- (D)  $f''(1) < f(1) < f'(1)$
- (E)  $f''(1) < f'(1) < f(1)$

# 17 is from 1998 AP Calc AB

<http://staff.4i.lane.edu/>

[~windom/AP/ap%20multiple](http://windom/AP/ap%20multiple)

[%20choice.pdf](#)

True/False

18.) If  $f$  is continuous, then  $f$  is differentiable.    T    F

19.) If  $f$  is differentiable, then  $f$  is continuous.    T    F

$\lim_{x \rightarrow a} f(x) = f(a)$  if  $f(a)$  is defined.

A) True

B) False

If  $y = f(t)$  represents the miles a car travels after  $t$  hours, then  $f'(t)$  is the velocity of that car.

A) True

B) False

2.2.3 [P] You're trying to guess  $\lim_{x \rightarrow 0} f(x)$ . You plug in  $x = 0.1, 0.01, 0.001, \dots$  and get  $f(x) = 0$  for

all these values. In fact, you're told that for all  $n = 1, 2, \dots$ , we have  $f(1), f\left(\frac{1}{10^n}\right) = 0$ .

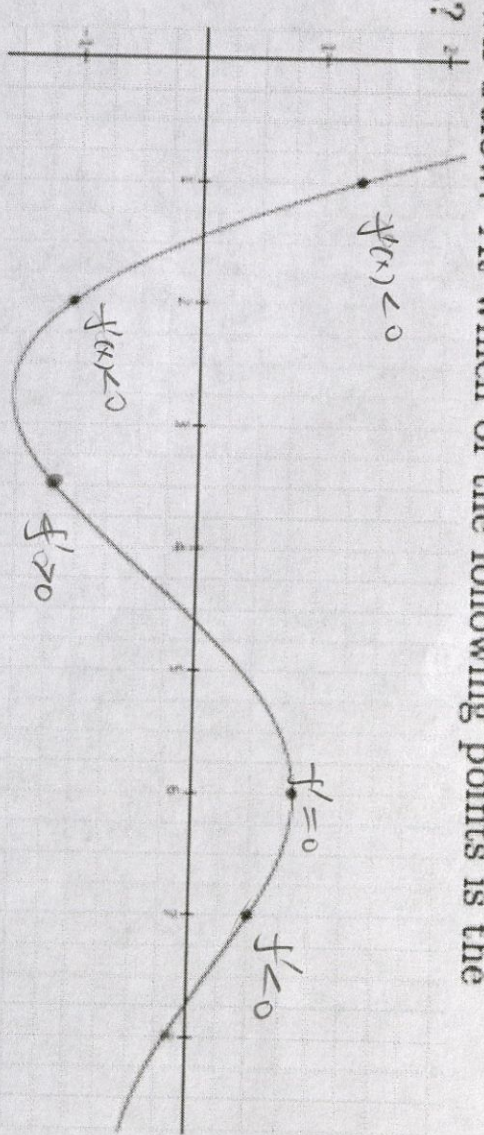
True or False: Since the sequence  $0.1, 0.01, 0.001, \dots$  goes to 0, we know  $\lim_{x \rightarrow 0} f(x) = 0$ .

F

from: [http://www.brandeis.edu/registrar/newstudent/docs/placement/calculus\\_test.pdf](http://www.brandeis.edu/registrar/newstudent/docs/placement/calculus_test.pdf)

7. The graph of a function  $f(x)$  is shown below. At which of the following points is the value of the derivative  $f'(x)$  biggest?

- (a) at  $x = 1$
- (b) at  $x = 2$
- (c) at  $x = 3.5$
- (d) at  $x = 6$
- (e) at  $x = 7$



8. Consider again the function  $f(x)$  whose graph is shown in problem 7. At which points is the second derivative  $f''(x)$  negative?

- (a) at  $x = 2$  and  $x = 3.5$
- (b) at  $x = 1, x = 2$  and  $x = 3.5$
- (c) at  $x = 6$  only
- (d) at  $x = 7$  only
- (e) at  $x = 6$  and  $x = 7$

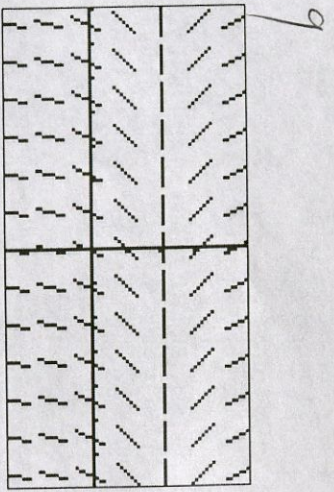
From: <http://www.math.cornell.edu/~GoodQuestions/JittMapleTA.pdf>

When we write  $\lim_{x \rightarrow a} f(x) = \infty$  this means that the limit exists and is a really big number.

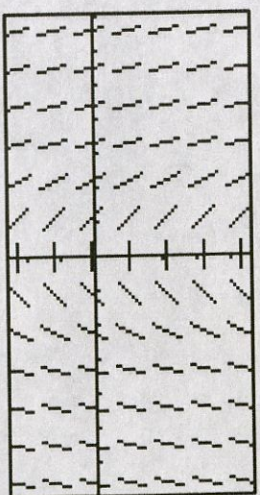
- a.) True
- b.) False

Match the slope fields with their differential equations.

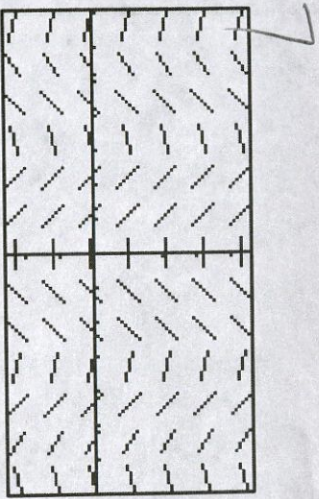
(A)



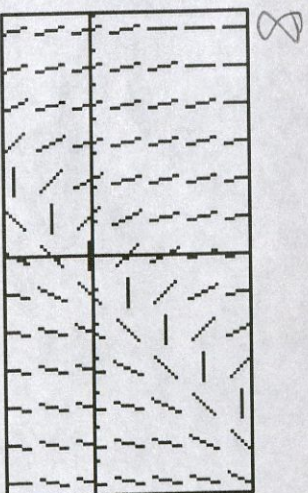
(B)



(C)



(D)



7.  $\frac{dy}{dx} = \sin x$

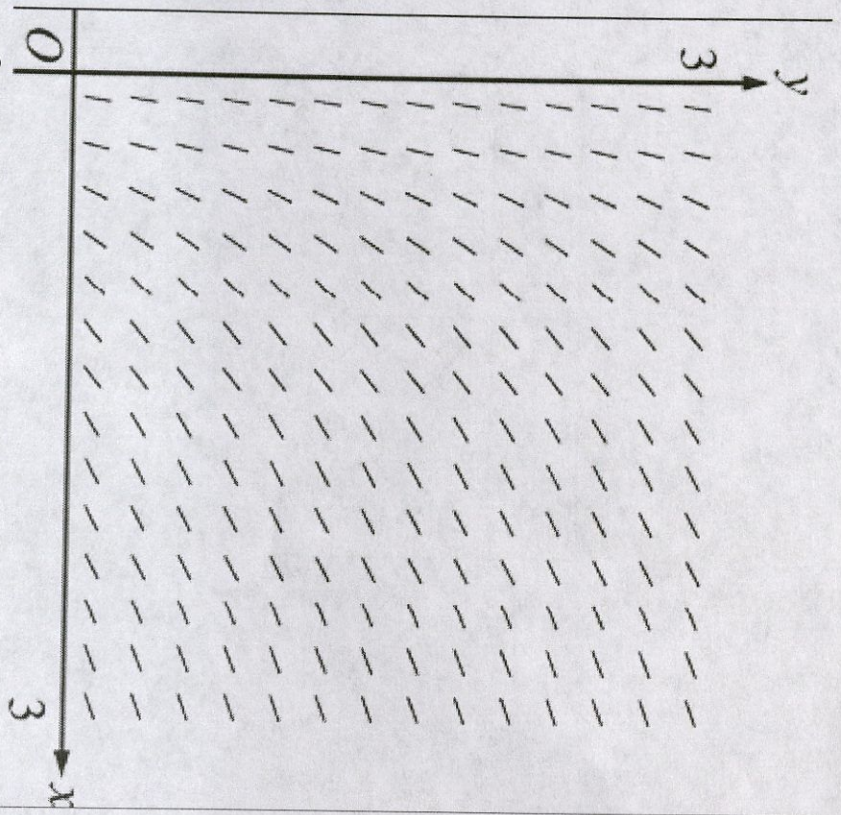
8.  $\frac{dy}{dx} = x - y$

9.  $\frac{dy}{dx} = 2 - y$

10.  $\frac{dy}{dx} = x$

From the May 2008 AP Calculus Course Description:  
15.

From: [http://apcentral.collegeboard.com/apc/public/repository/ap08\\_calculus\\_slopefields\\_worksheet.pdf](http://apcentral.collegeboard.com/apc/public/repository/ap08_calculus_slopefields_worksheet.pdf)



(A)  $y = x^2$

(B)  $y = e^x$

(C)  $y = e^{-x}$

(D)  $y = \cos x$

(E)  $y = \ln x$

The slope field from a certain differential equation is shown above. Which of the following could be a specific solution to that differential equation?

(A)  $y = x^2$

(B)  $y = e^x$

(C)  $y = e^{-x}$

(D)  $y = \cos x$

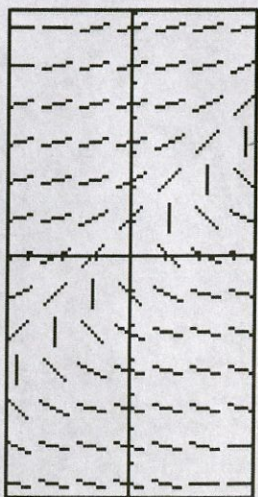
(E)  $y = \ln x$



Match the slope fields with their differential equations.

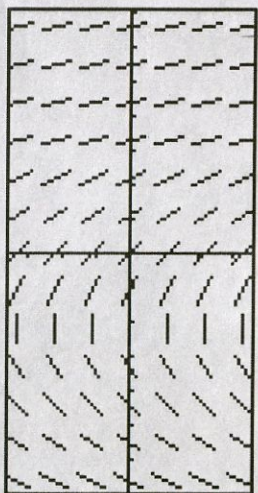
(A)

14



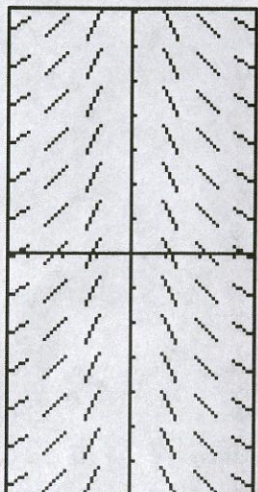
(B)

11



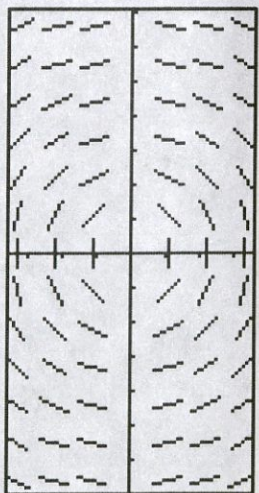
(C)

12



(D)

13



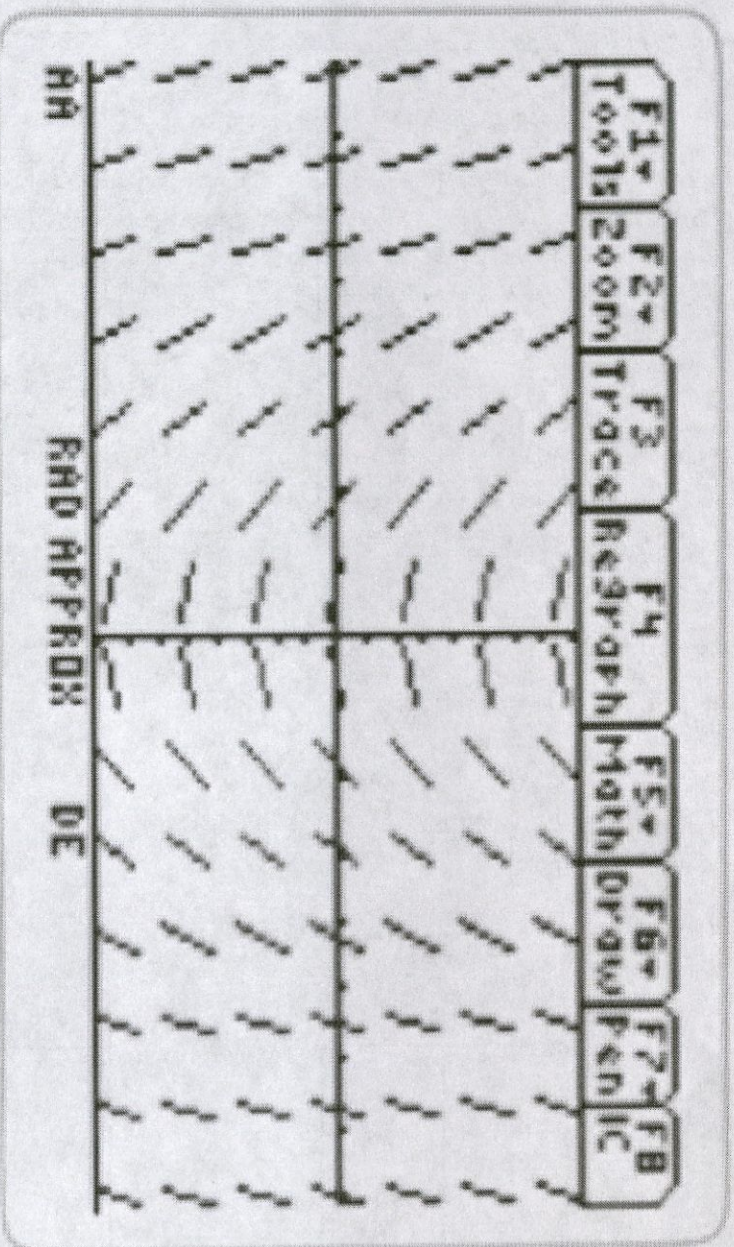
11.  $\frac{dy}{dx} = 0.5x - 1$

12.  $\frac{dy}{dx} = 0.5y$

13.  $\frac{dy}{dx} = -\frac{x}{y}$

14.  $\frac{dy}{dx} = x + y$

7. Which of the following could be a solution of the differential equation with the given slope field?



- (A)  $y = x + 1$                       (D)  $y = \ln(x + 1)$   
 (B)  $y = x^2 + 2$                       (E)  $y = 2e^x$   
 (C)  $y = x^3 - 2$